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Evaluation of KDS 14 Draft Model for One-Way Shear Strength of Slender Concrete Members Reinforced with Fiber-Reinforced Polymer (FRP) Rebars

Ngoc Hieu Dinh¹, Si-Hyun Kim¹ and Kyoung-Kyu Choi^{1*}

Abstract

Currently, the evaluation methods and design codes for predicting the shear strength of FRP-RC members are being continuously developed and updated. The revision draft of the Korean Standard KDS 14 20 22 (KDS 14 draft) adopts the compression zone failure mechanism theory to predict the one-way shear strength of slender steel-reinforced concrete members. This study extends the application of the KDS 14 draft model to slender concrete members reinforced with fiber-reinforced polymer (FRP) rebars. The model performance was evaluated using a comprehensive database of slender FRP-reinforced concrete (RC) specimens, including 304 and 110 specimens without and with FRP stirrups, respectively. The strength prediction of the KDS 14 draft model was compared with those of the existing state-of-the-art international design guidelines and of other recently developed models for FRP-RC members. The KDS 14 draft model demonstrated promising performance over a wide range of design parameters, exhibiting the lowest scatteredness among the evaluated methods. It exhibited a strong correlation with the dataset while maintaining an acceptable level of safety and reliability. Among the investigated design models, the ACI 440.11-22 design method exhibited the highest scatteredness and conservatism for specimens without FRP stirrups. However, the JSCE model provided overly conservative predictions for specimens with FRP stirrups because of the rigorous adoption of a strain limit for FRP stirrups. In addition, parametric analyses were conducted, and design examples were presented to further understand the influence of key design parameters and the applicability of the KDS 14 draft model for FRP-RC beams.

Keywords Fiber-reinforced polymer, One-way shear strength, Design codes, RC beams, Compression zone

1 Introduction

Fiber-reinforced polymer (FRP) reinforcement has gained significant attention in recent years as a viable alternative to traditional steel reinforcement in reinforced concrete (RC) members (Dinh et al., 2024; Park et al., 2021; Pham

et al., 2023). The primary advantage of FRP materials lies in their inherent resistance to corrosion, effectively addressing the durability challenges associated with steel reinforcement, particularly in environments exposed to deicing salts or marine conditions, which are known to accelerate steel corrosion. This corrosion resistance not only improves the durability and longevity of structures but also significantly reduces long-term maintenance and replacement costs, contributing to overall economic and sustainability benefits. In addition, FRP rebars offer other significant benefits, such as being lightweight, high tensile strength, and exhibiting outstanding fatigue

Journal information: ISSN 1976-0485 / eISSN 2234-1315.

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resistance (Dinh et al., 2023; Xue et al., 2016). These properties make FRP reinforcement an attractive choice for construction projects, as it can accelerate construction timelines and reduce labor costs due to its ease of handling, cutting, transportation, and installation.

From a structural perspective, FRP reinforcement exhibits high tensile strengths and are available at different stiffness levels and strengths, increasing their applicability in structural components, such as beams (Huang et al., 2021; Ruan et al., 2020), columns (Morgado et al., 2015), and slabs (Mohamed & Khattab, 2017). Unlike steel reinforcements, FRP rebars show linear elastic response up to failure without yielding, which may increase the potential for unexpected brittle shear failure modes in flexural members. Therefore, careful design and detailing are critical considerations when using FRP reinforcements (Michaluk et al., 1998; Kara, 2011).

Understanding one-way shear behavior is essential for structural design and assessment of slender concrete beams reinforced with FRP rebars. For example, Guadagnini (2002) comprehensively studied the shear mechanisms of FRP-reinforced concrete (FRP-RC) beams and reported that the strain developed in flexural and FRP shear reinforcements can significantly exceed the values prescribed by the current design codes for FRP-RC members. In addition, compared with steel-reinforced beams, FRP-reinforced beams exhibited a more pronounced increase in crack width as the load increased. This behavior reduced friction along the crack length, thereby diminishing aggregate interlock resistance. Similarly, Wegian and Abdalla (2005) conducted four-point bending tests to evaluate the shear resistance of concrete beams reinforced with carbon FRP and glass FRP. They demonstrated that FRP-RC displayed linear behavior up to the first cracking owing to the lower elastic moduli of FRP compared to steel bars, followed by a reduction in stiffness post-cracking. The shear resistance attributable to dowel action in FRP-RC elements was reduced by approximately 70% compared with that of steel-reinforced RC elements. El-Sayed et al., (2006a, 2006b) and Alam et al. (2011) further conducted experiments to assess the effects of the quantity and stiffness of FRP rebars on the shear strength of concrete beams. Their findings indicated that the behavior of concrete beams in the post-cracking stage was primarily influenced by the FRP axial stiffness, showing that the shear strength increased as the reinforcement ratio or elastic modulus of FRP reinforcement increased. Furthermore, a study by Alam et al. (2011) identified the linear relationship between the cubic root of axial stiffness of FRP reinforcement and the normalized shear strength. A more recent

study conducted by Betschoga et al. (2021) explored the effect of different loading types (concentrated and uniformly distributed loads), and boundary conditions (simply supported and cantilever conditions) on the shear behavior of FRP-reinforced beams without stirrups. They reported that these parameters caused notable differences in the location of critical shear cracks and the ultimate shear strength. In addition, they developed a shear strength model for FRP-RC beams based on the critical shear band concept, which was validated against existing data.

Recent studies have been carried out to address the challenges of predicting the one-way shear strength of FRP-RC members. Mukhtar and Deifalla (2023) developed a critical shear crack-based model supported by an extensive test database, offering a reliable approach for predicting shear strength in deep FRP-RC beams. Rahal (2023) proposed a unified shear strength equation applicable to both slabs and beams reinforced with FRP or steel, leveraging simplified cracked elastic properties for practical design. Wakjira et al. (2022) employed explainable machine learning models to enhance shear capacity predictions, demonstrating the potential of data-driven techniques in capturing complex shear capacity of FRP-RC beams. Nguyen and Dang (2025) extended the beam and arch action model using data-driven analysis, improving shear strength estimates for FRP-RC deep beams. Similarly, Xue et al. (2025) refined predictions by focusing on the average ultimate strain in stirrups, emphasizing the role of reasonable strain assessment in enhancing accuracy.

For practical design and performance assessment, existing design provisions adopted empirical or semi-empirical equations to predict the one-way shear strength of slender FRP-RC members, as summarized in Table 1. These equations are typically based on those originally developed for steel-RC members and are calibrated using different experimental datasets. The recent ACI 440.11-22 (ACI, 2022) model is based on modification of the ACI 318-19 (ACI, 2019) model, which was originally developed for steel RC members. This design model calculates the shear contribution of concrete (V_c) in FRP-RC members by considering factors such as the longitudinal FRP reinforcement ratio (ρ_f), square root of concrete compressive strength ($f'_c{}^{0.5}$), and modulus ratio between FRP reinforcement and concrete. In addition, the ACI 440.11-22 model also incorporates adjustments for the member depth size effect (λ_s) and accounts for the minimum shear strength contributed by the concrete. The JSCE (2007) design method stipulated by the Japan Society of Civil Engineering (JSCE)

Table 1 Summary of one-way shear strength models for FRP-RC members

Models	Shear strength equations for concrete contribution	Shear strength equations for stirrup contribution
ACI 440.11-22 (2022)	$V_c = \frac{2}{5} \sqrt{f'_c} \lambda_s b_w k d \geq V_{c,min}$ $k = \sqrt{2 \rho_f (E_{fl}/E_c) + (\rho_f E_{fl}/E_c)^2} - \rho_f E_{fl}/E_c$ $\lambda_s = \sqrt{2/(1 + 0.004d)} \leq 1.0, V_{c,min} = 0.067 \sqrt{f'_c} b d$	$V_{fv} = \frac{A_{fv} f_{fv} d}{s}$ $f_{fv} = 0.005 E_{fv} \leq f_{fb}, f_{fb} = (0.05 r_b/d_b + 0.3) f_{fvu}$
JSCE (2007)	$V_c = \beta_d \beta_p f_{vcd} b_w d$ $\beta_d = \sqrt[4]{1000/d} \leq 1.5 (d \text{ in mm}), \beta_p = (100 \rho_{fl} E_{fl}/E_s)^{1/3} \leq 1.5$ $f_{vud} = 0.2 (f'_c)^{1/3} \leq 0.72$	$V_{fv} = \frac{A_{fv} E_{fv} \varepsilon_{fv} z}{s}$ $\varepsilon_{fv} = 10^{-4} \sqrt{f_{fmc} d \frac{\rho_{fl} E_{fl}}{\rho_{fv} E_{fv}}} \leq f_{fb}/E_{fv}, f_{fb} = (0.05 r_b/d_b + 0.3) f_{fvu}$ $f_{fmc} d = \left(\frac{h}{300} \right)^{-1/10} f_{ct} (h \text{ is in mm})$
CSA/S806-12 (2021)	$V_n = 0.05 \lambda k_m k_s k_a (1 + (E_{fl} \rho_f)^{1/3}) (f'_c)^{1/3} b_w d_v$ $d_v = \max(0.9d, 0.72h)$ $k_m = (d/a)^{0.5} \leq 1, k_a = \begin{cases} 1.0 & \text{for } (a/d) \geq 2.5 \\ 2.5 d/a & \text{for } (a/d) < 2.5 \end{cases}$ $k_s = \frac{750}{450+d} \leq 1 (d \text{ in mm}), 0.11 \sqrt{f'_c} b d \leq V_n \leq 0.22 \sqrt{f'_c} b d$	$V_{fv} = \frac{A_{fv} f_{fv} d_v}{s} \cot \theta$ $f_{fv} = 0.005 E_{fv} \leq f_{fb}, f_{fb} = 0.4 f_{fvu}$ $\theta = 30 + 7000 \varepsilon_v, \varepsilon_1 = \frac{M_f/d_v + V_f}{2 E_{fl} A_{fl}}, 30^\circ \leq \theta \leq 60^\circ$
KDS 14 draft (2024)	$V_c = \lambda k_s f_{te} b_w c_u \sqrt{1 + f_{cc}/f_{te}}$ $k_s = 0.75 \leq \sqrt[4]{300/d} \leq 1.1$ $c_u = (-n \rho_{fl} + \sqrt{(n \rho_{fl})^2 + 2 n \rho_{fl}}) d, n = E_{fl}/E_{cfte} = 0.2 \sqrt{f'_c} t$ $f_{cc} = \frac{M_{ud}}{b_w c (j d)} M_{ud} = 0.75 M_u \geq 1.5 M_{cr}$	$V_{fv} = \frac{A_{fv} f_{fv} d}{s}$ $f_{fv} = 0.005 E_{fv} \leq f_{fb}$
Tarawneh et al. (2024)	$V_c = 0.4 \lambda (n_c \rho_{fl})^{1/3} \sqrt{f'_c} b_w d, n_c = E_{fl}/E_c$	

f'_c = Concrete compressive strength

b_w, d , and a = Web width, effective depth, and shear span of the beam, respectively

ρ_{fl}, E_{fl} = Reinforcement ratio and elastic modulus of FRP longitudinal rebars, respectively

$A_{fv}, f_{fv}, E_{fv}, \rho_{fv}, \varepsilon_{fv}, s$ = Cross-sectional area, design tensile strength, elastic modulus, reinforcement ratio, effective strain, and spacing of FRP shear rebars, respectively

E_s and E_c = Elastic modulus of steel and concrete, respectively

f_{fb} = Tensile strength of the bent portion of FRP shear rebar

guidelines considers several factors, including the modulus ratio $(E_{fl}/E_s)^{1/3}$ between the longitudinal FRP and steel rebars, size effect, and cube root of concrete compressive strength. The CSA/S806-12 (CSA, 2021) design method of the Canadian Standard Association (CSA) is based on the modified compression field theory (Vecchio & Collins, 1986). This approach takes into account the effects of axial stiffness of longitudinal rebars ($E_{fl} \rho_{fl}$), size effect, and effective shear depth (d_v).

The revision draft of the Korean Standard KDS 14 20 22 (2024) (KDS 14 draft) issued by the Korea Concrete Institute adopted the unified shear strength model originally developed by Park et al. (2006) and Choi et al. (2016) to evaluate the one-way shear of steel RC members. This model is based on the theory of compression zone failure mechanisms and demonstrates a strong correlation with a comprehensive database encompassing a wide range of design parameters (Choi et al., 2016). However, because the model was specifically developed for steel-RC beams, additional evaluation is required to determine its applicability to other types of reinforcements, such as FRP rebars.

To address this limitation, the present study evaluates the applicability of the KDS 14 draft model to predict the one-way shear strength of slender FRP-RC members. This evaluation was conducted based on a

comprehensive database of FRP-RC specimens, both with and without shear reinforcement. The prediction performance of the KDS 14 draft model was compared with those in the existing state-of-the-art international design guidelines and of other design models recently developed for FRP-RC members. In addition, a parametric analysis and a design example were conducted to understand the influence of primary design parameters and the applicability of the KDS 14 draft model for FRP-RC beams.

2 Review of One-Way Shear Model Based on Compression Zone Failure Mechanism

In the KDS 14 draft model, the one-way shear of RC members carried by uncracked concrete is evaluated based on the compression zone failure mechanism (Choi et al., 2016). Fig. 1 depicts the shear resistance mechanism and stress state at the shear-critical section in the compression zone of slender RC beams. During the initial loading stage, multiple flexural cracks initiated in the tension zone of the beams. These flexural cracks propagated toward the web of the beam with an increase in the applied load, eventually reaching the compression zone and leading to the formation of critical shear cracks. At the ultimate stage, the compression zone (A-B zone) could no longer function as a continuum and became

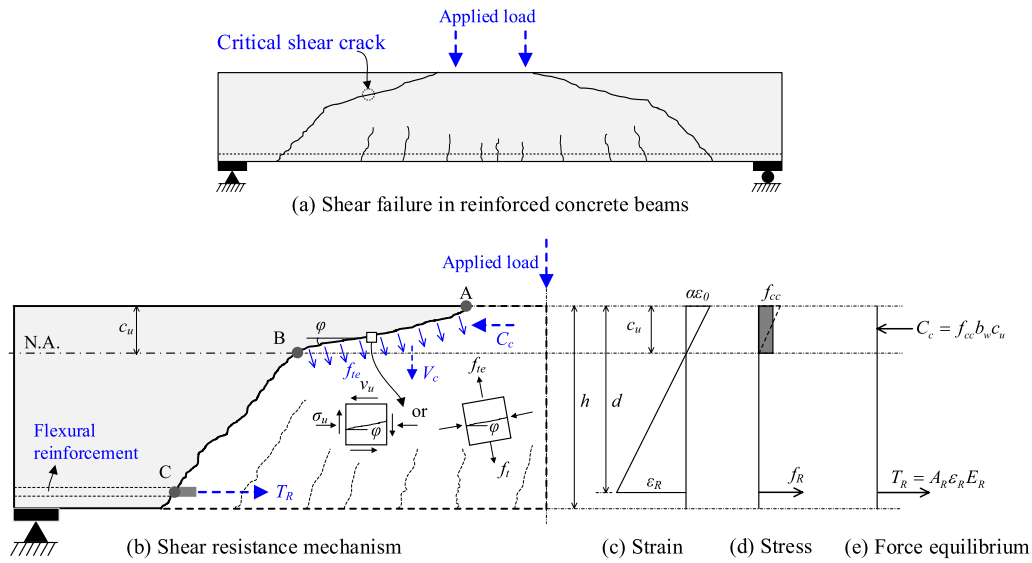


Fig. 1 Shear resistance mechanism of reinforced concrete beams and force equilibrium and strain compatibility at the critical section (Choi et al., 2016)

incapable of resisting the compressive forces triggered by the applied flexural moment, which facilitated the occurrence of brittle shear failure (Choi et al., 2016; Dinh et al., 2020). The shear resistance capacity provided by the compression zone could be estimated as follows (Choi et al., 2016):

$$V_c = f_{te} \frac{c_u}{\sin \varphi} b_w \cos \varphi = f_{te} b_w c_u \cot \varphi \quad (1)$$

where $f_{te} [=0.2\sqrt{f'_c}]$ is the concrete tensile strength specified in the KDS 14 draft model; c_u is the depth of the compression zone; f'_c is the compressive strength of concrete; b_w is the beam's web width, and φ is the average angle of inclined crack in the compression zone, defined by the principal stress axis using the Rankine failure criterion:

$$\cot \varphi = \sqrt{f_{te}(f_{te} + f_{cc})}/f_{te} \quad (2)$$

where f_{cc} = average compressive normal stress in the compression zone.

Substituting Eq. (2) into Eq. (1), the shear contribution of the compression zone is determined as:

$$V_c = f_{te} b_w c_u \sqrt{1 + f_{cc}/f_{te}} \quad (3)$$

By considering the size effect factor (k_s) and reduction factor for lightweight concrete (λ), the final expression for V_c in the KDS 14 draft model is given by:

$$V_c = \lambda k_s f_{te} b_w c_u \sqrt{1 + f_{cc}/f_{te}} \quad (4)$$

where

$$k_s = 0.75 \leq \sqrt[4]{300/d} \leq 1.1 \quad (5)$$

$$\lambda = \begin{cases} 1 & \text{for normal weight concrete} \\ 0.85 & \text{for lightweight concrete} \end{cases} \quad (6)$$

In the actual design, the depth of the compression zone c_u in Eq. (4) could be determined based on the conditions of force equilibrium and strain compatibility. As illustrated in Fig. 1c–e, these conditions can be expressed by assuming a linear distribution of compressive stress and strain in the compression zone:

$$C_c = T_R, \quad (7a)$$

or

$$\frac{1}{2} \alpha \varepsilon_0 E_c b_w c_u = A_R \varepsilon_R E_R = \rho_R b_w d \varepsilon_R E_R \quad (7b)$$

$$\varepsilon_R = \alpha \varepsilon_0 (d - c_u)/c_u \quad (8)$$

where α is the ratio of the current compressive strain to compressive normal strain at extreme compression fiber; T_R is the tensile force in the reinforcement; C_c is the resultant compressive force in the compression zone; A_R and E_R is the total cross-sectional area and elastic

modulus of the tensile reinforcement, respectively; ρ_R is the longitudinal reinforcement ratio; ε_0 [≈ 0.002] is the compressive strain corresponding to the concrete compressive strength; and ε_R is the strain in tensile reinforcement.

From Eqs. (7) and (8), the final equation for c_u is obtained as

$$c_u = d(-n\rho_R + \sqrt{(n\rho_R)^2 + 2n\rho_R}) \quad (9)$$

where $n [=E_R/E_c]$ is the modulus ratio between the tensile reinforcement and concrete.

The one-way shear strength in the compression failure mechanism-based model was significantly influenced by the magnitude of the average compressive stress (f_{cc}) acting on the compression zone, as indicated in Eq. (4). Under a factored flexural moment (M_u) at a given design section, f_{cc} can be directly calculated using the following equation (KDS 14 draft model, 2024):

$$f_{cc} = \frac{M_{ud}}{b_w c (jd)} \leq \frac{2}{3} f'_c \quad (10)$$

where $M_{ud} [=0.75M_u \geq 1.5M_{cr}]$ is the design-factored flexural moment for conservative design purposes, jd [$=d-c_u/3$] is the moment arm, which is simply calculated assuming that compressive stress follows a linear distribution in the compression zone, and M_{cr} is the cracking moment (ACI 318-19, 2019). It should be noted that in the KDS 14 draft design method, a lower limit of the flexural moment, set at $1.5M_{cr}$ in Eq. (10), is recommended. This accounts for the assumption in the compression zone failure theory (Choi et al., 2016) that significant damage in the tension zone is a prerequisite for the formation of inclined tensile cracking in the compression zone.

The design equations of the KDS 14 draft model are summarized in Table 1.

3 Evaluation of Design Provisions

3.1 Database of FRC-RC Specimens

A comprehensive database of concrete specimens reinforced with FRP rebars, obtained from one-way shear tests, was used to evaluate the applicability of the KDS 14 draft model. The dataset, detailed in the Appendix, comprised 304 specimens without FRP shear reinforcement (Table 2) and 110 specimens with stirrups (Table 3). It should be noted that the previous studies in the database reported two types of concrete compressive strength, from cylinder tests (f'_c) and cube tests (f'_{cu}). The data

presented in the database in the Appendix adopt a unified compressive strength as f'_c using the conversion relationship $f'_c = 0.80 f'_{cu}$ (Mosley, 1999).

Figs. 2 and 3 present the specimen number distribution in the database with respect to several design parameters. The database covered different types of FRP reinforcement: carbon FRP (CFRP), aramid FRP (AFRP), GFRP, and basalt FRP (BFRP).

In Fig. 2, the design parameters for FRP-RC specimens without stirrups are as follows: the axial stiffness of FRP reinforcement ($\rho_f E_{ff}$) varied from 150 to 7174 MPa; the compressive strength of concrete (f'_c) ranged from 20 to 102 MPa; and the shear span-to-effective depth ratio (a/d) varied from 2.5 to 8.

In Fig. 3, the design parameters for FRP-RC specimens with stirrups are as follows: the concrete compressive strength (f'_c) ranged from 20 to 102 MPa; the shear span-to-effective depth ratio (a/d) ranged from 1.19 to 4.5; and the axial stiffness of FRP longitudinal reinforcement ($\rho_{fl} E_{ff}$) varied between 246 and 7174 MPa; and the axial stiffness of FRP stirrups ($\rho_{fv} E_{fv}$) varied between 38 to 1470 MPa.

In addition, the database included other parameters, such as cross-sectional shapes (rectangular, I-shaped, and T-shaped), concrete types (normal weight and lightweight), and effective depths ranging from 73 to 937 mm. Most specimens in the two datasets were reinforced with CFRP (113 specimens) and GFRP rebars (273 specimens). Fig. 4 illustrates the influence of key design parameters on the normalized one-way shear strength of FRP-RC beams in the database. It was shown that the axial stiffness of the FRP longitudinal rebar and the effective depth most significantly influenced the shear strength, whereas the concrete compressive strength and the ratio of shear span to effective depth (a/d) exerted a comparatively lower impact for slender beams with $a/d \geq 2.5$.

3.2 Shear Design Provisions

In this study, three existing state-of-the-art international design guidelines are used for a comparative analysis with the KDS 14 draft model: ACI 440.11-22 (2022) issued by the ACI Committee 440, JSCE (2007) issued by the JSCE, and CSA/S806-12 (2021) issued by the CSA. In addition, we used a unified shear design model recently developed by Tarawneh et al. (2024) for slender RC members. This model is based on modifications of the ACI 318-19 model to account for the axial stiffness of longitudinal reinforcement and exhibits promising performance in predicting

the one-way shear of both steel-RC and FRP-RC members with and without shear reinforcement.

3.3 Shear Strength Evaluation Using the KDS 14 Draft

Model and Comparison with Existing Design Methods

Tables 2 and 3 in the Appendix summarize the test results for the one-way shear strength of FRP-RC specimens without and with stirrups, respectively. It should be noted that for the evaluation process, material reduction, and safety factors in the design equations were set to 1.0 to ensure a consistent comparison. Statistical parameters, such as the minimum, maximum, and average values, coefficient of variation (COV), and average absolute error (AAE) of the shear strength ratio between test and prediction results, were used to evaluate the reliability of design models. The AAE was calculated using Eq. (11) as follows:

$$AAE = \frac{1}{n} \sum_{i=1}^n \left| \frac{V_{predict,i} - V_{test,i}}{V_{test,i}} \right| \quad (11)$$

where n is the number of test specimens used in the statistics, and $V_{test,i}$ and $V_{predict,i}$ is the test results and predictions, respectively. AAE is one of the key statistical measures indicating the correlation between the dataset of prediction and test results: the lower the AAE value, the better the model correlates with the dataset. In addition, the safety of different design equations was assessed using the 5% fractal indicator ($P_{0.05}$), assuming a normal distribution of the ratio $V_{test}/V_{predict}$. The $P_{0.05}$ value is generally accepted as a characteristic value of resistance in the limit state theory (EN1990:2002, 2002): the closer the 5% fractal value closer to 1, the better the safety. In addition, the figures report the percentage of specimens with $V_{test}/V_{predict}$ less than 0.75, which corresponds to the strength reduction factor for shear design.

For the application of the KDS 14 draft model to the existing database, the elastic modulus (E_{fl}) and longitudinal reinforcement (ρ_{fl}) for FRP rebars were substituted for E_R and ρ_R values in design Eqs. (7–9). In addition, according to the KDS 14 draft model, the one-way shear strength of concrete (V_c) varied along the member length because of the variation in the average compressive stress (f_{cc}) caused by the factored flexural moment (Eq. 10). Therefore, V_c should be checked along the member length at the potential shear-critical sections during the design process. For most specimens in the database, which were simply supported and subjected to four-point bending, the KDS 14 draft model recommends checking the location of the critical shear section at a distance of 1.2 times

the effective depth from the end support. Therefore, the designed factored flexural moment (M_{ud}) in Eq. (10) can be calculated using $[M_{ud} = (1.2d)V_{test} \geq 1.5M_{cr}]$, where V_{test} is the shear load at failure obtained from test results.

3.3.1 FRP-RC Specimens Without Stirrups

Fig. 5 presents the distribution of the shear strength ratio $V_{test}/V_{predict}$ according to the axial stiffness of FRP longitudinal rebars and the effective depth for FRP-RC specimens without stirrups. Overall, all prediction models provided conservative estimations when compared to the experimental results across different design parameters. For all prediction models, the percentage of specimens with $V_{test}/V_{predict}$ ratios below 0.75 was minimal, ranging from 0% to 1.32%.

Among the models, ACI 440.11-22 (Fig. 5b) exhibited the highest scatteredness, with a COV of 22% and the highest conservatism compared to the experimental data, reflected in a mean value of $V_{test}/V_{predict}$ of 1.71 and a $P_{0.05}$ value of 1.38. Compared to other models, the prediction results of the KDS 14 draft model (Fig. 5a) exhibited the lowest scatteredness, with a COV value of 20% and good correlation with the test results, as evidenced by a mean $V_{test}/V_{predict}$ ratio of 1.29 and AAE of 0.22. In addition, the KDS 14 draft model yielded a $P_{0.05}$ value close to 1.0, indicating an acceptable level of safety and reliability.

Compared to the KDS 14 draft model, the empirical model proposed by Tarawneh et al. (2024) (Fig. 5e) yielded a similar performance, whereas the JSCE model (Fig. 5c) displayed slightly higher variability and mean strength ratios. Although the CSA/S0806 model (Fig. 5d) exhibited a good correlation with test results, with a mean $V_{test}/V_{predict}$ ratio of 1.17 and an AAE of 0.18, it displayed a lower safety level compared to other models, with a $P_{0.05}$ value of 0.74.

3.3.2 FRP-RC Specimens with Stirrups

Fig. 6 shows the distribution of the shear strength ratio $V_{test}/V_{predict}$ according to the FRP shear reinforcement ratio (ρ_v) and the effective depth for FRP-RC specimens with stirrups. The shear reinforcement ratio was calculated as $[A_{fv}/b_w s]$, where A_{fv} is the area of the FRP shear reinforcement ratio within the spacing s . Table 1 summarizes the shear strength equations for stirrup contributions for different design codes. Generally, in all design models, the shear contribution of FRP reinforcement is expressed as

$$V_{f_v} = \frac{A_{f_v} f_{f_v} d_v}{s} \cot \theta \quad (12)$$

where f_{f_v} is the effective tensile strength of FRP reinforcement used for shear design, θ is the inclination angle of the diagonal concrete strut, and d_v is the effective shear depth.

As shown in Table 1, the primary differences between design codes for calculating V_{f_v} concern the effective tensile strength of FRP stirrups and the inclination angle of the diagonal concrete strut. Considering that FRP exhibited linear behavior up to failure, different codes prescribed varying strain limits for FRP stirrups to control the crack width (Tarawneh et al., 2024). The ACI 440.11-22 and CSA/S806 models adopted the design strength of FRP stirrups corresponding to a strain limit of 0.005 or a strength limit based on the tensile strength of the bent portion of FRP stirrups (f_{fb}). In contrast, the JSCE model specifies a more conservative strain limit of FRP stirrups, considering the axial stiffness ratio between longitudinal ($\rho_l E_{fl}$) and shear ($\rho_{fv} E_{fv}$) reinforcement, as well as concrete compressive strength. In addition, the CSA/S806 model adopted an empirical equation based on the MCFT to determine the inclination angle of the diagonal concrete strut, which was different from the value of 45° used in the ACI 440.11-22 and JSCE models. The KDS 14 draft model for steel reinforcement adopted the same design equation as ACI 318-19 (ACI, 2019) for stirrup shear contribution. Therefore, we adopted the same shear strength equation for FRP stirrup contributions using the ACI 440.11-22 method.

The prediction results of the KDS 14 draft model (Fig. 6a) exhibited the lowest scatteredness, with a COV value of 22%, and displayed the best correlation with test results, as represented by a mean $V_{test}/V_{predict}$ ratio of 1.18 and an AAE of 0.2. The percentage of specimens with $V_{test}/V_{predict}$ ratios below 0.75 predicted by the KDS 14 draft model was relatively small, within an acceptable level (2.73%). The ACI 440.11-22 and CSA/S806 (Fig. 6b & c) yielded similar performances with mean $V_{test}/V_{predict}$ ratios of 1.52–1.54, COVs of 25–27%, and AAEs of 0.32–0.33. The model by Tarawneh et al. (Fig. 6e) maintained a balance between safety and reasonable correlation with the experimental dataset. In particular, the JSCE model (Fig. 6d) displayed overly conservative predictions reflected in a mean value of $V_{test}/V_{predict}$ of 2.62 and very high scatteredness (COV of 30%). This is attributed to the fact that the JSCE

model adopted an excessively conservative strain limit for FRP stirrups, thereby underestimating the shear contribution of stirrups.

4 Parametric Study Using Design Models

Fig. 7 shows the parametric study results using the KDS 14 draft and existing design models to understand the influence of primary parameters on the one-way shear strength of concrete beams reinforced with FRP bars. The effect of the effective depth of the beam is shown in Fig. 7a. The effective depth of analytical beams varied from 0.15 to 0.55 m, whereas that of other design parameters was similar to that examined by Ashour and Kara (2014). For all design models, the anticipated shear strength increased proportionally with the effective depth of the beams. In the KDS 14 draft model, an increase in the effective depth increased the compression zone depth (Eq. 9), which, consequently, enhanced the shear strength. An analogous increasing tendency of shear strength was observed (Fig. 7b) as the concrete compressive strength increased from 20 to 90 MPa. This phenomenon is attributed to the increase in compressive strength that increases the tensile strength of the concrete and contributes to the overall shear resistance of the compression zone (Eq. 1).

The influence of axial stiffness of FRP longitudinal rebars ($\rho_l E_{fl}$) is shown in Fig. 7c. The analytical beams used $\rho_l E_{fl}$ varied from 202 to 968 MPa by increasing the FRP reinforcement ratio from 0.5% to 2.4%. Higher axial stiffness led to higher shear strength prediction because the KDS 14 draft model determined the compression zone depth considering the effect of FRP axial stiffness, as shown in the Eqs. (7)–(9) for force equilibrium and strain compatibility. A similar increasing trend in shear strength is observed with an increase in the shear reinforcement ratio, as shown in Fig. 7d, due to the enhanced contribution of stirrups to the overall shear strength.

Overall, the parametric study presented in Fig. 7 indicates that one-way shear strength predictions by the KDS 14 draft model exhibited a similar trend to the state-of-the-art design methods for FRP-RC beams, which were conservative and consistent with the test results in several current studies (Alam, 2010; Ashour & Kara, 2014; Johnson, 2014; Yost et al., 2001).

5 Design Example

To understand the KDS 14 draft methods, a design example was provided for a fixed-end concrete beam reinforced with FRP rebars and subjected to a uniformly distributed

load of $w_u = 100$ kN/m (including the self-weight), as presented in Fig. 8. The beam had a span length of $L = 8$ m and cross-sectional dimensions of $b \times d = 0.4 \times 0.6$ m. The beam used normal-weight concrete with $f'_c = 27$ MPa and GFRP bars as longitudinal and shear reinforcements with $f_{fu}^* = 700$ MPa and $E_f = 47.5$ GPa. The longitudinal reinforcement ratio was $\rho_{fl} = 1.02\%$ ($5\Phi 25$), whereas the shear reinforcement ratio was $\rho_{fv} = 0.39\%$ ($\Phi 10@100$ mm) within two lengths of $L/4$ from the support end and $\rho_{fv} = 0.26\%$ ($\Phi 10@150$ mm) in the remaining span.

Assuming interior exposure conditions for the design process, the designed tensile strength of GFRP bars was calculated as $f_{fu} = C_e f_{fu}^* = (0.8)(700) = 560$ MPa. Shear strengths were calculated and checked at several cross sections: A_1 within the shear span (at a distance d from the support end) and (A_2 – A_3) outside the shear span. Fig. 8b and c shows the factored moment and shear force distributions, respectively.

The representative calculation at cross-section A_1 following the KDS 14 draft design method is as follows:

- Calculation of the compression zone depth:

$$n = E_f / E_c = 47,500 / (4700\sqrt{27}) = 1.945$$

$$\begin{aligned} c_u &= d \left(-n\rho_f + \sqrt{(n\rho_f)^2 + 2n\rho_f} \right) \\ &= 0.6 \left(-0.0199 + \sqrt{(0.0199)^2 + 2 \times 0.0199} \right) = 0.108 \text{ m} \end{aligned}$$

- Calculation of the compression zone crack angle:

$$\begin{aligned} M_{ud} &= 0.75M_u = 163.5 \text{ kNm} \\ &\geq 1.5M_{cr} = 157.8 \text{ kNm} \end{aligned}$$

$$f_{cc} = \frac{M_{ud}}{b_w c_u (jd)} = \frac{157.8}{0.4(0.108)(0.6 - 0.108/3)} = 6.69 \text{ MPa} \leq \frac{2}{3}f'_c = 18 \text{ MPa}$$

$$\begin{aligned} \cot \varphi &= \sqrt{1 + f_{cc}/f_{te}} \\ &= \sqrt{1 + 6.69/(0.2\sqrt{27})} = 2.73 \end{aligned}$$

- Calculation of shear contribution by concrete and FRP shear reinforcement:

$$k_s = \sqrt[4]{300/d} = 0.841 \rightarrow 0.75 \leq k_s \leq 1.1$$

$$\begin{aligned} V_c &= \lambda k_s f_{te} b_w c_u \cot \varphi \\ &= 1(0.841)(1.04)(0.4)(0.108)(2.73) \\ &= 103 \text{ kN} \end{aligned}$$

$$f_{fv} = 0.005E_{fv} = 238 \text{ MPa} < f_{fv} = 560 \text{ MPa}$$

$$\begin{aligned} V_{fv} &= \frac{A_{fv} f_{fv} d}{s} = \rho_{fv} b_w d f_{fv} \\ &= 0.0039(0.4)(0.6)238 = 224 \text{ kN} \end{aligned}$$

- Calculation of shear strength at cross-section A_1 and checking the condition:

ϕV_n (at A_1) = $\phi(V_c + V_{fv}) = 0.75(103 + 224) = 245 \text{ kN} > V_u = 238 \text{ kN}$. Thus, the beam satisfied the safety conditions.

We used the same calculation process to express the shear strengths at cross-section A_2 according to the KDS 14 draft design method and safety conditions as follows:

ϕV_n (at A_2) = $\phi(V_c + V_{fv}) = 0.75(58 + 149) = 208 \text{ kN} > V_u = 140 \text{ kN}$. Thus, the beam satisfied the safety conditions.

6 Conclusion

This study evaluated the applicability of the KDS 14 draft design method to predict the one-way shear strength of slender concrete members reinforced with FRP rebars. The evaluation was conducted using a large dataset of FRP-RC members, including 304 specimens without FRP stirrups and 110 specimens with FRP stirrups. The

performance of the KDS 14 draft model was compared with that of state-of-the-art design codes and an empirical design model recently developed by Tarawneh et al. (2024). In addition, a parametric study analysis was conducted, and a design example was presented to investigate the influence of primary design parameters and the applicability of the KDS 14 draft design method for FRP-RC beams. The main conclusions are as follows:

1. The KDS 14 draft model demonstrated promising performance in predicting the one-way shear strength of a large dataset of slender FRP-RC members without FRP stirrups. It exhibited the lowest scatteredness compared to other current design methods, with a COV value of 20%. In addition, the model correlated well with the dataset, presented by a mean shear strength ratio of 1.29 and AAE of 0.22. The KDS 14 draft design method provided an acceptable level of safety and reliability, with a $P_{0.05}$ value of 0.86. The ACI 440.11-22 design method exhibited the highest scatteredness and conservatism, with a mean shear strength ratio of 1.71 and a $P_{0.05}$ value of 1.38.
2. For FRP-RC members with FRP stirrups, different design codes adopted different strain limits for FRP reinforcement to calculate the shear contribution of FRP stirrups. Compared to other methods, prediction results of the KDS 14 draft model exhibited the lowest scatteredness, with a COV value of 22%, and displayed the best correlation with the test results, as represented by a mean shear strength ratio of 1.18 and an AAE of 0.2. In addition, the percentage of specimens with shear strength ratios below 0.75 was relatively low (2.73%), indicating an acceptable level of safety. Overall, compared with the experimental dataset, all existing design methods yielded conservative predictions. In particular, the JSCE model displayed overly conservative predictions owing to the adoption of an excessively conservative strain limit for FRP stirrups.
3. A parametric study was conducted to examine the primary design parameters affecting the one-way shear strength of FRP-RC members, including the beam's effective depth, concrete compressive strength, axial stiffness of FRP longitudinal reinforcement, and shear reinforcement ratio. Overall, the KDS 14 draft model predictions exhibited a trend similar to that of the state-of-the-art design methods for FRP-RC beams, which were conservative and consistent with the test results in previous studies. In the KDS 14 draft model, increases in effective depth, concrete compressive strength, and FRP axial stiffness increased the compression zone depth determined by force equilibrium and strain compatibility conditions, leading to enhance the overall one-way shear strength.
4. The anticipated shear strength in the KDS 14 draft model, which is based on the compression zone failure theory, displayed a proportional increase in the effective depth of the beams due to increased compression zone depth. A similar tendency was observed with an increase in the concrete compressive strength, which was attributed to the improved tensile strength of concrete, thereby contributing to the overall shear resistance in the compression zone. Furthermore, the axial stiffness of FRP longitudinal rebars significantly affected the one-way shear strength of concrete members. Higher axial stiffness resulted in higher shear strength prediction owing to the improved compression zone depth.

Table 2 Database of FRP-RC beams without FRP shear reinforcement

Authors	Specimen	Cross-section	L (m)	b _w (m)	h (m)	d (m)	a/d	f _c (MPa)	Concrete type	FRP type	f _{tu} (MPa)	E _f (GPa)	ρ _f (%)	V _{c, test} (kN)	V _{c, KDS} (kN)	V _{c, test} /V _{c, KDS}
Yost et al., (2001)	1FRP	R	2.13	0.23	0.29	0.23	4.10	36	NW	GFRP	690	40.3	1.11	39.1	32.7	1.20
	2FRP	R	2.13	0.18	0.29	0.23	4.10	36	NW	GFRP	690	40.3	1.42	32.5	27.1	1.20
	3FRP	R	2.13	0.23	0.29	0.23	4.10	36	NW	GFRP	690	40.3	1.65	45.4	36.3	1.25
	4FRP	R	2.13	0.28	0.29	0.23	4.10	36	NW	GFRP	690	40.3	1.81	46.5	45.4	1.02
	5FRP	R	2.13	0.25	0.29	0.23	4.10	36	NW	GFRP	690	40.3	2.05	46.2	42.7	1.08
	6FRP	R	2.13	0.23	0.29	0.23	4.10	36	NW	GFRP	690	40.3	2.27	43.2	39.5	1.09
El-Sayed et al. (2005)	S-C1	R	2.50	1.00	0.20	0.17	6.06	40	NW	CFRP	1536	114.0	0.39	143.8	106.7	1.35
	S-C2B	R	2.50	1.00	0.20	0.17	6.06	40	NW	CFRP	1536	114.0	0.78	170.8	128.4	1.33
	S-C3B	R	2.50	1.00	0.20	0.16	6.21	40	NW	CFRP	1536	114.0	1.17	193.8	142.4	1.36
	S-G1	R	2.50	1.00	0.20	0.16	6.17	40	NW	GFRP	597	40.0	0.86	116.8	99.4	1.17
	S-G2	R	2.50	1.00	0.20	0.16	6.29	40	NW	GFRP	540	40.0	1.70	145.8	118.9	1.23
	S-G2B	R	2.50	1.00	0.20	0.16	6.17	40	NW	GFRP	597	40.0	1.71	166.8	119.4	1.40
El-Sayed et al., (2006a)	S-G3	R	2.50	1.00	0.20	0.16	6.29	40	NW	GFRP	540	40.0	2.44	166.8	130.9	1.27
	S-G3B	R	2.50	1.00	0.20	0.15	6.49	40	NW	GFRP	597	40.0	2.63	171.8	132.9	1.29
	CN-1	R	2.75	0.25	0.40	0.33	3.07	50	NW	CFRP	1536	128.0	0.87	79.7	65.7	1.21
	GN-1	R	2.75	0.25	0.40	0.33	3.07	50	NW	GFRP	608	39.0	0.87	72.7	47.9	1.52
	CN-2	R	2.75	0.25	0.40	0.33	3.07	45	NW	CFRP	986	134.0	1.24	106.2	70.3	1.51
	GN-2	R	2.75	0.25	0.40	0.33	3.07	45	NW	GFRP	754	42.0	1.22	62.2	51.4	1.21
El-Sayed et al. (2009)	CN-3	R	2.75	0.25	0.40	0.33	3.07	44	NW	CFRP	986	134.0	1.72	126.7	82.1	1.54
	GN-3	R	2.75	0.25	0.40	0.33	3.07	44	NW	GFRP	754	42.0	1.71	79.7	55.8	1.43
	CH-1.7	R	2.75	0.25	0.40	0.33	3.07	63	NW	CFRP	769	135.0	1.71	132.2	88.6	1.49
	GH-1.7	R	2.75	0.25	0.40	0.33	3.07	63	NW	GFRP	754	42.0	1.71	89.2	63.7	1.40
	CH-2.2	R	2.75	0.25	0.40	0.33	3.07	63	NW	CFRP	769	135.0	2.20	176.2	106.6	1.65
	GH-2.2	R	2.75	0.25	0.40	0.33	3.07	63	NW	GFRP	754	42.0	2.20	117.7	68.1	1.73
Ashour (2006)	G1	R	4.50	0.60	0.30	0.26	6.68	68	NW	GFRP	683	48.0	0.77	89.2	105.1	0.85
	G2	R	4.50	0.60	0.30	0.26	6.68	68	NW	GFRP	683	48.0	1.53	116.2	126.3	0.92
	Beam 1	R	2.00	0.15	0.20	0.18	3.70	28	NW	GFRP	650	38.0	0.45	13.0	11.0	1.18
	Beam 3	R	2.00	0.15	0.25	0.22	3.03	28	NW	GFRP	705	32.0	0.71	18.1	14.5	1.25
	Beam 5	R	2.00	0.15	0.30	0.24	2.78	28	NW	GFRP	705	32.0	0.86	25.8	17.8	1.45
	Beam 7	R	2.00	0.15	0.20	0.18	3.70	49	NW	GFRP	705	32.0	1.39	18.0	17.4	1.03
Tureyen and Frosch (2002)	Beam 9	R	2.00	0.15	0.25	0.22	3.03	49	NW	GFRP	705	32.0	1.06	28.1	19.8	1.42
	Beam 11	R	2.00	0.15	0.30	0.24	2.78	49	NW	GFRP	705	32.0	1.15	30.8	23.6	1.31
	V-G1-1	R	2.44	0.46	0.41	0.36	3.40	35	NW	GFRP	606	40.5	0.96	108.1	79.7	1.36
	V-G2-1	R	2.44	0.46	0.41	0.36	3.40	35	NW	GFRP	593	37.9	0.96	94.7	78.2	1.21
	V-A-1	R	2.44	0.46	0.41	0.36	3.40	35	NW	BFRP	1420	47.1	0.96	114.8	83.0	1.38
	V-G1-2	R	2.44	0.46	0.43	0.36	3.40	35	NW	GFRP	606	40.5	1.92	137.0	100.3	1.37

Table 2 (continued)

Authors	Specimen	Cross-section	L (m)	b _w (m)	h (m)	d (m)	a/d	f _c (MPa)	Concrete type	FRP type	f _{tu} (MPa)	E _f (GPa)	ρ _f (%)	V _{c,rest} (kN)	V _{c,KDS} (kN)	V _{c,rest} /V _{c,KDS}
Razaqpur et al. (2004)	V-G2-2	R	2.44	0.46	0.43	0.36	3.40	35	NW	GFRP	593	37.9	1.92	152.6	98.5	1.55
	V-A-2	R	2.44	0.46	0.43	0.36	3.40	35	NW	BFRP	1420	47.1	1.92	177.0	104.4	1.69
	BR1	R	2.00	0.20	0.25	0.23	2.67	41	NW	CFRP	2250	145.0	0.25	37.0	25.2	1.47
	BR2/BA2	R	2.00	0.20	0.25	0.23	2.67	49	NW	CFRP	2250	145.0	0.50	47.9	32.4	1.48
	BR3	R	2.00	0.20	0.25	0.23	2.67	41	NW	CFRP	2250	145.0	0.63	48.1	32.9	1.46
	BR3	R	2.00	0.20	0.25	0.23	2.67	41	NW	CFRP	2250	145.0	0.88	43.6	35.4	1.23
Zhao et al. (1995)	BA3	R	2.00	0.20	0.25	0.23	3.56	41	NW	CFRP	2250	145.0	0.50	47.8	30.9	1.55
	BA4	R	2.00	0.20	0.25	0.23	4.50	41	NW	CFRP	2250	145.0	0.50	39.2	30.3	1.29
	#1	R	1.80	0.15	0.30	0.25	3.00	34	NW	CFRP	1124	105.0	1.51	45.6	31.7	1.44
	#6	R	1.80	0.15	0.30	0.25	3.00	34	NW	CFRP	1124	105.0	3.02	46.6	38.3	1.22
	#15	R	1.80	0.15	0.30	0.25	3.00	34	NW	CFRP	1124	105.0	2.27	41.1	33.8	1.22
	BM7	R	1.50	0.18	0.33	0.28	2.69	24	NW	GFRP	717	40.0	2.30	54.0	32.0	1.69
Alkhrdaji et al. (2001)	BM8	R	1.50	0.18	0.33	0.29	2.61	24	NW	GFRP	717	40.0	0.77	36.6	21.8	1.68
	BM9	R	1.50	0.18	0.33	0.29	2.61	24	NW	GFRP	717	40.0	1.34	40.6	25.3	1.61
	G07N	R	2.50	0.16	0.38	0.35	2.75	37	NW	GFRP	674	42.0	0.72	60.3	26.8	2.25
	G10N	R	2.50	0.16	0.38	0.35	3.32	43	NW	GFRP	674	42.0	1.10	45.1	29.9	1.51
	G15N	R	2.50	0.16	0.38	0.33	3.54	34	NW	GFRP	674	42.0	1.54	47.8	30.2	1.58
	C07N	R	2.50	0.13	0.38	0.31	3.06	37	NW	CFRP	1506	120.0	0.72	48.5	27.7	1.75
Deitz et al. (1999)	C10N	R	2.50	0.13	0.38	0.31	3.71	43	NW	CFRP	1506	120.0	1.10	51.0	32.6	1.57
	C15N	R	2.50	0.13	0.38	0.31	3.71	34	NW	CFRP	1506	120.0	1.54	57.9	36.0	1.61
	GFRP1	R	2.13	0.31	0.19	0.16	4.50	29	NW	GFRP	650	40.0	0.73	27.8	24.6	1.13
	GFRP2	R	2.74	0.31	0.19	0.16	5.80	30	NW	GFRP	650	40.0	0.73	29.6	24.9	1.19
	GFRP3	R	2.74	0.31	0.19	0.16	5.80	27	NW	GFRP	650	40.0	0.73	30.5	23.9	1.27
	GB2	R	2.30	0.15	0.25	0.21	3.65	38	NW	GFRP	800	45.0	1.31	27.2	21.1	1.29
Duranovic et al., (1997)	GB6	R	2.30	0.15	0.25	0.21	3.65	33	NW	GFRP	800	45.0	1.36	22.7	20.2	1.12
	L05-0	R	7.10	0.45	0.10	0.94	3.26	46	NW	GFRP	397	37.0	0.51	142.3	88.7	1.60
	M05-0	R	3.05	0.45	0.50	0.44	3.48	35	NW	GFRP	474	37	0.55	87.80	77.2	1.14
	S05-0	R	1.52	0.45	0.25	0.194	3.93	35	NW	GFRP	397	37	0.66	55.10	48.5	1.14
	L20-0	R	7.10	0.45	0.10	0.857	3.56	36	NW	GFRP	397	37	2.23	240.30	155.1	1.55
	M05-0	R	3.05	0.45	0.50	0.405	3.77	35	NW	GFRP	397	37	2.36	140.30	115.1	1.22
Kim and Jang (2014)	S20-0	R	1.52	0.45	0.25	0.188	4.05	35	NW	GFRP	397	37	2.54	74.60	68.8	1.08
	C-2.5-R1	R	2.20	0.20	0.25	0.22	2.5	30	NW	CFRP	2130	146.2	0.32	35.40	24.1	1.47
	C-2.5-R2	R	2.20	0.15	0.25	0.22	2.5	30	NW	CFRP	2130.00	146.20	0.43	25	19.6	1.28
	C-2.5-R3	R	2.20	0.15	0.25	0.22	2.50	30	NW	CFRP	2023	147.9	0.77	26.1	23.0	1.14
	C-3.5-R1	R	2.20	0.20	0.25	0.22	3.50	30	NW	CFRP	2130	146.2	0.32	29.4	24.1	1.22
	C-3.5-R2	R	2.20	0.15	0.25	0.22	3.50	30	NW	CFRP	2130	146.2	0.43	26.9	19.6	1.37

Table 2 (continued)

Authors	Specimen	Cross-section	L (m)	b _w (m)	h (m)	d (m)	a/d	f _c (MPa)	Concrete type	FRP type	f _{tu} (MPa)	E _f (GPa)	ρ _f (%)	V _{c,rest} (kN)	V _{c,KDS} (kN)	V _{c,rest} /V _{c,KDS}
Guadagnini et al. (2006)	C-3.5-R3	R	2.20	0.15	0.25	0.22	3.50	30	NW	CFRP	2023	147.9	0.77	29.6	23.0	1.29
	C-4.5-R1	R	2.20	0.20	0.25	0.22	4.50	30	NW	CFRP	2130	146.2	0.32	26.6	24.1	1.10
	C-4.5-R2	R	2.20	0.15	0.25	0.22	4.50	30	NW	CFRP	2130	146.2	0.43	24.6	19.6	1.26
	C-4.5-R3	R	2.20	0.15	0.25	0.22	4.50	30	NW	CFRP	2023	147.9	0.77	28.1	23.0	1.22
	G-2.5-R1	R	2.20	0.20	0.25	0.22	2.50	30	NW	GFRP	980	48.2	0.32	25.7	17.9	1.44
	G-2.5-R2	R	2.20	0.15	0.25	0.22	2.50	30	NW	GFRP	980	48.2	0.43	24.4	14.5	1.68
	G-2.5-R3	R	2.20	0.15	0.25	0.22	2.50	30	NW	GFRP	941	49.1	0.77	27.3	17.1	1.60
	G-3.5-R1	R	2.20	0.20	0.25	0.22	3.50	30	NW	GFRP	980	48.2	0.32	27.2	17.9	1.52
	G-3.5-R2	R	2.20	0.15	0.25	0.22	3.50	30	NW	GFRP	980	48.2	0.43	21.1	14.5	1.45
	G-3.5-R3	R	2.20	0.15	0.25	0.22	3.50	30	NW	GFRP	941	49.1	0.77	19.5	17.1	1.14
	G-4.5-R1	R	2.20	0.20	0.25	0.22	4.50	30	NW	GFRP	980	48.2	0.32	20.0	17.9	1.12
	G-4.5-R2	R	2.20	0.15	0.25	0.22	4.50	30	NW	GFRP	980	48.2	0.43	17.2	14.5	1.18
	G-4.5-R3	R	2.20	0.15	0.25	0.22	4.50	30	NW	GFRP	941	49.1	0.77	20.5	17.1	1.20
	C-L-18-R1	R	2.00	0.20	0.25	0.22	3.00	34	LW	CFRP	2130	146.2	0.32	26.2	21.4	1.22
	C-L-18-R2	R	2.00	0.15	0.25	0.22	3.00	34	LW	CFRP	2130	146.2	0.43	19.2	17.4	1.10
	C-L-27-R1	R	2.00	0.20	0.25	0.22	3.00	40	LW	CFRP	2130	146.2	0.32	23.6	22.8	1.04
	C-L-27-R2	R	2.00	0.15	0.25	0.22	3.00	40	LW	CFRP	2130	146.2	0.43	21.4	18.5	1.16
	C-L-27-R3	R	2.00	0.15	0.25	0.22	3.00	40	LW	CFRP	2023	147.9	0.77	26.5	21.7	1.22
	G-L-18-R1	R	2.00	0.20	0.25	0.22	3.00	34	LW	GFRP	980	48.2	0.32	21.1	15.9	1.32
	G-L-18-R2	R	2.00	0.15	0.25	0.22	3.00	34	LW	GFRP	980	48.2	0.43	18.9	12.9	1.46
	G-L-27-R1	R	2.00	0.20	0.25	0.22	3.00	40	LW	GFRP	980	48.2	0.32	20.8	16.9	1.23
	G-L-27-R2	R	2.00	0.15	0.25	0.22	3.00	40	LW	GFRP	980	48.2	0.43	20.3	13.7	1.48
	G-L-27-R3	R	2.00	0.15	0.25	0.22	3.00	40	LW	GFRP	941	49.1	0.77	21.8	16.1	1.35
Matta et al. (2013)	GB43	R	2.30	0.15	0.25	0.22	3.30	40	NW	GFRP	765	45.0	1.10	27.9	20.4	1.37
	S1-0.12-1A	R	7.32	0.46	0.98	0.88	3.10	30	NW	GFRP	476	41.0	0.60	179.6	128.4	1.40
	S1-0.12-2B	R	7.32	0.46	0.98	0.88	3.10	30	NW	GFRP	483	41.0	0.60	176.9	128.4	1.38
	S3-0.12-1A	R	2.13	0.11	0.33	0.29	3.10	32	NW	GFRP	849	43.2	0.60	19.8	14.8	1.34
	S3-0.12-2A	R	2.13	0.11	0.33	0.29	3.10	32	NW	GFRP	849	43.2	0.60	18.5	14.8	1.25
	S6-0.12-1A	R	1.22	0.23	0.18	0.15	3.10	60	NW	GFRP	849	43.2	0.60	29.0	21.9	1.33
	S6-0.12-2A	R	1.22	0.23	0.18	0.15	3.10	32	NW	GFRP	849	43.2	0.60	37.3	17.6	2.12
	S6-0.12-3A	R	1.22	0.23	0.18	0.15	3.10	32	NW	GFRP	849	43.2	0.60	26.7	17.3	1.54
	S1-0.24-1A	R	7.32	0.46	0.98	0.88	3.10	30	NW	GFRP	476	41.0	1.20	246.2	154.9	1.59
	S1-0.24-2B	R	7.32	0.46	0.98	0.88	3.10	31	NW	GFRP	483	41.0	1.20	238.2	156.8	1.52
	S3-0.24-1B	R	2.13	0.11	0.33	0.29	3.10	41	NW	GFRP	751	48.2	1.21	22.6	20.1	1.12
	S3-0.24-2B	R	2.13	0.11	0.33	0.29	3.10	41	NW	GFRP	751	48.2	1.21	21.2	20.1	1.05
	S6-0.24-1B	R	1.22	0.23	0.18	0.15	3.10	41	NW	GFRP	751	48.2	1.20	33.4	23.5	1.42

Table 2 (continued)

Authors	Specimen	Cross-section	L (m)	b _w (m)	h (m)	d (m)	a/d	f _c (MPa)	Concrete type	FRP type	f _{tu} (MPa)	E _f (GPa)	ρ _f (%)	V _{c,rest} (kN)	V _{c,KDS} (kN)	V _{c,rest} /V _{c,KDS}
Olivito and Zuccarello (2010)	S6-0.24-2B	R	1.22	0.23	0.18	0.15	3.10	41	NW	GFRP	751	48.2	1.20	32.9	23.5	1.40
	Series (5)	R	2.00	0.15	0.20	0.18	5.60	20	NW	CFRP	1725	115.0	0.87	19.1	15.7	1.22
	Series II(5)	R	2.00	0.15	0.20	0.18	5.60	20	NW	CFRP	1725	115.0	1.46	24.4	19.8	1.23
	Series III(5)	R	2.00	0.15	0.20	0.18	5.60	27	NW	CFRP	1725	115.0	0.87	26.2	18.6	1.41
	Series IV(5)	R	2.00	0.15	0.20	0.18	5.60	27	NW	CFRP	1725	115.0	1.46	27.5	21.8	1.26
Alam (2010)	G-2.5	R	2.40	0.25	0.35	0.31	2.50	39	NW	GFRP	751	48.0	0.84	62.8	41.1	1.53
	G-3.5	R	3.10	0.25	0.35	0.31	3.50	39	NW	GFRP	751	48.0	0.84	45.9	41.1	1.12
	C-2.5	R	2.40	0.25	0.35	0.31	2.50	33	NW	CFRP	1899	144.0	0.42	79.0	44.4	1.78
	C-3.5	R	3.10	0.25	0.35	0.31	3.50	33	NW	CFRP	1899	144.0	0.42	61.1	43.0	1.42
	G-500	R	3.10	0.25	0.50	0.44	2.50	43	NW	GFRP	751	48.0	0.89	132.5	58.8	2.25
	G-650	R	3.60	0.30	0.65	0.58	2.50	36	NW	GFRP	751	48.0	0.91	118.1	77.5	1.52
	G-500-70	R	3.10	0.25	0.50	0.44	2.50	72	NW	GFRP	751	48.2	1.46	119.2	77.8	1.53
	G-650-70	R	3.60	0.30	0.65	0.58	2.50	72	NW	GFRP	751	48.2	1.51	160.5	114.7	1.40
	C-500	R	3.10	0.25	0.50	0.46	2.50	41	NW	CFRP	1899	144.0	0.44	67.6	61.4	1.10
	C-650	R	3.60	0.30	0.65	0.59	2.50	36	NW	CFRP	1899	144.0	0.43	143.7	85.0	1.69
	C-500-70	R	3.10	0.25	0.50	0.45	2.50	72	NW	CFRP	1899	144.0	0.82	103.5	89.4	1.16
	C-650-70	R	3.60	0.30	0.65	0.59	2.50	72	NW	CFRP	1899	144.0	0.73	151.3	126.4	1.20
	G-2.5-350(1)	R	2.40	0.25	0.35	0.30	2.50	36	NW	GFRP	786	46.3	1.41	67.3	45.5	1.48
	G-2.5-350(2)	R	2.40	0.25	0.35	0.30	2.50	36	NW	GFRP	786	46.3	1.41	72.7	45.5	1.60
	G-0.5-500	R	3.10	0.25	0.50	0.46	2.50	41	NW	GFRP	786	46.3	0.35	71.1	42.5	1.67
	G-2.5-500	R	3.10	0.25	0.50	0.43	2.50	41	NW	GFRP	786	46.3	1.46	95.3	62.8	1.52
Nakamura and Higai (1995)	C-0.5-350	R	2.40	0.25	0.35	0.31	2.50	41	NW	CFRP	1899	144.0	0.18	60.5	37.1	1.63
	C-2.5-350	R	2.40	0.25	0.35	0.31	2.50	41	NW	CFRP	1899	144.0	0.66	74.3	52.6	1.41
	C-0.5-500	R	3.10	0.25	0.50	0.46	2.50	41	NW	CFRP	1899	144.0	0.22	73.3	50.8	1.44
	C-2.5-500	R	3.10	0.25	0.50	0.44	2.50	41	NW	CFRP	1899	144.0	0.65	85.6	68.5	1.25
	G50	R	2.40	0.25	0.35	0.29	2.50	63	NW	GFRP	786	46.3	0.87	77.4	49.2	1.57
Swamy and Aburawi (1997)	G-70	R	2.40	0.25	0.35	0.29	2.50	85	NW	GFRP	786	46.3	0.87	82.0	55.0	1.49
	C50	R	2.40	0.25	0.35	0.31	2.50	63	NW	CFRP	1899	144.0	0.42	73.4	54.5	1.35
	G01	R	1.20	0.30	0.20	0.15	4.00	23	NW	GFRP	751	29.0	1.34	33.5	24.9	1.34
	G02	R	1.20	0.30	0.20	0.15	4.00	28	NW	GFRP	751	29.0	1.79	36.5	28.9	1.26
	F3-CF	R	2.10	0.15	0.25	0.22	3.15	39	NW	GFRP	586	34.0	1.55	39.7	22.3	1.78
Liu (2011)	#1 B1NW	R	2.44	0.64	0.24	0.20	6.04	72	NW	GFRP	715	43.3	0.94	138.4	96.9	1.43
	#2 B2NW	R	2.44	0.64	0.24	0.20	6.04	87	NW	GFRP	715	43.3	0.94	136.6	103.8	1.32
	#3 B2NW	R	2.44	0.64	0.24	0.20	6.04	60	NW	GFRP	715	43.3	0.94	125.0	90.6	1.38
	#4 B1LW	R	2.44	0.64	0.24	0.20	6.04	63	LW	GFRP	715	43.3	0.94	113.9	78.4	1.45

Table 2 (continued)

Authors	Specimen	Cross-section	L (m)	b _w (m)	h (m)	d (m)	a/d	f _c (MPa)	Concrete type	FRP type	f _{tu} (MPa)	E _f (GPa)	ρ _f (%)	V _{c,rest} (kN)	V _{c,KDS} (kN)	V _{c,rest} /V _{c,KDS}
Razaqpur et al. (2011)	#5 B1LW	R	2.44	0.64	0.24	0.20	6.04	75	LW	GFRP	715	43.3	0.94	104.1	83.6	1.25
	#6 B2LW	R	2.44	0.64	0.24	0.20	6.04	60	LW	GFRP	715	43.3	0.94	104.6	77.0	1.36
	#7 B1LW	R	2.03	0.64	0.26	0.23	4.47	68	LW	GFRP	715	43.3	0.94	124.0	87.1	1.42
	#8 B1NW	R	2.90	0.64	0.27	0.24	6.04	79	NW	GFRP	715	43.3	0.79	109.0	107.1	1.02
	#9 B2NW	R	2.90	0.64	0.27	0.24	6.04	61	NW	GFRP	715	43.3	0.79	126.4	97.4	1.30
	#10 B1LW	R	2.90	0.64	0.27	0.24	6.04	63	LW	GFRP	715	43.3	0.79	101.0	83.8	1.21
	#11 B2LW	R	2.90	0.64	0.27	0.24	6.04	67	LW	GFRP	715	43.3	0.79	106.8	85.7	1.25
	#12 B1NW	R	2.44	1.85	0.24	0.20	6.04	84	NW	GFRP	715	43.3	0.96	396.3	301.0	1.32
	#13 B2NW	R	2.44	1.85	0.24	0.20	6.04	59	NW	GFRP	715	43.3	0.96	330.0	264.4	1.25
	#14 B1LW	R	2.44	1.85	0.24	0.20	6.04	63	LW	GFRP	715	43.3	0.96	279.3	230.2	1.21
Zeidan et al. (2011)	#15 B1LW	R	2.44	1.85	0.24	0.20	6.04	63	LW	GFRP	715	43.3	0.96	294.9	230.2	1.28
	#16 B2LW	R	2.44	1.85	0.24	0.20	6.04	57	LW	GFRP	715	43.3	0.96	303.8	222.0	1.37
	#17 B2LW	R	2.44	1.85	0.24	0.20	6.04	56	LW	GFRP	715	43.3	0.96	307.3	220.5	1.39
	#18 B1NWE	R	2.44	1.85	0.24	0.20	6.04	84	NW	GFRP	715	43.3	0.54	282.9	258.4	1.09
	#19 B1LWE	R	2.44	1.85	0.24	0.20	6.04	63	LW	GFRP	715	43.3	0.54	254.0	197.6	1.29
	#20 B2LWE	R	2.44	1.85	0.24	0.20	6.04	56	LW	GFRP	715	43.3	0.54	225.9	189.2	1.19
	B1	R	3.00	0.30	0.23	0.20	3.50	52	NW	CFRP	1500	114.0	0.35	64.6	39.6	1.63
	B2	R	3.00	0.30	0.33	0.30	3.50	52	NW	CFRP	1500	114.0	0.32	62.3	50.7	1.23
	B3	R	3.00	0.30	0.43	0.40	3.50	52	NW	CFRP	1500	114.0	0.30	57.3	60.6	0.95
	B4	R	3.00	0.30	0.53	0.50	3.50	52	NW	CFRP	1500	114.0	0.28	71.5	69.4	1.03
Khaja and Sherwood (2013)	B5	R	3.00	0.30	0.43	0.40	6.50	52	NW	CFRP	1500	114.0	0.30	55.2	60.6	0.91
	B6	R	3.00	0.30	0.43	0.40	6.00	52	NW	CFRP	1500	114.0	0.30	65.9	60.6	1.09
	A-II-2.5	R	2.00	0.15	0.30	0.28	2.50	45	NW	CFRP	2840	148.0	0.11	23.2	18.0	1.29
	A-II-5.0	R	3.40	0.15	0.30	0.28	5.00	49	NW	CFRP	2840	148.0	0.11	13.6	18.5	0.73
	B-II-2.5	R	2.00	0.15	0.30	0.28	2.50	46	NW	CFRP	2840	148.0	0.21	28.2	21.5	1.31
	A-I-2.5	R	2.00	0.15	0.30	0.28	2.50	24	NW	CFRP	2840	148.0	0.11	23.2	14.3	1.63
	MB-1	R	1.50	0.40	0.28	0.25	3.00	51	NW	GFRP	728	47.5	0.57	57.1	54.9	1.04
	MB-2	R	1.50	0.40	0.28	0.25	3.00	49	NW	GFRP	728	47.5	0.86	75.1	60.4	1.24
	MB-3	R	1.50	0.40	0.28	0.25	3.00	51	NW	GFRP	728	47.5	1.14	86.1	66.2	1.30
	MB-4	R	1.50	0.40	0.28	0.25	3.00	51	NW	GFRP	728	47.5	1.71	109.1	73.8	1.48
	MB-5	R	1.50	0.40	0.28	0.25	3.00	52	NW	GFRP	728	47.5	2.28	116.1	80.4	1.44
	MB-6	R	1.50	0.40	0.28	0.25	3.00	50	NW	GFRP	728	47.5	0.86	79.1	60.9	1.30
	MB-7	R	2.00	0.40	0.28	0.25	4.00	51	NW	GFRP	728	47.5	1.14	90.4	66.2	1.37
	MB-8	R	3.00	0.40	0.28	0.25	6.00	50	NW	GFRP	728	47.5	1.71	91.1	73.3	1.24
	MB-9	R	4.00	0.40	0.28	0.25	8.00	48	NW	GFRP	728	47.5	2.28	84.8	78.1	1.09
	MB-10	R	1.50	0.40	0.28	0.25	3.00	51	NW	GFRP	675	51.9	4.05	136.1	101.9	1.34

Table 2 (continued)

Authors	Specimen	Cross-section	L (m)	b _w (m)	h (m)	d (m)	a/d	f _c (MPa)	Concrete type	FRP type	f _{tu} (MPa)	E _f (GPa)	ρ _f (%)	V _{c,rest} (kN)	V _{c,KDS} (kN)	V _{c,rest} /V _{c,KDS}
Farahmand (1996)	MB-11	R	4.00	0.40	0.28	0.25	8.00	48	NW	GFRP	675	51.9	4.05	99.8	93.4	1.07
	Beam #1	R	2.00	0.20	0.30	0.25	4.00	31	NW	GFRP	692	41.3	0.68	24.5	24.6	1.00
	Beam #2	R	2.00	0.20	0.30	0.25	4.00	31	NW	GFRP	692	41.3	0.79	26.6	25.6	1.04
	Beam #3	R	2.00	0.20	0.30	0.25	4.00	31	NW	GFRP	692	41.3	1.08	33.4	27.8	1.20
	Beam #4	R	1.50	0.20	0.30	0.25	3.00	35	NW	GFRP	692	41.3	0.51	30.5	23.8	1.28
	Beam #5	R	1.50	0.20	0.30	0.25	3.00	35	NW	GFRP	692	41.3	0.76	39.9	26.5	1.51
Ashour and Kara (2014)	Beam #6	R	1.50	0.20	0.30	0.25	3.00	35	NW	GFRP	692	41.3	1.01	37.8	28.5	1.32
	B-400-2	R	2.80	0.20	0.40	0.37	2.70	22	NW	CFRP	1100	141.0	0.12	34.7	23.1	1.50
	B-400-4	R	2.80	0.20	0.40	0.37	2.70	22	NW	CFRP	1100	141.0	0.24	37.9	27.9	1.36
	B-300-2	R	2.80	0.20	0.30	0.27	3.60	29	NW	CFRP	1100	141.0	0.16	34.2	22.4	1.53
	B-300-4	R	2.80	0.20	0.30	0.27	3.60	29	NW	CFRP	1100	141.0	0.33	34.2	27.2	1.26
	B-200-2	R	2.80	0.20	0.20	0.17	5.90	24	NW	CFRP	1100	141.0	0.26	18.5	16.9	1.10
Abdul-Salam (2014)	B-200-4	R	2.80	0.20	0.20	0.17	5.90	24	NW	CFRP	1100	141.0	0.52	21.7	20.3	1.07
	GA-56	R	3.49	1.00	0.20	0.14	6.07	48	NW	GFRP	724	41.0	1.01	100.6	110.2	0.91
	GV-46	R	3.49	1.00	0.20	0.14	6.07	48	NW	GFRP	588	47.6	0.79	125.1	107.5	1.16
	GV-56	R	3.49	1.00	0.20	0.14	6.07	48	NW	GFRP	588	47.6	1.01	112.1	114.5	0.98
	GV-66	R	3.49	1.00	0.20	0.14	6.07	48	NW	GFRP	588	47.6	1.22	125.1	120.3	1.04
	GV-76	R	3.49	1.00	0.20	0.14	6.07	50	NW	GFRP	588	47.6	1.42	170.0	127.1	1.34
Gross et al. (2003)	GV-58	R	3.49	1.00	0.20	0.14	6.18	48	NW	GFRP	666	51.9	1.85	151.8	136.8	1.11
	GH-56	R	3.49	1.00	0.20	0.14	6.07	43	NW	GFRP	1197	69.5	1.01	174.6	121.4	1.44
	GH-66	R	3.49	1.00	0.20	0.14	6.07	49	NW	GFRP	1197	69.5	1.21	128.1	133.5	0.96
	GH-66B	R	3.49	1.00	0.20	0.14	6.07	49	NW	GFRP	1197	69.5	2.43	126.6	159.9	0.79
	GH-78	R	3.49	1.00	0.20	0.14	6.18	50	NW	GFRP	1197	69.5	2.55	127.6	162.7	0.78
	GH-56a	R	3.49	1.00	0.20	0.14	6.07	77	NW	GFRP	1197	69.5	1.01	161.3	150.5	1.07
	GH-56b	R	3.49	1.00	0.20	0.14	6.07	83	NW	GFRP	1197	69.5	1.03	143.7	155.6	0.92
	CV-54	R	3.49	1.00	0.20	0.14	5.92	50	NW	CFRP	1690	144.0	0.45	173.9	126.0	1.38
	CV-64	R	3.49	1.00	0.20	0.14	5.92	50	NW	CFRP	1690	144.0	0.54	147.6	132.1	1.12
	CV-74	R	3.49	1.00	0.20	0.14	5.92	52	NW	CFRP	1690	144.0	0.63	165.6	139.5	1.19
	CV-84	R	3.49	1.00	0.20	0.14	5.92	45	NW	CFRP	1690	144.0	0.72	163.6	137.0	1.19
	CV-65	R	3.49	1.00	0.20	0.14	5.96	46	NW	CFRP	1690	140.0	0.84	179.6	142.7	1.26
	CV-75	R	3.49	1.00	0.20	0.14	5.96	49	NW	CFRP	1690	140.0	0.98	192.6	152.0	1.27
	CV-85	R	3.49	1.00	0.20	0.14	5.96	41	NW	CFRP	1690	140.0	1.11	198.6	147.0	1.35
	CV-74a	R	3.49	1.00	0.20	0.14	5.92	76	NW	CFRP	1690	144.0	0.63	174.6	160.6	1.09
	CV-74b	R	3.49	1.00	0.20	0.14	5.92	86	NW	CFRP	1690	144.0	0.63	219.4	168.1	1.31
Gross et al. (2003)	FRP-1-26-HS	R	2.13	0.20	0.29	0.23	4.06	80	NW	GFRP	690	40.3	1.25	38.9	40.1	0.97
	FRP-2-26-HS	R	2.13	0.15	0.29	0.23	4.06	80	NW	GFRP	690	40.3	1.66	33.2	32.4	1.03

Table 2 (continued)

Authors	Specimen	Cross-section	L (m)	b _w (m)	h (m)	d (m)	a/d	f' _c (MPa)	Concrete type	FRP type	f _{tu} (MPa)	E _f (GPa)	ρ _f (%)	V _{c,rest} (kN)	V _{c,KDS} (kN)	V _{c,rest} /V _{c,KDS}
Gross et al. (2004)	FRP-3-27-HS	R	2.13	0.17	0.29	0.23	4.06	80	NW	GFRP	690	40.3	2.10	36.5	37.4	0.98
	FRP-4-37-HS	R	2.13	0.20	0.29	0.22	4.06	80	NW	GFRP	690	40.3	2.56	47.3	48.5	0.97
	8-2	R	1.97	0.13	0.17	0.14	6.36	60	NW	CFRP	2640	139.0	0.33	14.3	13.6	1.05
	8-3	R	1.97	0.16	0.17	0.14	6.45	62	NW	CFRP	2640	139.0	0.58	20.3	20.1	1.01
	11-2	R	1.97	0.09	0.17	0.14	6.36	81	NW	CFRP	2640	139.0	0.47	10.0	11.7	0.85
Maruyama and Zhao (1994)	11-3	R	1.97	0.12	0.17	0.14	6.45	81	NW	CFRP	2640	139.0	0.76	15.7	18.1	0.87
	FN1	R	3.00	0.15	0.30	0.25	3.00	28	NW	CFRP	1308	94.0	0.55	38.3	21.2	1.80
	FN2	R	3.00	0.15	0.30	0.25	3.00	33	NW	CFRP	1308	94.0	1.10	43.8	27.7	1.58
	FN3	R	3.00	0.15	0.30	0.25	3.00	31	NW	CFRP	1308	94.0	1.39	48.3	30.4	1.59
	FN4	R	3.00	0.15	0.30	0.25	3.00	35	NW	CFRP	1308	94.0	2.20	59.1	38.0	1.55
Maruyama (1996)	#24	R	1.25	0.15	0.30	0.25	2.50	34	NW	CFRP	1200	100.0	1.04	38.8	27.0	1.43
	#30	R	2.50	0.30	0.55	0.50	2.50	30	NW	CFRP	1200	100.0	1.04	145.4	85.1	1.71
	I	R	2.00	0.15	0.20	0.17	4.12	24	NW	GFRP	1000	45.8	0.92	12.7	13.1	0.97
Caporale and Luciano (2009)	II	R	2.00	0.15	0.20	0.17	4.12	24	NW	GFRP	1000	45.8	1.54	13.6	15.1	0.90
	III	R	2.00	0.15	0.20	0.17	4.12	31	NW	GFRP	1000	45.8	0.92	14.1	14.4	0.98
	IV	R	2.00	0.15	0.20	0.17	4.12	31	NW	GFRP	1000	45.8	1.54	15.3	16.6	0.92
	Q-C-2L	R	3.96	0.30	0.55	0.44	3.02	42	NW	GFRP	1000	62.6	3.65	145.4	112.9	1.29
Niewels (2008)	Q-A-3L	R	3.90	0.30	0.50	0.41	3.16	43	NW	GFRP	480	44.0	3.25	153.9	94.2	1.63
	Q-A-5L	R	4.50	0.30	0.50	0.40	3.71	28	NW	GFRP	1000	62.6	3.98	107.6	93.1	1.16
	1a	R	1.10	0.42	0.10	0.08	3.61	61	NW	GFRP	780	42.0	0.61	19.9	22.6	0.88
Kilpatrick and Easden (2005)	1b	R	1.50	0.42	0.10	0.08	6.10	61	NW	GFRP	725	42.0	1.10	25.5	26.4	0.97
	1c	R	1.50	0.42	0.10	0.08	6.25	61	NW	GFRP	655	40.0	1.77	32.0	29.5	1.09
	1d	R	1.50	0.42	0.10	0.08	6.41	61	NW	GFRP	630	40.0	2.61	40.5	32.6	1.24
	2a	R	1.10	0.42	0.10	0.08	3.61	74	NW	GFRP	780	42.0	0.61	24.9	24.3	1.03
	2b	R	1.50	0.42	0.10	0.08	6.10	74	NW	GFRP	725	42.0	1.10	22.0	28.3	0.78
	2c	R	1.50	0.42	0.10	0.08	6.25	74	NW	GFRP	655	40.0	1.77	32.0	31.7	1.01
	2d	R	1.50	0.42	0.10	0.08	6.41	74	NW	GFRP	630	40.0	2.61	36.5	35.0	1.04
	3a	R	1.10	0.42	0.10	0.08	3.61	93	NW	GFRP	780	42.0	0.61	35.9	26.4	1.36
	3b	R	1.50	0.42	0.10	0.08	6.10	93	NW	GFRP	725	42.0	1.10	23.0	30.8	0.75
	3c	R	1.50	0.42	0.10	0.08	6.25	93	NW	GFRP	655	40.0	1.77	32.0	34.4	0.93
	3d	R	1.50	0.42	0.10	0.08	6.41	93	NW	GFRP	630	40.0	2.61	38.5	38.0	1.01
	B1	R	0.90	0.42	0.10	0.08	6.00	48	NW	GFRP	840	42.0	0.68	24.8	21.1	1.17
	B2	R	1.40	0.42	0.10	0.07	6.16	48	NW	GFRP	840	42.0	0.93	27.6	22.9	1.21
Kilpatrick and Dawborn (2006)	B3	R	0.90	0.42	0.10	0.07	6.16	48	NW	GFRP	840	42.0	1.16	29.6	24.2	1.22

Table 2 (continued)

Authors	Specimen	Cross-section	L (m)	b _w (m)	h (m)	d (m)	a/d	f _c (MPa)	Concrete type	FRP type	f _{tu} (MPa)	E _f (GPa)	ρ _f (%)	V _{c,rest} (kN)	V _{c,KDS} (kN)	V _{c,rest} /V _{c,KDS}
Tomlinson and Fam (2015)	B4	R	0.90	0.42	0.10	0.08	6.00	76	NW	GFRP	840	42.0	0.68	27.5	25.0	1.10
	B5	R	1.40	0.42	0.10	0.07	6.16	76	NW	GFRP	840	42.0	0.93	26.5	27.1	0.98
	B6	R	0.90	0.42	0.10	0.07	6.16	76	NW	GFRP	840	42.0	1.16	31.4	28.7	1.09
	B7	R	0.90	0.42	0.10	0.08	6.00	92	NW	GFRP	840	42.0	0.68	23.7	26.9	0.88
	B8	R	1.40	0.42	0.10	0.07	6.16	92	NW	GFRP	840	42.0	0.93	25.7	29.1	0.88
	B9	R	0.90	0.42	0.10	0.07	6.16	92	NW	GFRP	840	42.0	1.16	34.5	30.8	1.12
	NT	R	2.90	0.15	0.30	0.27	4.07	60	NW	BFRP	1100	70.0	0.39	19.8	23.0	0.86
	NB	R	2.90	0.15	0.30	0.27	4.07	60	NW	BFRP	1100	70.0	0.51	23.0	24.8	0.93
	NC	R	2.90	0.15	0.30	0.25	4.49	57	NW	BFRP	1100	70.0	0.85	28.6	28.2	1.01
Kralj (2014)	BM25-INF	R	1.35	0.20	0.33	0.27	2.50	47	NW	GFRP	1000	64.0	1.82	82.1	47.8	1.72
	BM16-INF	R	1.35	0.20	0.35	0.27	2.50	47	NW	GFRP	1000	64.0	2.23	75.7	49.3	1.53
	BM12-INF	R	1.35	0.20	0.35	0.27	2.50	47	NW	GFRP	1000	64.0	2.51	63.1	51.5	1.23
Johnson (2014)	JSC32-NT	R	3.36	0.40	0.65	0.58	2.92	32	NW	GFRP	1265	61.2	1.00	159.5	108.6	1.47
	JSV40-NT	R	3.36	0.40	0.65	0.58	2.92	40	NW	GFRP	1264	71.2	1.00	169.0	122.7	1.38
	JSC100-NT	R	3.36	0.40	0.65	0.58	2.92	102	NW	GFRP	1265	61.2	1.00	166.0	165.8	1.00
Noël and Soudki (2014)	G1	R	4.50	0.60	0.30	0.26	6.68	58	NW	GFRP	934	55.4	0.76	89.2	102.6	0.87
	G2	R	4.50	0.60	0.30	0.26	6.68	58	NW	GFRP	934	55.4	1.51	116.2	123.5	0.94
Chang and Seo (2012)	FS200-12	R	3.60	1.20	0.20	0.18	5.80	33	NW	GFRP	705	44	0.66	140.7	107.5	1.31
	FS200-16	R	3.60	1.20	0.20	0.18	5.80	33	NW	GFRP	705	44	0.88	151.7	116.2	1.31
	FS200-20	R	3.60	1.20	0.20	0.18	5.80	33	NW	GFRP	705	44	1.10	158.7	123.5	1.29
	NFS200-6	R	3.60	1.20	0.20	0.18	5.80	33	NW	GFRP	1050	50	0.33	102.8	92.4	1.11
	NFS200-8	R	3.60	1.20	0.20	0.18	5.80	33	NW	GFRP	1050	50	0.44	133.1	99.8	1.33
	NFS200-12	R	3.60	1.20	0.20	0.18	5.80	33	NW	GFRP	1050	50	0.57	166.6	107.0	1.56
	B-3.3-R1	R	1.60	0.15	0.25	0.22	3.30	49	NW	BFRP	1168	50	0.30	17.4	16.4	1.06
El Refai and Abed (2016)	B-3.3-R2	R	1.60	0.15	0.25	0.22	3.30	49	NW	BFRP	1168	50	0.47	23.5	18.5	1.27
	B-3.3-R3	R	1.60	0.15	0.25	0.22	3.30	49	NW	BFRP	1168	50	0.68	19.0	20.4	0.93
	B-3.3-R4	R	1.60	0.15	0.25	0.22	3.30	49	NW	BFRP	1168	50	0.94	28.4	22.2	1.28
	B-3.3-R5	R	1.60	0.15	0.25	0.22	3.30	49	NW	BFRP	1168	50	1.35	30.4	24.5	1.24
	B-2.5-R1	R	1.60	0.15	0.25	0.22	2.50	49	NW	BFRP	1168	50	0.30	20.0	16.4	1.22
	B-2.5-R2	R	1.60	0.15	0.25	0.22	2.50	49	NW	BFRP	1168	50	0.47	32.1	18.5	1.74
	B-2.5-R3	R	1.60	0.15	0.25	0.22	2.50	49	NW	BFRP	1168	50	0.68	27.5	20.4	1.35
	5-10N5	R	3.05	0.20	0.30	0.17	5.56	36	NW	BFRP	1070	53	1.21	30.9	32.7	0.94
	5-13N5	R	3.05	0.20	0.30	0.17	5.56	36	NW	BFRP	1050	51	2.00	40.3	36.8	1.10
	5-16N5	R	3.05	0.20	0.30	0.17	5.56	36	NW	BFRP	1060	51	3.09	46.8	41.0	1.14
Issa et al. (2016)	6-16N7	R	3.05	0.20	0.30	0.17	7.00	36	NW	BFRP	1060	51	3.74	41.6	43.0	0.97
	3-25N7	R	3.05	0.20	0.30	0.17	7.00	36	NW	BFRP	1060	48	4.64	49.8	44.5	1.12

Table 2 (continued)

Authors	Specimen	Cross-section	L (m)	b _w (m)	h (m)	d (m)	a/d	f _c (MPa)	Concrete type	FRP type	f _{tu} (MPa)	E _f (GPa)	ρ _f (%)	V _{c, test} (kN)	V _{c, KDS} (kN)	V _{c, test} /V _{c, KDS}
Acciaï et al. (2016)	4-25N7	R	3.05	0.20	0.30	0.17	7.00	36	NW	BFRP	1060	48	6.18	52.9	47.7	1.11
	D-G1×13	R	2.00	0.10	0.20	0.18	5.56	41	NW	GFRP	690	40.8	0.74	10.2	9.8	1.04
	D-G2×13	R	2.00	0.10	0.20	0.18	5.56	41	NW	GFRP	690	40.8	1.48	12.3	11.8	1.04
	D-C1×9	R	2.00	0.10	0.20	0.18	5.56	66	NW	CFRP	2068	124	0.35	9.1	12.9	0.71
	D-C2×9	R	2.00	0.10	0.20	0.18	5.56	66	NW	CFRP	2068	124	0.71	14.2	15.6	0.91
Kaszubska et al. (2018)	G-512-30-15	T	1.80	0.15	0.40	0.38	2.90	31	NW	GFRP	1281	51.5	0.99	35.3	26.4	1.33
	G-316-30-15	T	1.80	0.15	0.40	0.38	2.92	33	NW	GFRP	1205	51.5	1.07	32.8	27.7	1.19
	G-318-30-15	T	1.80	0.15	0.40	0.38	2.93	33	NW	GFRP	1109	51.5	1.35	39.6	29.5	1.34
	G-416-30-15	T	1.80	0.15	0.40	0.38	2.92	31	NW	GFRP	1205	51.5	1.42	35.8	29.2	1.23
	G-418-30-15	T	1.80	0.15	0.40	0.38	2.93	33	NW	GFRP	1109	51.5	1.80	39.2	31.9	1.23
	G-312/212-30-15	T	1.80	0.15	0.40	0.37	2.99	31	NW	GFRP	1281	51.5	1.02	35.8	26.7	1.34
	G-318/118-30-15	T	1.80	0.15	0.40	0.37	3.00	33	NW	GFRP	1109	51.5	1.85	48.8	32.3	1.51
	S1AN-0-1	I	6.00	0.10	0.65	0.57	3.53	34	NW	GFRP	1124	59	8.52	131.8	68.3	1.93
Kurth (2012)	S3AH-0-5	I	6.00	0.10	0.65	0.57	3.53	80	NW	GFRP	1124	59	11.36	189.8	98.6	1.92
	S5BN-0-9	I	6.00	0.10	0.65	0.57	3.50	43	NW	GFRP	1124	59	8.43	141.8	73.4	1.93
	S7BH-0-13	I	6.00	0.10	0.65	0.56	3.57	75	NW	GFRP	1000	62.6	11.46	210.8	103.4	2.04
	S9CN-0-17	I	6.00	0.10	0.65	0.57	3.50	37	NW	GFRP	1000	62.6	8.43	127.8	69.3	1.84
	I.1,2	R	1.20	0.11	0.22	0.20	2.50	35	NW	CFRP	2172	124	0.66	19.7	14.6	1.35
Spadea et al. (2017)	I.1,2	R	1.20	0.11	0.22	0.20	2.50	35	NW	CFRP	2172	124	0.66	19.7	14.6	1.35
Maranan et al. (2018)	GG-3.0-5	R	1.86	0.20	0.30	0.24	3.05	35	NW	GFRP	1184	62.6	2.10	63.9	40.5	1.58

f_c = concrete compressive strength; E_f, f_{tu} = elastic modulus and tensile strength of FRP rebars, respectively

ρ_f = longitudinal reinforcement ratio of FRP rebars

L, b_w, h, d = span length, web width, height, and effective depth of the beams, respectively

Cross section: R = rectangular, T = T-shape, I = I-shape

Concrete type: NW = normal-weight concrete, LW = lightweight concrete

Table 3 Database of FRP-RC beams with FRP shear reinforcement

Authors	Specimen	Dimension and geometry of beams							Concrete	FRP type	Longitudinal reinforcement		Shear reinforcement			$V_{n, test}$ (kN)	$V_{n, KDS}$ (kN)	$V_{n, test}/V_{n, KDS}$	
		Cross-section									f_{fu} (MPa)	E_{fl} (GPa)	ρ_{fl} (%)	f_{fvt} (MPa)	E_{fv} (GPa)				ρ_{fv} (%)
		L (m)	b _w (m)	h (m)	d (m)	a/d	f' _c (MPa)												
Maruyama and Zhao (1994)	FF1-20	R	3.00	0.15	0.30	0.25	3.00	36	NW	CFRP	1308	94.0	0.55	1308	94.0	0.12	61.6	48.4	1.27
	FF2-10	R	3.00	0.15	0.30	0.25	3.00	33	NW	CFRP	1308	94.0	1.10	1308	94.0	0.24	91.6	80.7	1.13
	FF1-10	R	3.00	0.15	0.30	0.25	3.00	38	NW	CFRP	1308	94.0	0.55	1308	94.0	0.24	86.6	74.4	1.16
	FF3-10	R	3.00	0.15	0.30	0.25	3.00	31	NW	CFRP	1308	94.0	1.39	1308	94.0	0.24	97.6	83.9	1.16
	FF2-20	R	3.00	0.15	0.30	0.25	3.00	35	NW	CFRP	1308	94.0	1.06	1308	94.0	0.12	75.4	56.3	1.34
	FF4-10	R	3.00	0.15	0.30	0.25	3.00	31	NW	CFRP	1308	94.0	2.11	1308	94.0	0.24	122.1	93.3	1.31
	FF4-13	R	3.00	0.15	0.30	0.25	3.00	31	NW	CFRP	1308	94.0	2.11	1308	94.0	0.18	88.6	75.8	1.17
	FF4-16	R	3.00	0.15	0.30	0.25	3.00	31	NW	CFRP	1308	94.0	2.11	1308	94.0	0.15	77.6	68.0	1.14
	FF4-20	R	3.00	0.15	0.30	0.25	3.00	35	NW	CFRP	1308	94.0	2.11	1308	94.0	0.12	85.1	65.3	1.30
	AA1060M	R	3.00	0.25	0.30	0.25	1.19	38	NW	GFRP	1167	61.0	1.90	1167	61.0	1.05	271.7	290.8	0.93
Okamoto et al. (1994)	AA1060M-C	R	3.00	0.25	0.30	0.25	1.19	37	NW	GFRP	1167	61.0	1.90	1167	61.0	1.05	252.1	287.6	0.88
	AA1090M	R	3.30	0.25	0.30	0.25	1.78	38	NW	GFRP	1167	61.0	1.90	1167	61.0	1.05	264.9	289.8	0.91
	AC0512M	R	3.60	0.25	0.30	0.25	1.78	33	NW	GFRP	1167	61.0	1.90	1167	61.0	0.51	158.9	165.7	0.96
	AC1060M-C	R	3.00	0.25	0.30	0.25	1.78	37	NW	GFRP	1167	61.0	1.90	1167	61.0	1.03	267.8	286.2	0.94
	AC1060M	R	3.00	0.25	0.30	0.25	1.19	38	NW	GFRP	1167	61.0	1.90	1167	61.0	1.03	278.6	288.0	0.97
	AC1090M	R	3.30	0.25	0.30	0.25	1.78	38	NW	GFRP	1167	61.0	1.90	1167	61.0	1.03	286.5	289.2	0.99
	AC1012M	R	3.60	0.25	0.30	0.25	1.78	33	NW	GFRP	1167	61.0	1.90	1167	61.0	1.03	229.6	278.7	0.82
	AC1560M	R	3.00	0.25	0.30	0.25	1.19	33	NW	GFRP	1167	61.0	1.90	1167	61.0	1.05	359.0	288.6	1.24
	AC1590L	R	3.30	0.25	0.30	0.25	1.78	29	NW	GFRP	1167	61.0	1.90	1167	61.0	1.05	217.8	279.1	0.78
	AC1512M	R	3.60	0.25	0.30	0.25	2.37	33	NW	GFRP	1167	61.0	1.90	1167	61.0	1.05	262.9	287.8	0.91
Nakamura and Higai (1995)	GG05-10	R	1.50	0.20	0.30	0.25	3.00	35	NW	GFRP	751	29.4	1.61	828	31.0	0.35	83.9	62.8	1.34
	GG10-10	R	1.50	0.20	0.30	0.25	3.00	33	NW	GFRP	751	29.4	1.61	828	31.4	0.35	100.6	65.9	1.53
Zhao et al. (1995)	GG05-20	R	1.50	0.20	0.30	0.25	3.00	35	NW	GFRP	751	29.4	1.61	828	31.0	0.18	56.0	43.7	1.28
	GG10-20	R	1.50	0.20	0.30	0.25	3.00	35	NW	GFRP	751	29.4	1.61	828	31.0	0.18	66.0	45.9	1.44
	#10	R	1.80	0.15	0.30	0.25	3.00	34	NW	CFRP	1124	105.0	3.03	1100	39.0	0.42	114.3	86.9	1.32
	#14	R	1.80	0.15	0.30	0.25	3.00	34	NW	CFRP	1124	105.0	3.03	1300	39.0	0.42	127.2	89.7	1.42
Maruyama (1996)	#16	R	1.80	0.15	0.30	0.25	3.00	34	NW	CFRP	1124	105.0	2.27	1100	39.0	0.42	117.5	83.8	1.40
	#19	R	2.00	0.15	0.30	0.25	4.00	34	NW	CFRP	1124	105.0	1.51	1100	39.0	0.42	74.4	69.8	1.07
	#25	R	1.80	0.15	0.30	0.25	2.50	34	NW	CFRP	1200	100.0	1.51	600	30.0	0.43	109.9	70.3	1.56

Table 3 (continued)

Authors	Specimen	Dimension and geometry of beams							Concrete	FRP type	Longitudinal reinforcement		Shear reinforcement			$V_{n, test}$ (kN)	$V_{n, KDS}$ (kN)	$V_{n, test}/V_{n, KDS}$	
		Cross-section	L (m)	b _w (m)	h (m)	d (m)	a/d	f' _c (MPa)			Longitudinal reinforcement		Shear reinforcement						
											f _{lu} (MPa)	E _{fl} (GPa)	ρ _{fl} (%)	f _{fv} (MPa)	E _{fv} (GPa)				ρ _{fv} (%)
Vijay et al. (1996)	#26	R	1.80	0.15	0.30	0.25	2.50	34	NW	CFRP	1200	100.0	1.51	600	30.0	0.43	109.9	70.3	1.56
	#27	R	1.80	0.15	0.30	0.25	2.50	34	NW	CFRP	1200	100.0	1.51	600	30.0	0.86	140.9	100.2	1.41
	#28	R	1.80	0.15	0.30	0.25	2.50	34	NW	CFRP	1200	100.0	1.51	600	30.0	0.86	140.9	100.2	1.41
	#30	R	2.50	0.30	0.55	0.50	2.50	34	NW	CFRP	1200	100.0	1.04	600	30.0	0.43	375.4	228.3	1.64
	#32	R	3.75	0.45	0.80	0.75	2.50	34	NW	CFRP	1200	100.0	1.04	600	30.0	0.43	607.7	448.0	1.36
	S2	R	0.00	0.15	0.30	0.27	1.89	45	NW	GFRP	655	54.0	1.43	655	54.0	0.83	127.8	133.4	0.96
Duranovic et al., (1997)	S3	R	0.00	0.15	0.30	0.27	1.89	45	NW	GFRP	655	54.0	1.43	655	54.0	0.56	116.0	102.4	1.13
	S5	R	0.00	0.15	0.30	0.27	1.89	31	NW	GFRP	655	54.0	0.67	655	54.0	0.83	124.2	120.0	1.04
	S6	R	0.00	0.15	0.30	0.27	1.89	31	NW	GFRP	655	54.0	0.67	655	54.0	0.56	124.3	91.0	1.37
	GB 11	R	0.00	0.15	0.25	0.21	3.65	40	NW	GFRP	1000	45.0	1.36	1000	45.0	0.17	49.8	36.9	1.35
Alsayed (1998)	GB 12	R	0.00	0.15	0.25	0.21	2.44	40	NW	GFRP	1000	45.0	1.36	1000	45.0	0.17	67.4	40.6	1.66
	B1	R	2.20	0.20	0.36	0.32	3.13	36	NW	GFRP	764	42.0	1.33	565	43.0	0.21	70.9	66.3	1.07
Shehata et al. (2000)	CC-3	T	5.00	0.14	0.56	0.47	3.19	50	NW	CFRP	2200	137.0	1.25	1730	137.0	0.36	309.8	248.7	1.25
	CG-3	T	5.00	0.14	0.56	0.47	3.19	50	NW	CFRP	2200	137.0	1.25	640	41.0	1.07	309.3	231.3	1.34
Alkhrdaji et al. (2001)	BM1	R	1.50	0.18	0.33	0.28	2.69	24	NW	GFRP	717	40.0	2.30	717	40.0	0.52	82.4	90.1	0.91
	BM2	R	1.50	0.18	0.33	0.28	2.69	24	NW	GFRP	717	40.0	2.30	717	40.0	0.39	71.8	74.9	0.96
Niewels (2008)	BM5	R	1.50	0.18	0.33	0.28	2.69	25	NW	GFRP	717	40.0	2.30	717	40.0	0.52	81.6	90.2	0.90
	BM6	R	1.50	0.18	0.33	0.28	2.69	25	NW	GFRP	717	40.0	1.19	717	40.0	0.39	53.5	65.7	0.81
	Q-C-1R	R	2.66	0.30	0.55	0.44	3.02	48	NW	GFRP	1000	63.0	3.65	322	31.0	0.54	364.7	271.1	1.35
	Q-C-2R	R	3.96	0.30	0.55	0.44	3.02	43	NW	GFRP	1000	63.0	3.65	322	31.0	0.38	245.4	210.4	1.17
Ascione et al. (2010)	Q-A-3R	R	3.90	0.30	0.50	0.41	3.16	43	NW	GFRP	480	44.0	3.25	1000	49.0	0.30	305.8	217.7	1.40
	Q-A-4R	R	3.90	0.30	0.50	0.41	3.16	47	NW	GFRP	480	44.0	3.25	1000	49.0	0.24	270.8	194.4	1.39
	I.1.2.3.4.5	R	2.00	0.15	0.20	0.17	4.12	20	NW	GFRP	970	46.0	0.62	970	46.0	0.29	21.0	28.2	0.74
	II.1.2.3.4.5	R	2.00	0.15	0.20	0.17	4.12	20	NW	GFRP	970	46.0	1.54	970	46.0	0.29	29.1	33.5	0.87
	III.1.2.3.4.5	R	2.00	0.15	0.20	0.17	4.12	25	NW	GFRP	970	46.0	0.62	970	46.0	0.29	24.0	29.3	0.82
V.1.2.3.4.5	IV.1.2.3.4.5	R	2.00	0.15	0.20	0.17	4.12	25	NW	GFRP	970	46.0	1.54	970	46.0	0.29	33.9	35.2	0.96
	V.1.2.3.4.5	R	2.00	0.15	0.20	0.17	4.12	20	NW	CFRP	2000	115.0	0.89	2000	115.0	0.29	39.8	63.3	0.63
	VII.1.2.3.4.5	R	2.00	0.15	0.20	0.17	4.12	25	NW	CFRP	2000	115.0	0.89	2000	115.0	0.29	40.3	64.1	0.63

Table 3 (continued)

Authors	Specimen	Dimension and geometry of beams							Concrete	FRP type	Longitudinal reinforcement		Shear reinforcement			$V_{n, test}$ (kN)	$V_{n, KDS}$ (kN)	$V_{n, test}/V_{n, KDS}$				
		Cross-section		beams							f'_c (MPa)	d (m)	a/d	f_{lu} (MPa)	E_{fl} (GPa)				ρ_{fl} (%)	f_{lv} (MPa)	E_{fv} (GPa)	ρ_{fv} (%)
		L (m)	b _w (m)	h (m)	d (m)	d'																
Bentz et al. (2010)	L20-1	R	7.10	0.45	1.00	0.86	3.56	36	NW	GFRP	397	37.1	2.23	397	40.8	0.09	425.0	268.8	1.58			
	L20-2	R	7.10	0.45	1.00	0.86	3.56	42	NW	GFRP	397	37.1	2.23	397	40.8	0.19	675.0	391.5	1.72			
	M20-1	R	3.05	0.45	0.50	0.41	3.77	35	NW	GFRP	397	37.1	2.36	397	40.8	0.09	151.5	149.9	1.01			
	FT	R	2.90	0.15	0.30	0.27	4.07	51	NW	BFRP	1100	70.0	0.39	1100	70.0	0.17	37.4	45.5	0.82			
Tomlinson and Fam (2015)																						
	FB	R	2.90	0.15	0.30	0.27	4.07	53	NW	BFRP	1100	70.0	0.51	1100	70.0	0.17	45.9	47.4	0.97			
	FC	R	2.90	0.15	0.30	0.25	4.49	52	NW	BFRP	1100	70	0.85	1100	70.0	0.168	54.50	49.6	1.10			
	S1AN-1.3-2	I	6.00	0.10	0.65	0.566	3.53	38	NW	GFRP	1124	59	8.52	1000	56.2	1.26	435.60	320.4	1.36			
Kurth (2012)																						
	S2AN-0.8-3	I	6.00	0.10	0.65	0.566	3.53	34	NW	GFRP	1124	59	8.52	1000	56.2	0.75	340.60	224.3	1.52			
	S2AN-2.3-4	I	6.00	0.10	0.65	0.566	3.53	34	NW	GFRP	1124	59	8.52	1000	56.2	2.26	494.60	473.9	1.04			
	S3AH-1.3-6	I	6.00	0.10	0.65	0.566	3.53	82	NW	GFRP	1124	59	11.36	1000	56.2	1.26	579.60	365.1	1.59			
Matta et al. (2013)	S4AH-0.8-7	I	6.00	0.10	0.65	0.566	3.53	42	NW	GFRP	1124	59	11.36	1000	56.2	0.75	334.60	233.8	1.43			
	S4AH-2.3-8	I	6.00	0.10	0.65	0.566	3.53	43	NW	GFRP	1124.00	59.00	11.36	1000	56.2	2.26	553	503.9	1.10			
	S5BN-1.3-10	I	6.00	0.10	0.65	0.57	3.50	43	NW	GFRP	1124	59.0	8.43	1000	57.0	1.26	447.6	329.4	1.36			
	S6BN-0.8-11	I	6.00	0.10	0.65	0.57	3.50	30	NW	GFRP	1000	62.6	8.43	1000	57.0	0.75	310.6	222.2	1.40			
	S6BN-2.3-12	I	6.00	0.10	0.65	0.57	3.50	31	NW	GFRP	1000	62.6	8.43	1000	57.0	2.26	456.6	479.8	0.95			
	S7BH-1.3-14	I	6.00	0.10	0.65	0.56	3.57	76	NW	GFRP	1000	62.6	11.46	1000	57.0	1.26	634.6	373.5	1.70			
	S8BH-0.8-15	I	6.00	0.10	0.65	0.56	3.57	73	NW	GFRP	1000	62.6	11.46	1000	57.0	0.75	447.6	264.9	1.69			
	S8BH-2.3-16	I	6.00	0.10	0.65	0.56	3.57	70	NW	GFRP	1000	62.6	11.46	1000	57.0	2.26	589.6	525.4	1.12			
	S1-0.12-MA	R	7.32	0.46	0.98	0.88	3.10	39	NW	GFRP	476	41.0	0.60	690	40.2	0.22	290.3	319.8	0.91			
	Kral (2014)																					
		BM12-220	R	1.35	0.20	0.33	0.27	2.50	47	NW	GFRP	1000	60.0	1.82	900	50.0	0.51	191.8	137.8	1.39		
		BM12-150	R	1.35	0.20	0.33	0.27	2.50	47	NW	GFRP	1000	60.0	1.82	900	50.0	0.75	203.2	172.0	1.18		
BM16-220		R	1.35	0.20	0.35	0.27	2.50	47	NW	GFRP	1000	60.0	2.23	900	50.0	0.51	155.2	134.6	1.15			
BM16-150		R	1.35	0.20	0.35	0.27	2.50	47	NW	GFRP	1000	60.0	2.23	900	50.0	0.75	208.8	176.6	1.18			
BM25-220		R	1.35	0.20	0.35	0.27	2.50	47	NW	GFRP	1000	60.0	2.51	900	50.0	0.51	180.6	141.4	1.28			
BM25-150		R	1.35	0.20	0.35	0.27	2.50	47	NW	GFRP	1000	60.0	2.51	900	50.0	0.75	208.5	178.8	1.17			
BM25-s230		R	1.35	0.23	0.35	0.27	2.50	47	NW	GFRP	1000	60.0	1.58	900	50.0	1.19	234.1	263.4	0.89			
BM16-s230		R	1.35	0.23	0.36	0.27	2.50	47	NW	GFRP	1000	60.0	1.94	900	50.0	1.19	225.7	266.1	0.85			
BM12-s230		R	1.35	0.23	0.37	0.27	2.50	47	NW	GFRP	1000	60.0	2.18	900	50.0	1.19	222.7	268.0	0.83			
JSC32-22B		R	3.36	0.40	0.65	0.58	2.92	32	NW	GFRP	1204	61.2	1.04	911	57.5	0.28	392.5	328.2	1.20			

Table 3 (continued)

Authors	Specimen	Dimension and geometry of beams							Concrete type	FRP type	Longitudinal reinforcement		Shear reinforcement			$V_{n, test}$ (kN)	$V_{n, KDS}$ (kN)	$V_{n, test}/V_{n, KDS}$		
		Cross-section		L (m)	b_w (m)	h (m)	d (m)	a/d			f'_c (MPa)	f_t (MPa)	E_n (GPa)	ρ_n (%)	f_{tu} (MPa)				E_{fv} (GPa)	ρ_{fv} (%)
Issa et al. (2016)	JSC32-40B	R	3.36	0.40	0.65	0.58	2.92	32	NW	GFRP	1204	61.2	1.04	911	57.5	0.37	456.0	397.9	1.15	
	JSC32-50B	R	3.36	0.40	0.65	0.58	2.92	32	NW	GFRP	1204	61.2	1.04	911	57.5	0.50	553.0	498.1	1.11	
	JSV40-22B	R	3.36	0.40	0.65	0.58	2.92	40	NW	GFRP	1264	71.2	1.03	655	41.5	0.32	380.0	303.8	1.25	
	JSV40-40B	R	3.36	0.40	0.65	0.58	2.92	40	NW	GFRP	1264	71.2	1.03	655	41.5	0.42	453.0	364.0	1.24	
	JSV40-50B	R	3.36	0.40	0.65	0.58	2.92	40	NW	GFRP	1264	71.2	1.03	655	41.5	0.57	539.0	449.1	1.20	
	JSC100-50B	R	3.36	0.40	0.65	0.58	2.92	102	NW	GFRP	1204	61.2	1.04	911	57.5	0.50	565.5	530.0	1.07	
Maranan et al. (2018)	2-13SB1	R	3.05	0.20	0.30	0.28	1.50	36	NW	BFRP	1060	51.0	0.50	1070	53.0	0.54	149.1	117.6	1.27	
	3-13SB1	R	3.05	0.20	0.30	0.28	1.50	36	NW	BFRP	1060	51.0	0.75	1070	53.0	0.54	197.4	125.5	1.57	
	3-16SB1	R	3.05	0.20	0.30	0.27	1.50	36	NW	BFRP	1060	51.0	1.17	1070	53.0	0.54	215.6	133.8	1.61	
	2-25B1	R	3.05	0.20	0.30	0.27	1.50	36	NW	BFRP	1060	51.0	1.92	1070	53.0	0.54	193.7	140.4	1.38	
	3-16B2	R	3.05	0.20	0.30	0.27	2.50	36	NW	BFRP	1060	51.0	1.17	1070	53.0	0.54	136.5	125.9	1.08	
	3-16B3	R	3.05	0.20	0.30	0.27	3.50	36	NW	BFRP	1060	51.0	1.17	1070	53.0	0.54	93.1	118.0	0.79	
Imjai (2007)	GG-3.0-5-S100	R	1.86	0.20	0.30	0.24	3.05	35	NW	GFRP	1184	62.6	2.10	1029	50.0	0.95	202.4	180.5	1.12	
	GG-3.0-5-S100	R	1.86	0.20	0.30	0.24	3.05	35	NW	GFRP	1184	62.6	2.10	1029	50.0	0.72	187.4	150.9	1.24	
	GG-3.0-5-S150	R	1.86	0.20	0.30	0.24	3.05	35	NW	GFRP	1184	62.6	2.10	1029	50.0	0.48	150.4	116.1	1.30	
	GG-3.0-5-S100	R	1.86	0.20	0.30	0.24	3.05	35	NW	GFRP	1184	62.6	2.10	1029	50.0	0.72	156.4	145.6	1.07	
	TB2B	R	2.30	0.15	0.25	0.22	3.50	48	NW	GFRP	1000	60.0	1.22	720	27.9	0.37	66.5	47.8	1.39	
	TB4B	R	2.30	0.15	0.25	0.22	3.50	48	NW	GFRP	750	45.0	1.30	720	27.9	0.36	60.0	44.4	1.35	
Yang (2014)	TB5B	R	2.30	0.15	0.25	0.22	3.50	48	NW	GFRP	750	45.0	1.30	720	27.9	0.48	67.8	51.5	1.32	
	GB50-P150	R	2.30	0.15	0.25	0.22	3.52	35	NW	GFRP	758	46.0	0.81	720	27.9	0.27	30.7	30.3	1.01	
	CB51-P150	R	2.30	0.15	0.25	0.22	3.52	35	NW	CFRP	758	124.0	0.81	720	27.9	0.27	42.6	38.6	1.10	
	GB52-P80	R	1.80	0.15	0.25	0.22	2.75	35	NW	GFRP	2068	46.0	0.81	720	27.9	0.50	47.7	44.1	1.08	
	C000-C4-3	I	1.22	0.08	0.41	0.37	3.00	62	NW	CFRP	2930	149.0	2.92	2840	150.0	0.98	208.3	272.2	0.77	
	Spadea et al. (2017)	II.1.2	R	1.20	0.11	0.22	0.20	2.50	35	NW	CFRP	2172	124.0	0.66	1313	100.8	0.13	60.3	37.5	1.61

f'_c = concrete compressive strength; E_{fi} , f_{tu} , ρ_{fi} = elastic modulus, tensile strength, and reinforcement ratio of FRP longitudinal rebars, respectively; E_{fv} , f_{tu} , ρ_{fv} = elastic modulus, tensile strength, and reinforcement ratio of FRP shear rebars, respectively; L, b_w, h, d = span length, web width, height, and effective depth of the beams, respectively. Cross section: R = rectangular, T = T-shape, I = I-shape. Concrete type: NW = normal-weight concrete, LW = lightweight concrete

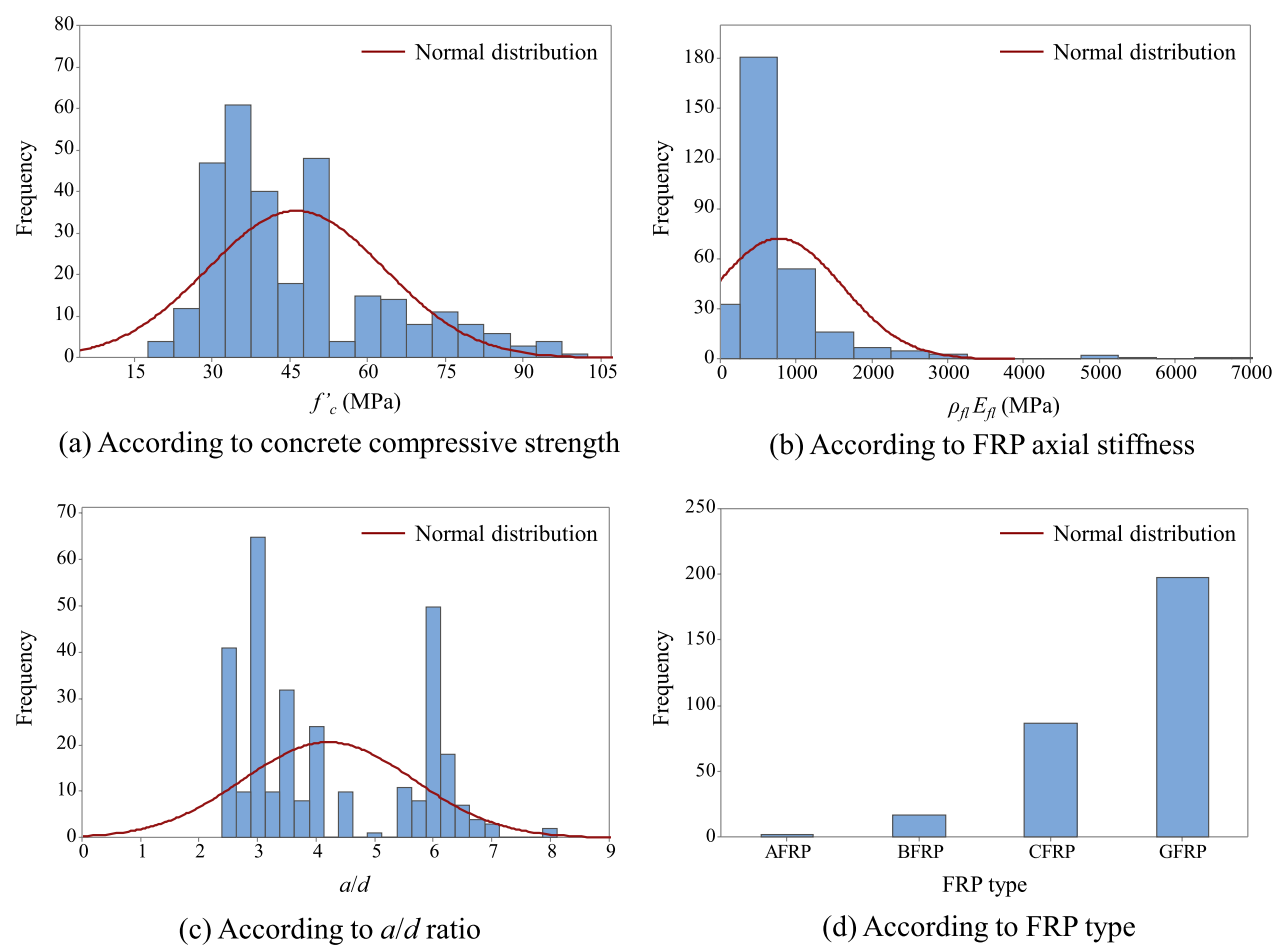


Fig. 2 Distribution of design parameters for the database of specimens without stirrups (304 specimens)

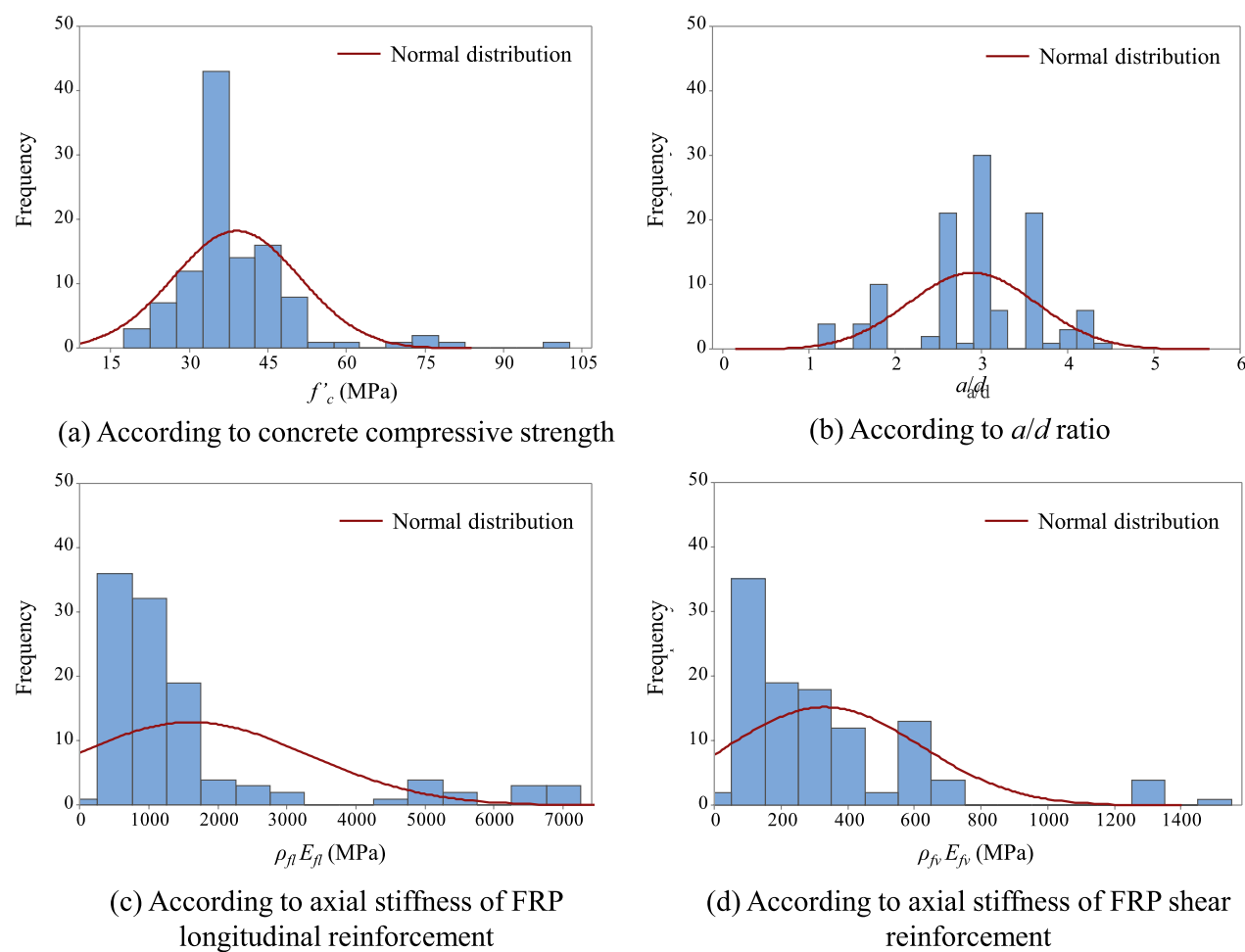


Fig. 3 Distribution of design parameters for the database of specimens with stirrups (110 specimens)

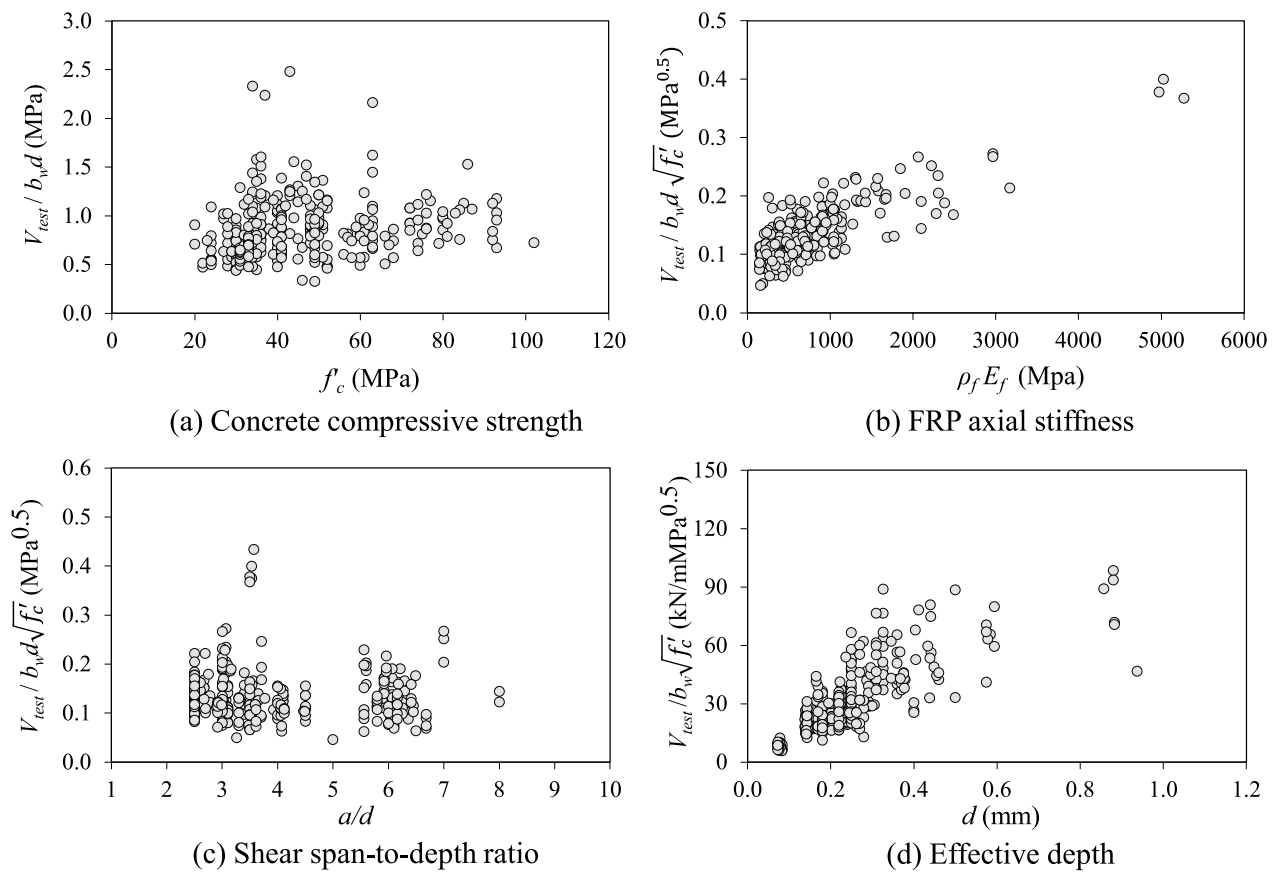


Fig. 4 Effect of primary design parameters on the normalized one-way shear strength of FRP-RC specimens

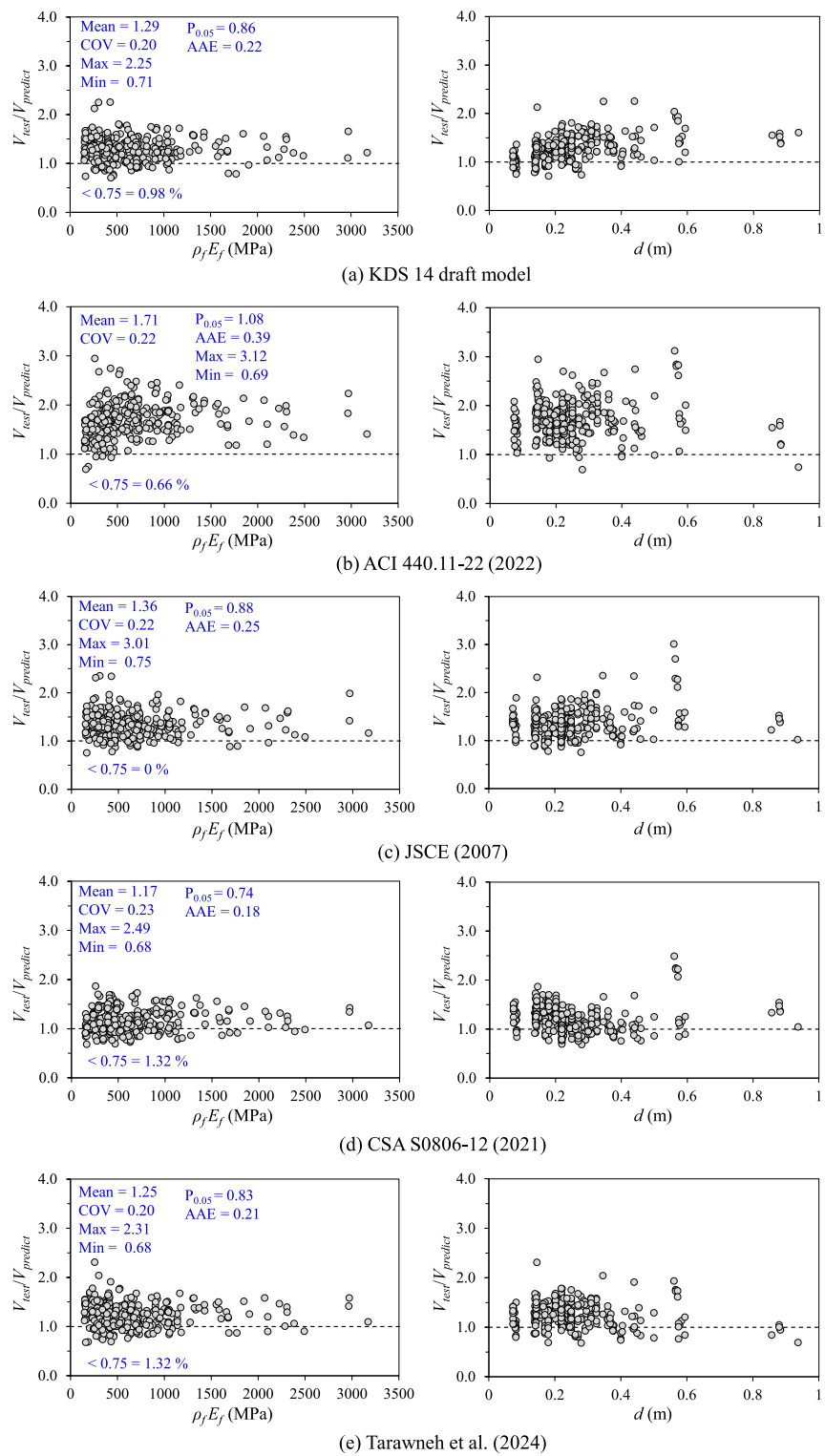


Fig. 5 Comparative analysis of the shear strength ratios using different design codes for specimens without FRP stirrups

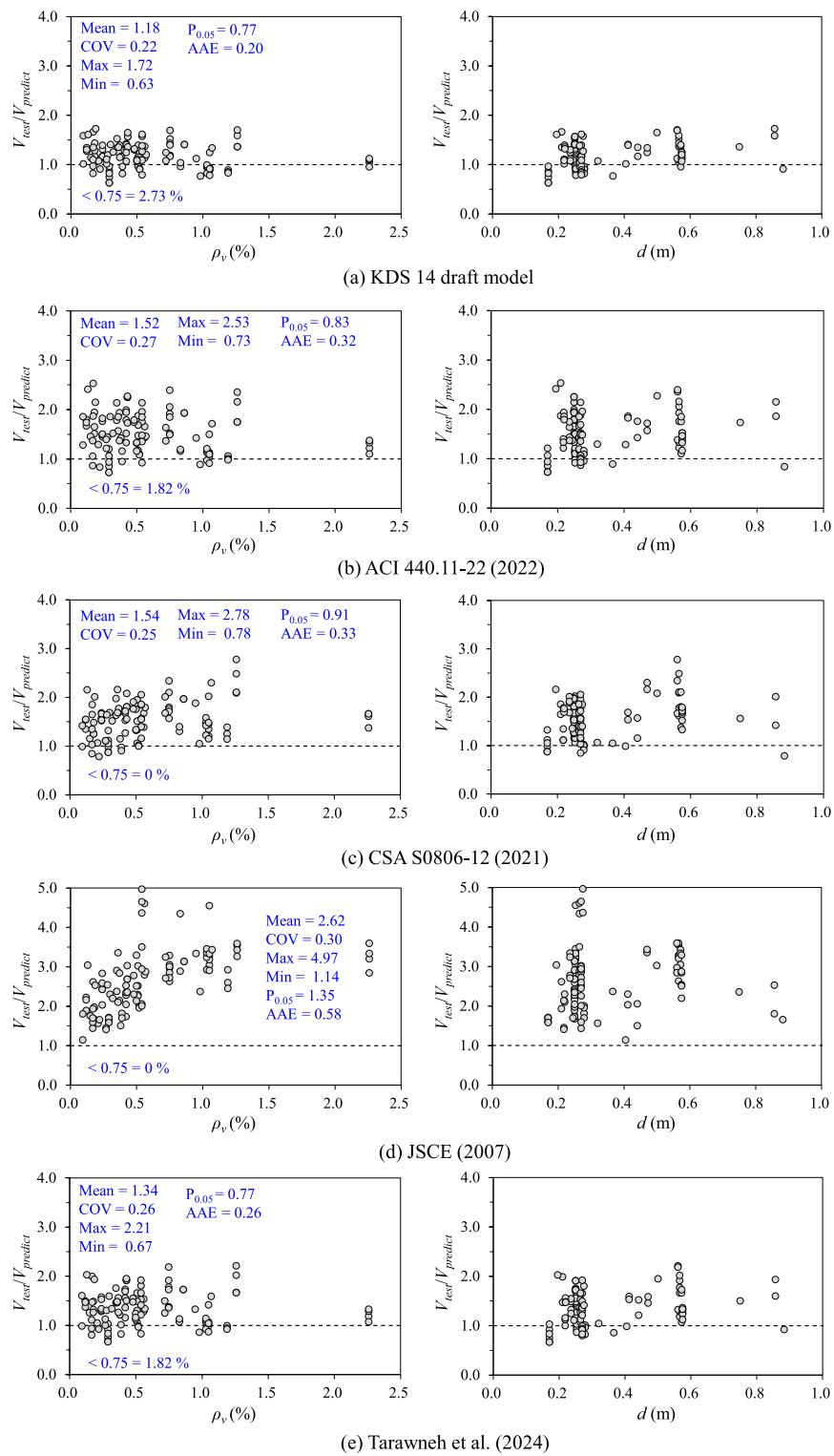


Fig. 6 Comparative analysis of the shear strength ratios using different design codes for specimens with FRP stirrups

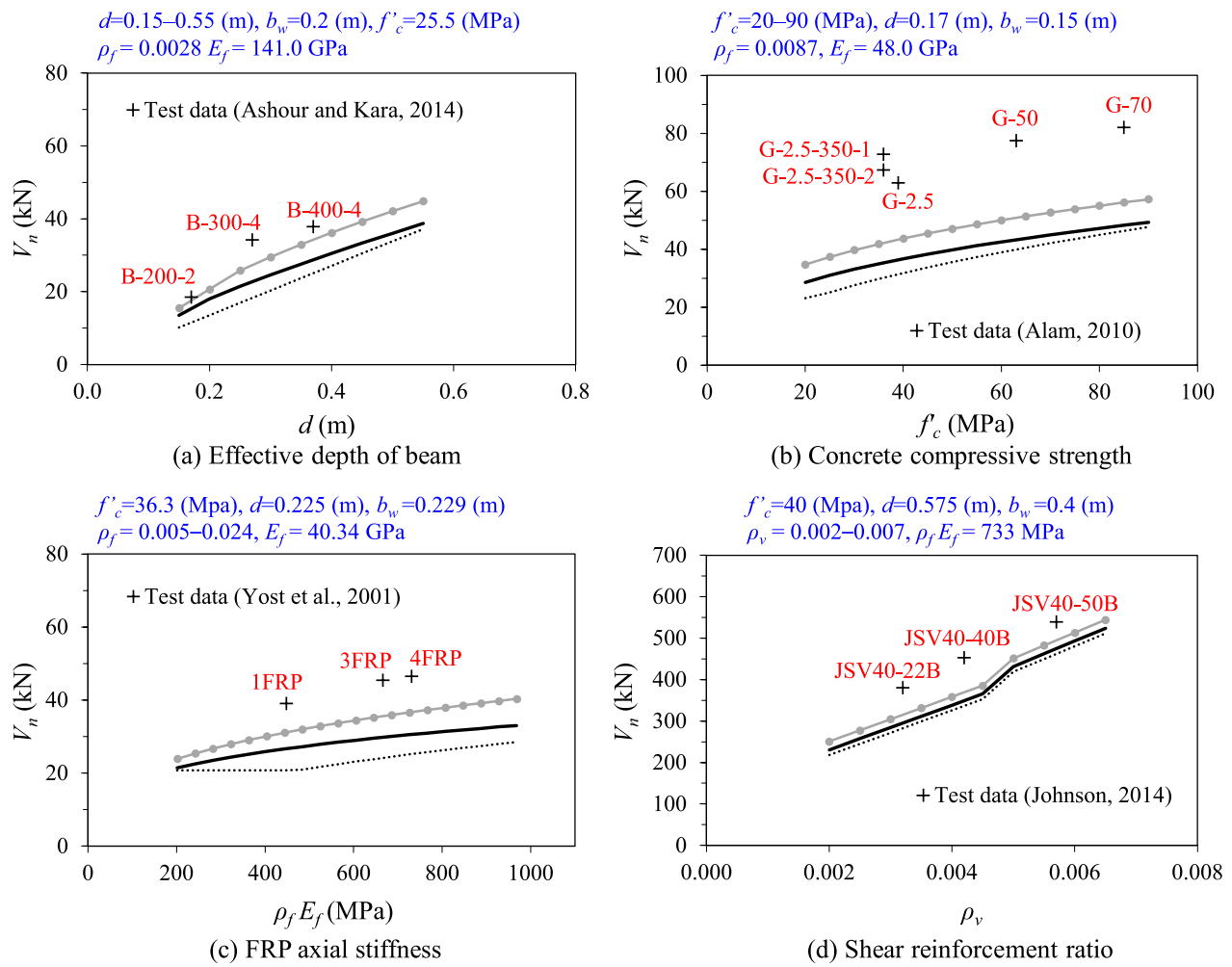


Fig. 7 Parametric study using KDS 14 draft and existing design models

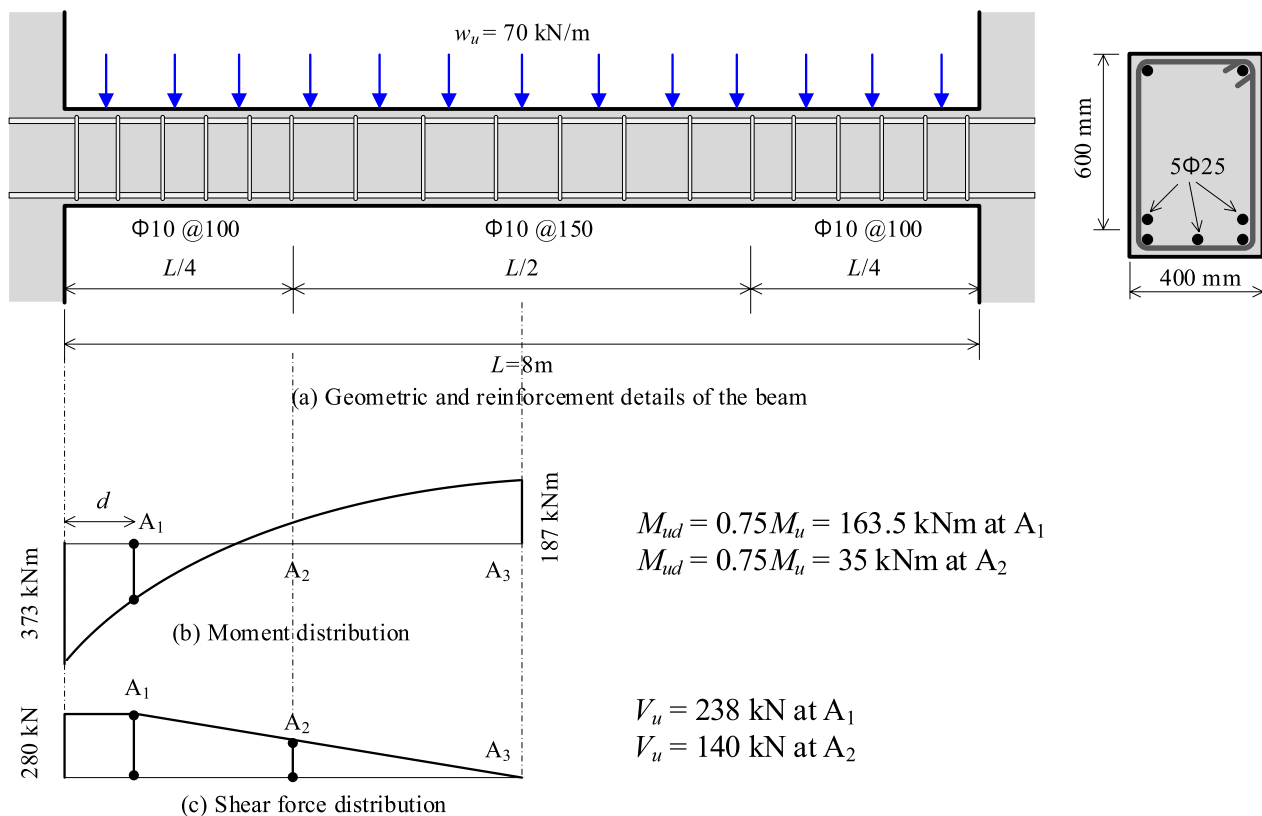


Fig. 8 Shear design example for FRP-RC beam using the KDS 14 draft model

Competing Interests

The authors declare no competing interests.

Appendix: Database for one-way shear tests of FRP-RC members.

See Tables 2, 3.

Acknowledgements

The authors gratefully acknowledge the financial support provided by the Basic Science Research Program of the National Research Foundation of Korea (Grant nos. NRF-2022R1A2C2004351 and NRF-2020R1A6A1A03044977).

Author Contributions

N.H.D: conceptualization, methodology, data curation, writing—original draft. S.-H. K: data curation, investigation. K.-K. C: conceptualization, writing—original draft, review and editing, funding acquisition. All the authors read and approved the final manuscript.

Availability of Data and Materials

The authors declare that the datasets used or analyzed during the current study are available from the corresponding author on reasonable request.

Declarations

Ethics Approval and Consent to Participate

Not applicable.

Consent for Publication

Not applicable.

Received: 20 November 2024 Accepted: 18 May 2025

Published online: 07 August 2025

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