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College Station, TX



# MACHINE LEARNING-BASED MIX DESIGN TOOLS TO MINIMIZE CARBON FOOTPRINT AND COST OF UHPC

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*Postdoctoral Researcher*

*Zachry Department of Civil and Environmental Engineering*

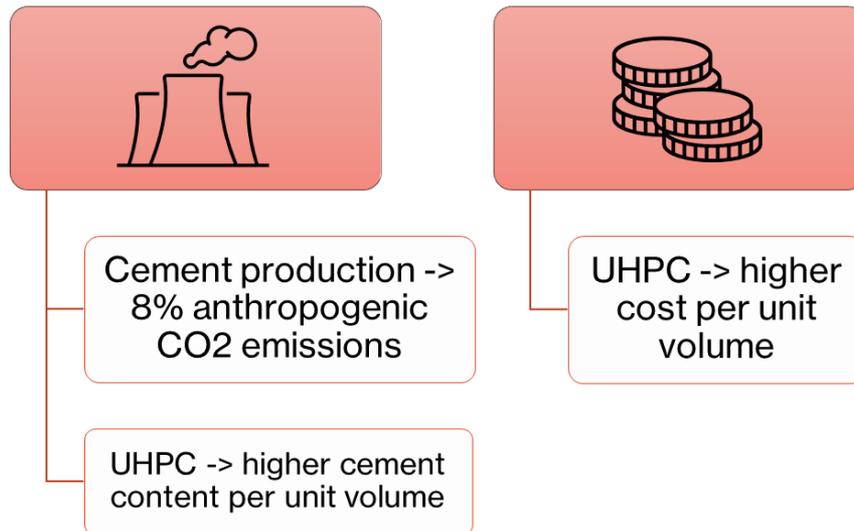
*Texas A&M University*



# MOTIVATION OF THIS STUDY

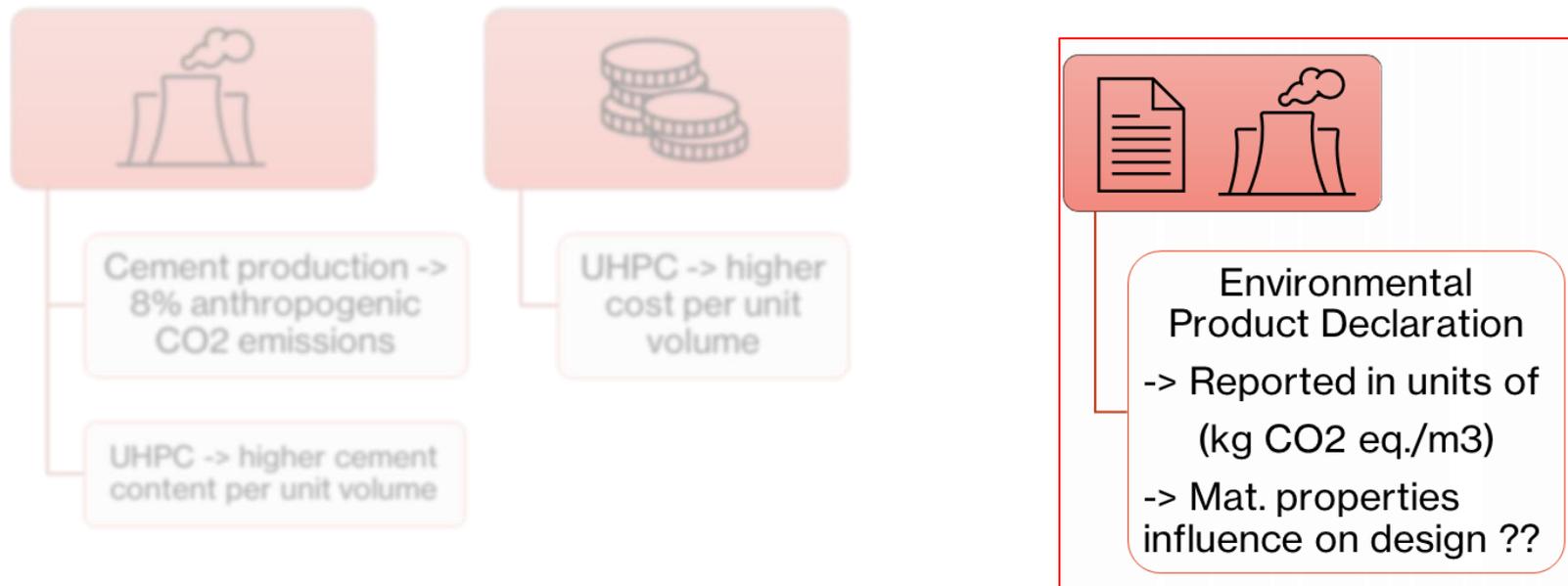
# Problem Statement

## Emergence of UHPC vs Global Sustainability Efforts



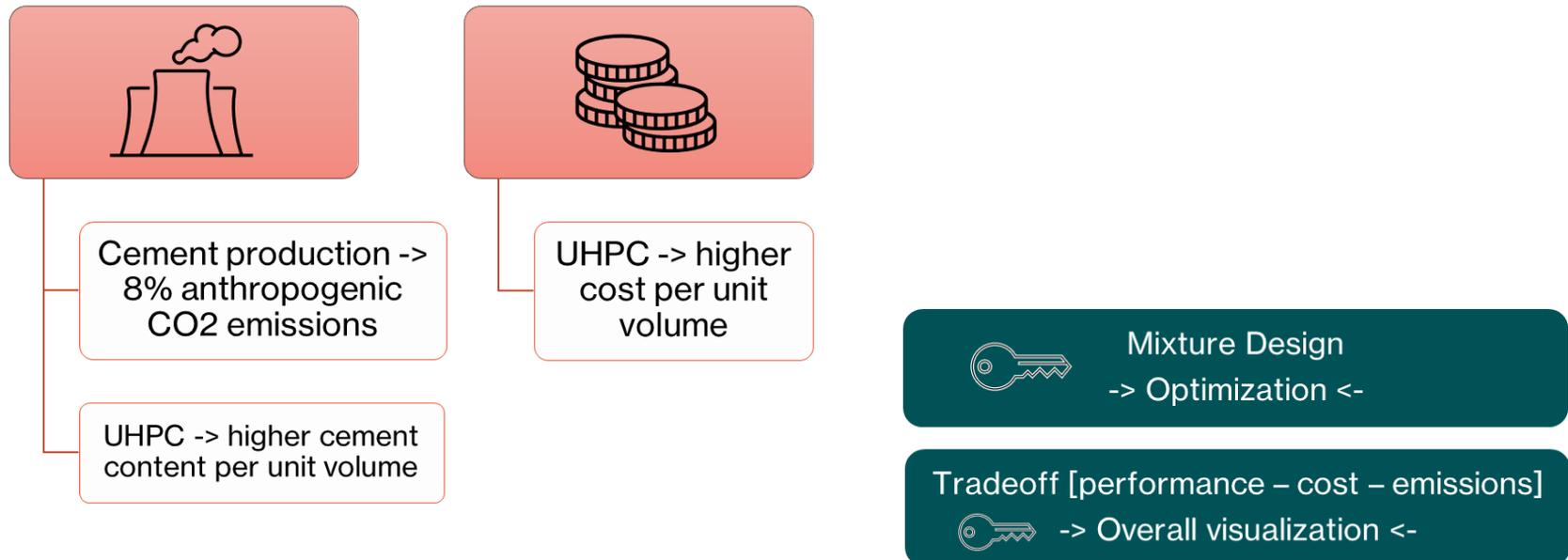
# Problem Statement

## Emergence of UHPC vs Global Sustainability Efforts



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## Emergence of UHPC vs Global Sustainability Efforts





# Research Questions

# Key questions addressed in this research

1. Can we accurately estimate the relationship between **compressive strength** and **mix proportions** of UHPC with a **few experimental runs & ML models**?
2. Can we evaluate the effect of changes in mix proportioning on mechanical performance in an easy and intuitive way?
3. Can we evaluate the effect of mix proportioning & mechanical performance on cost and eco-efficiency concurrently?
4. Are high paste content, high strength (and ultra-high strength) concrete technologies detrimental to cost and/or eco efficiencies?

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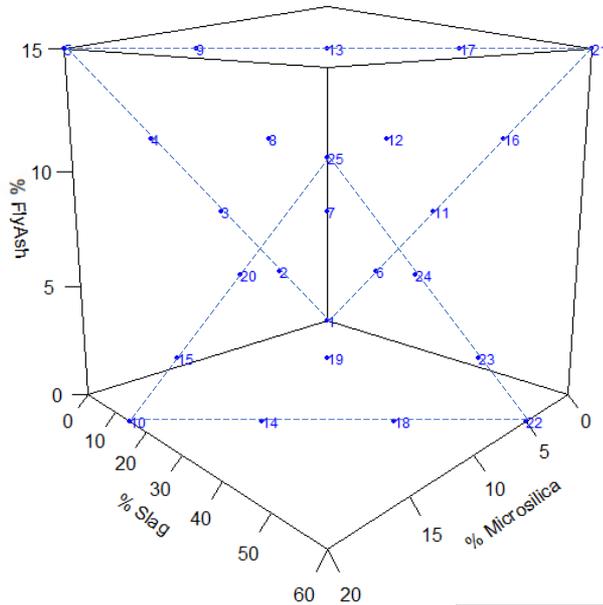
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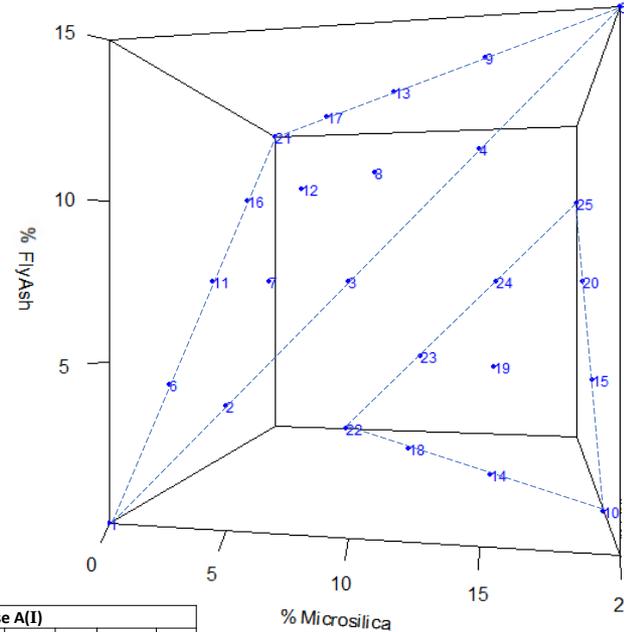
# Conceptual Framework

# Reduced experimental runs

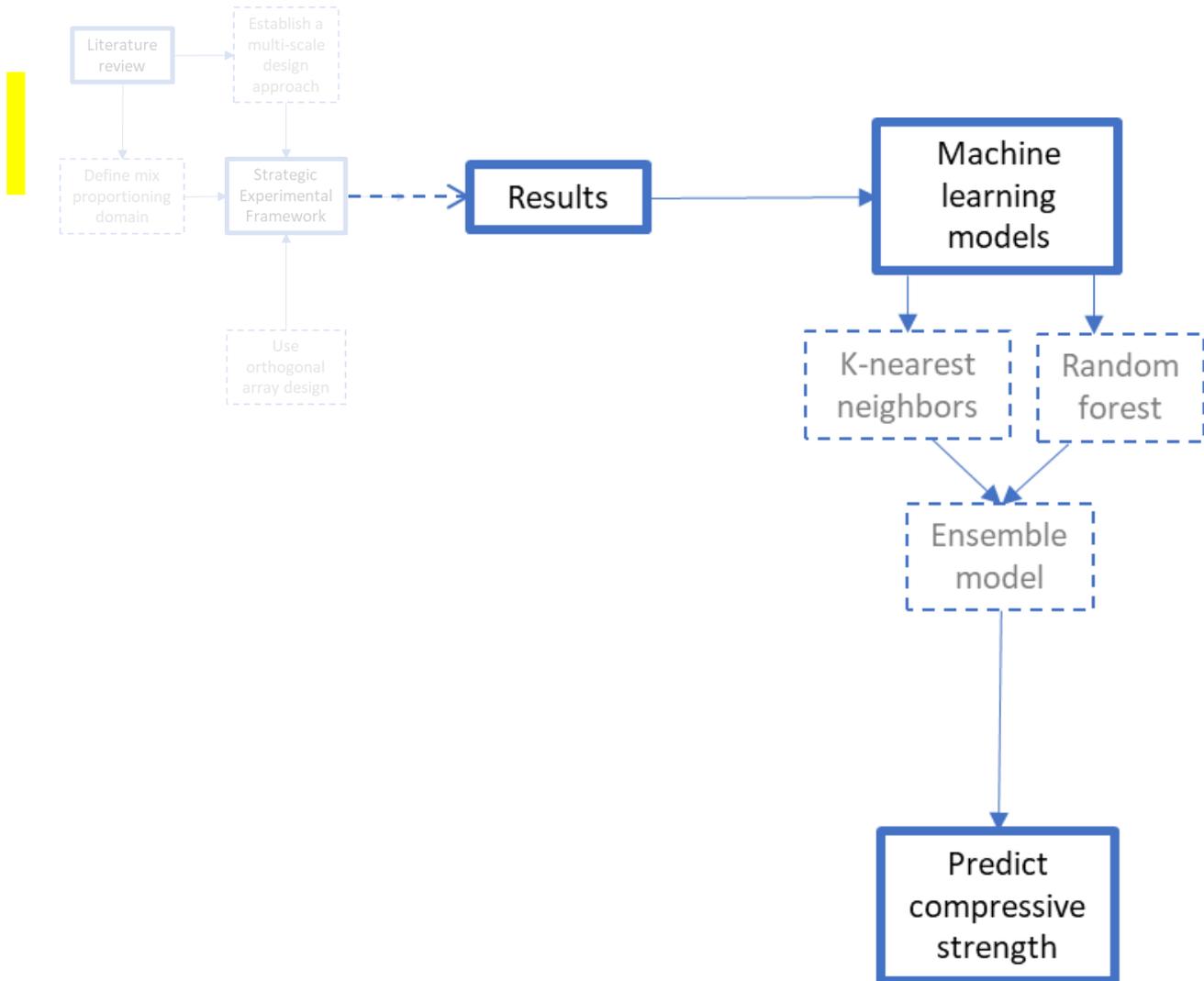
L25 Orthogonal array

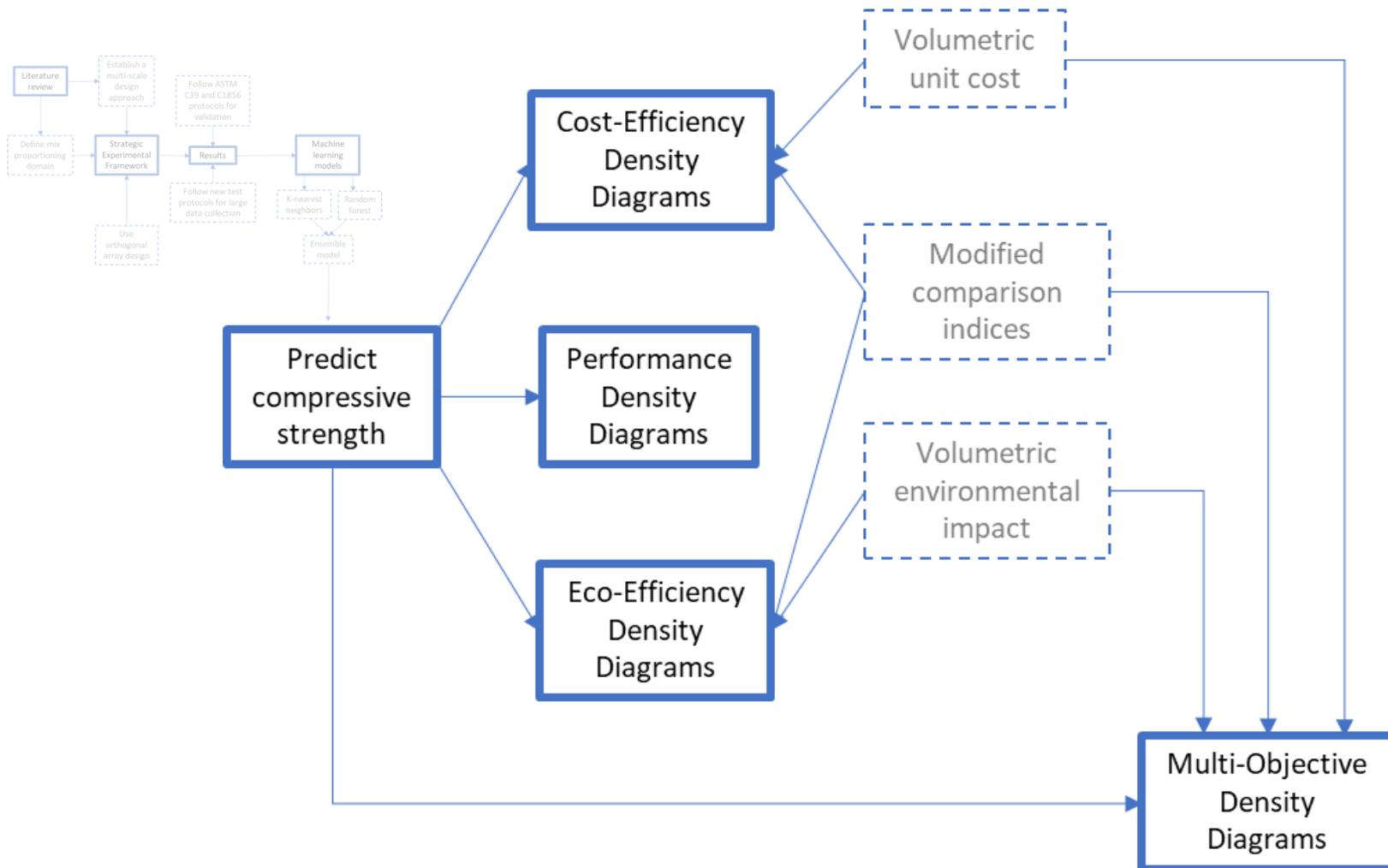


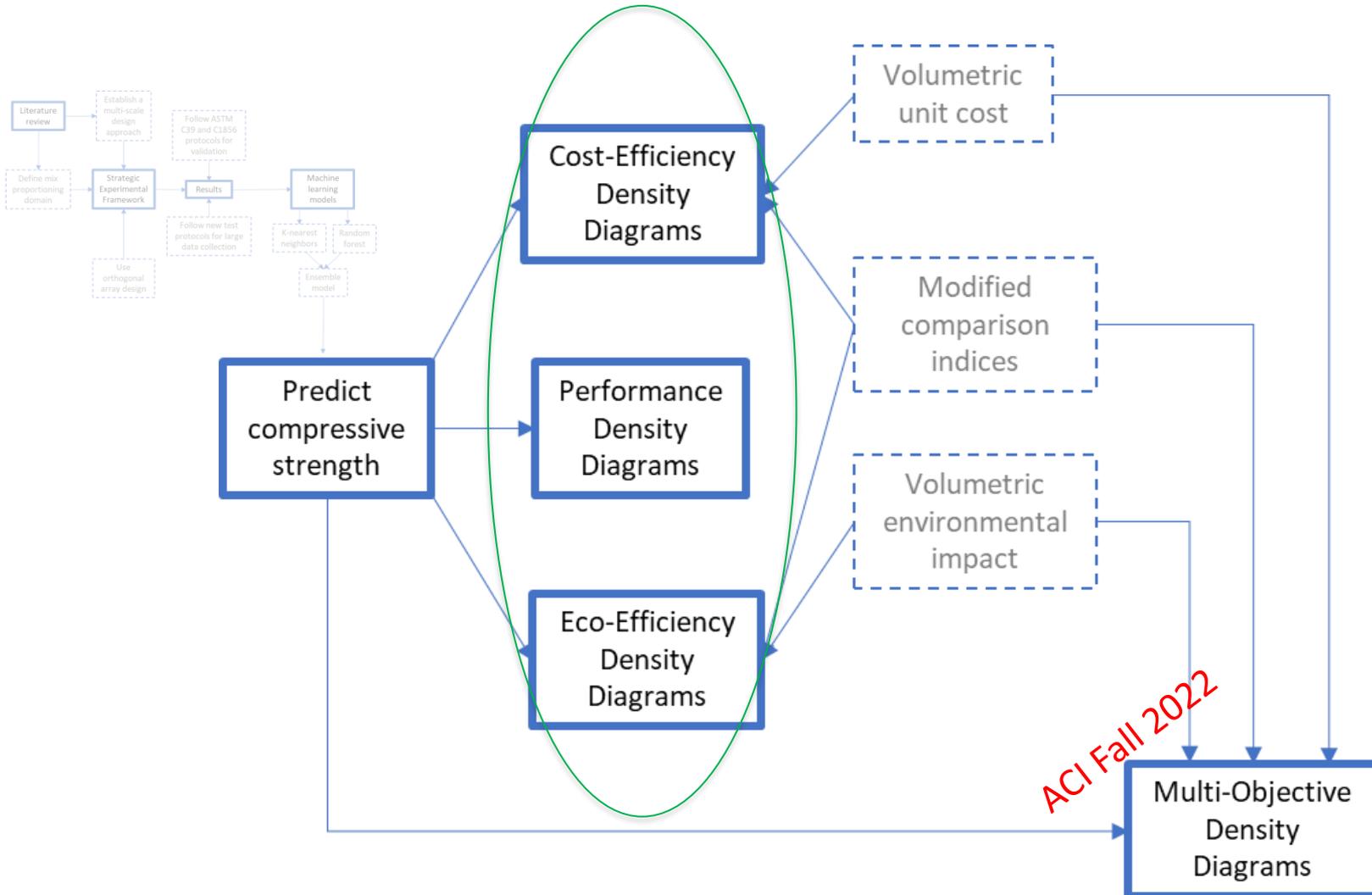
L25 Orthogonal array



		Phase A(I)				
Levels		1	2	3	4	5
Features	Slag	0	15	30	45	60
	Microsilica	0	5	10	15	20
	Fly Ash	0	3.75	7.5	11.25	15







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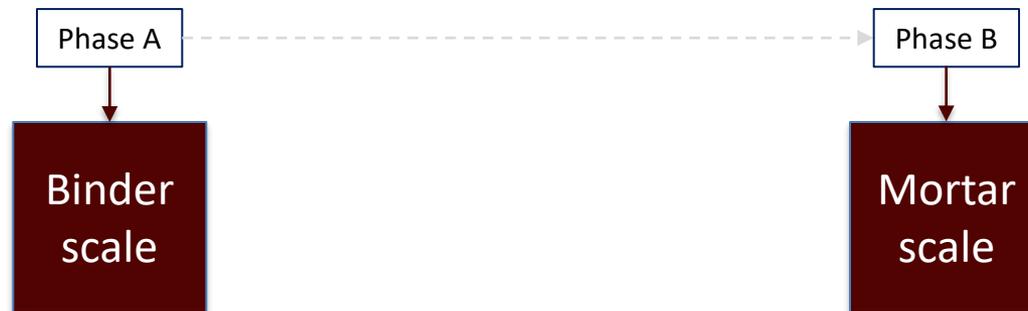


# METHODOLOGY

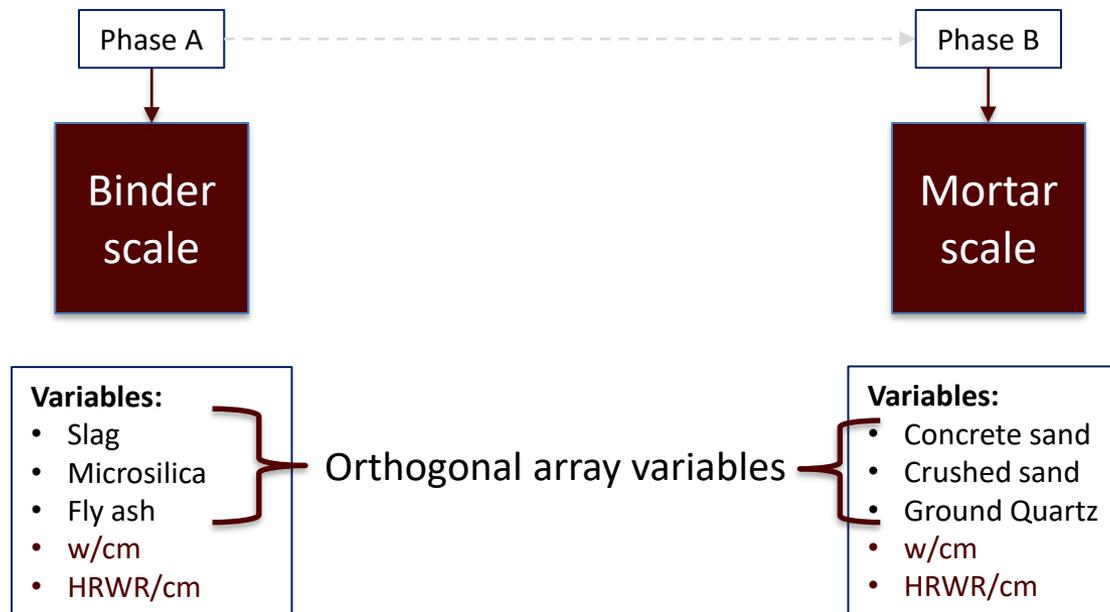
# Design strategy



# Design strategy



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# MODELING

# Modeling

Methods/algorithms:

- kNN
- Random Forest
- Linear regression (polynomial models)

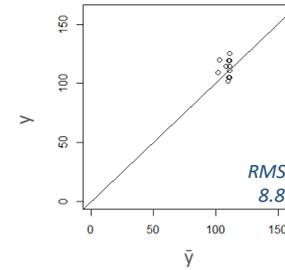
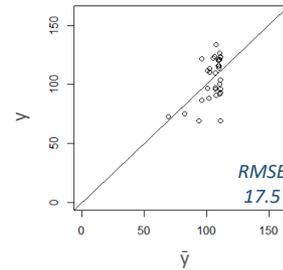
# Modeling

Model

Train set

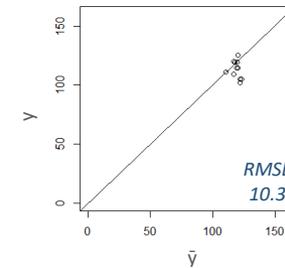
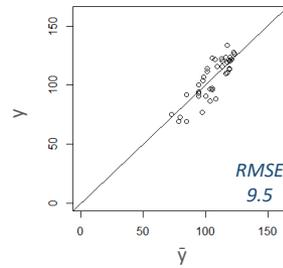
Optimum Test set

poly3\_avg\_84\_Phase A(I)+A(II)  
with 3 variables



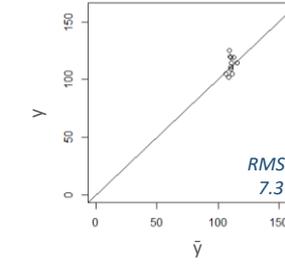
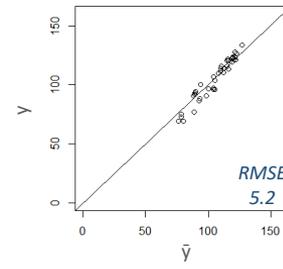
kNN\_avg\_100\_Phase A(I)+A(II)  
with 4 variables

Cross validation RMSE  
12.8



RF\_avg\_100\_Phase A(I)+A(II)  
with 4 variables

Bootstrap aggregation RMSE  
12.8



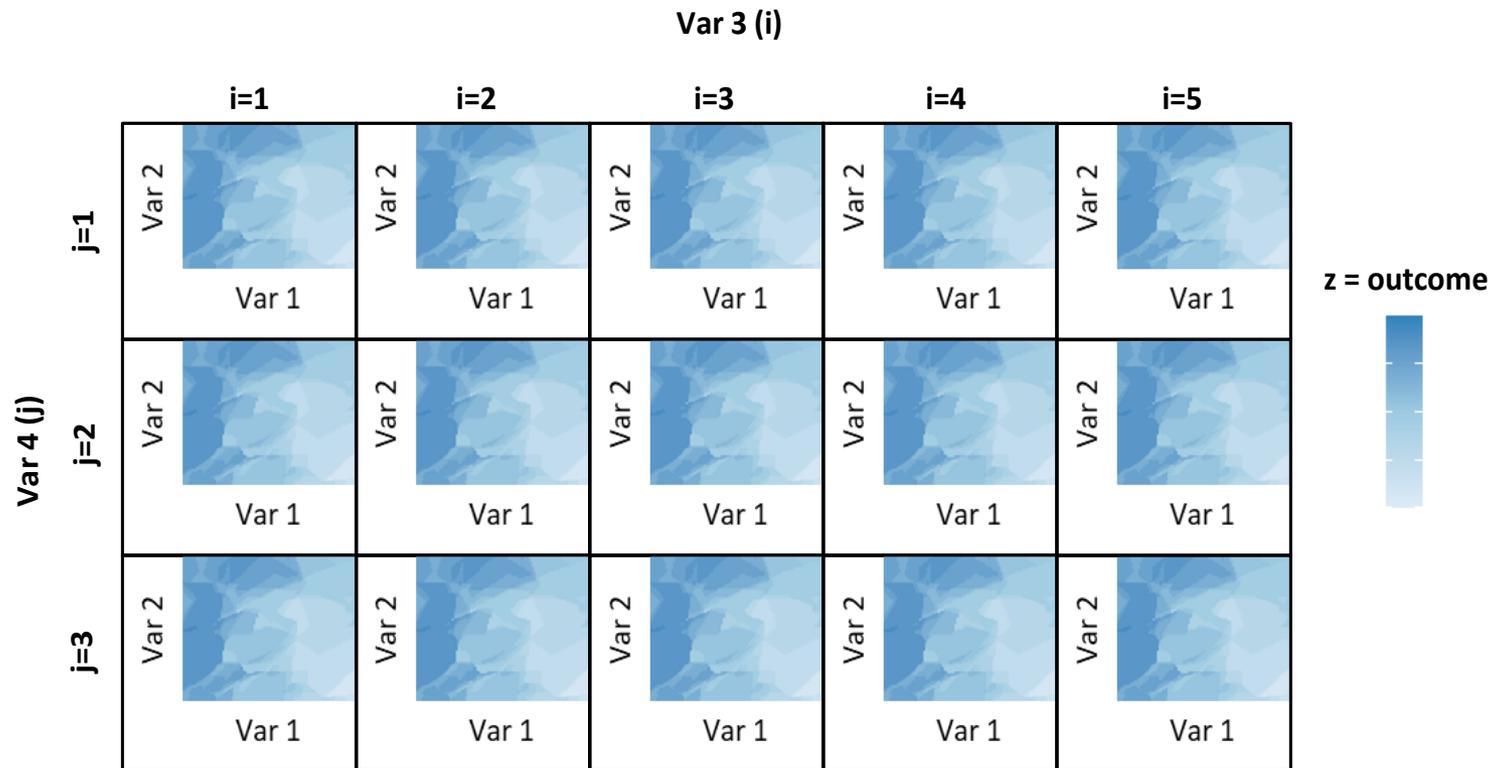
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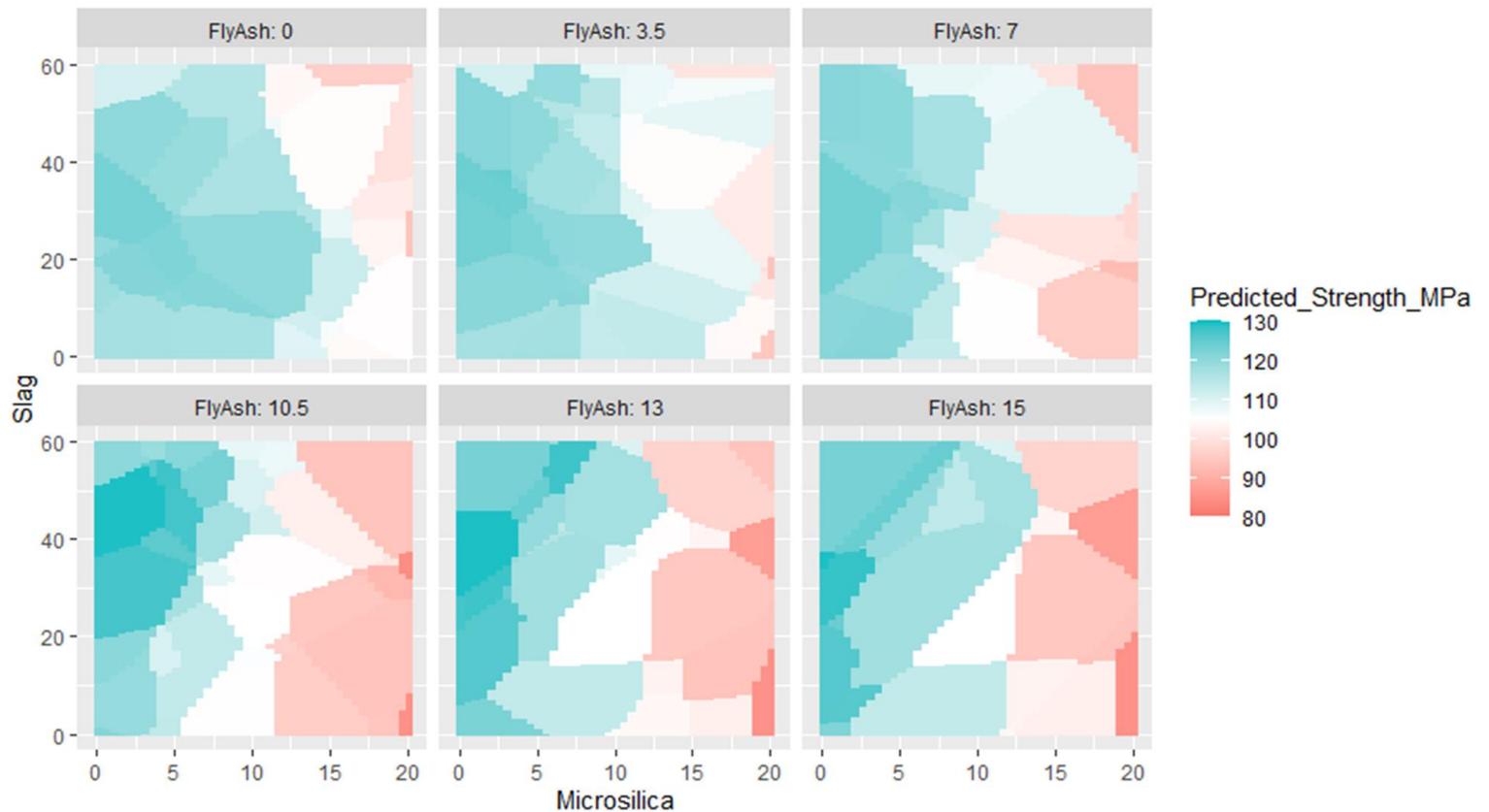
# Performance Density Diagrams

# PDD



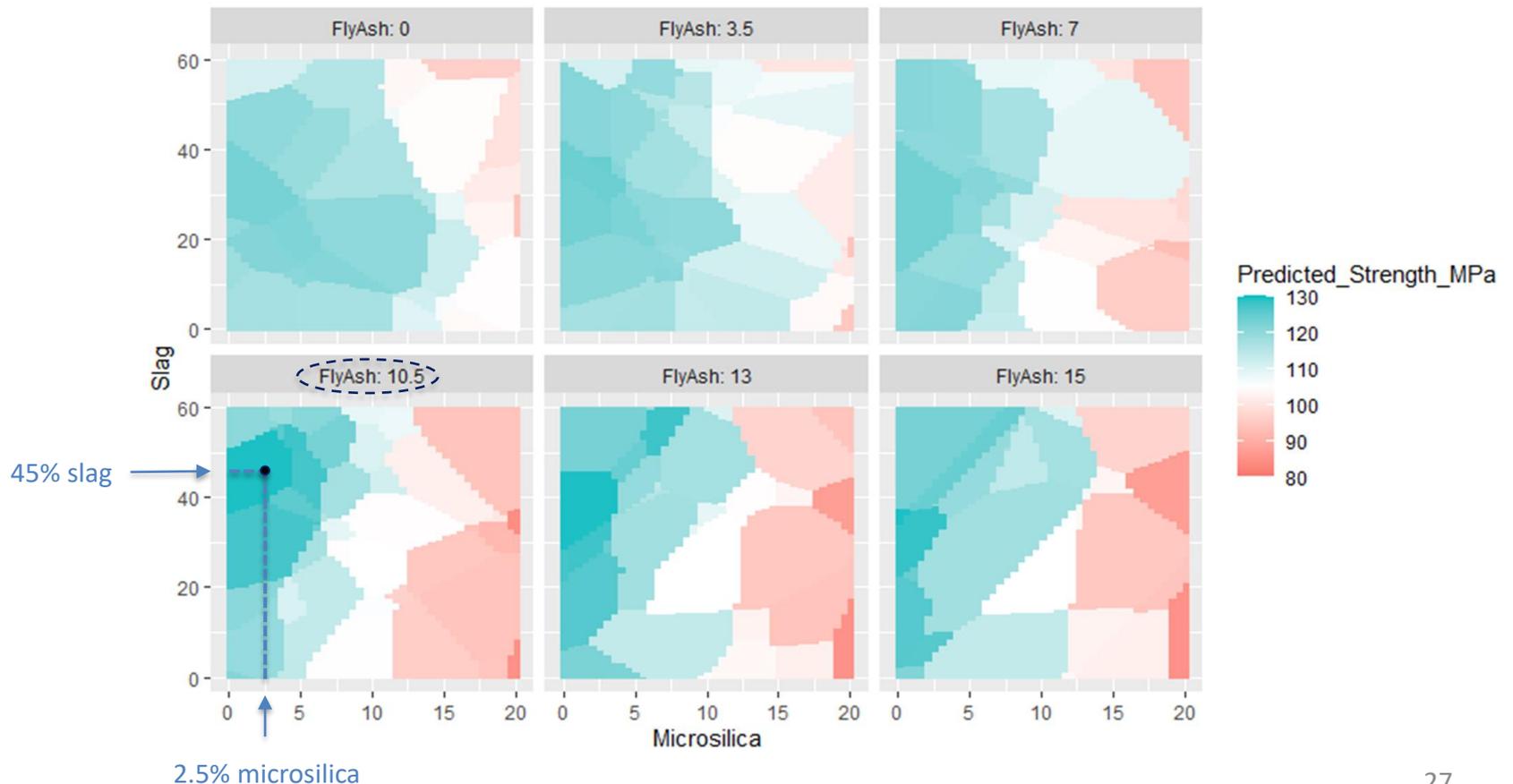
# PDD

1. Use to optimize a certain material property (e.g.,  $f_c = 130$  MPa)



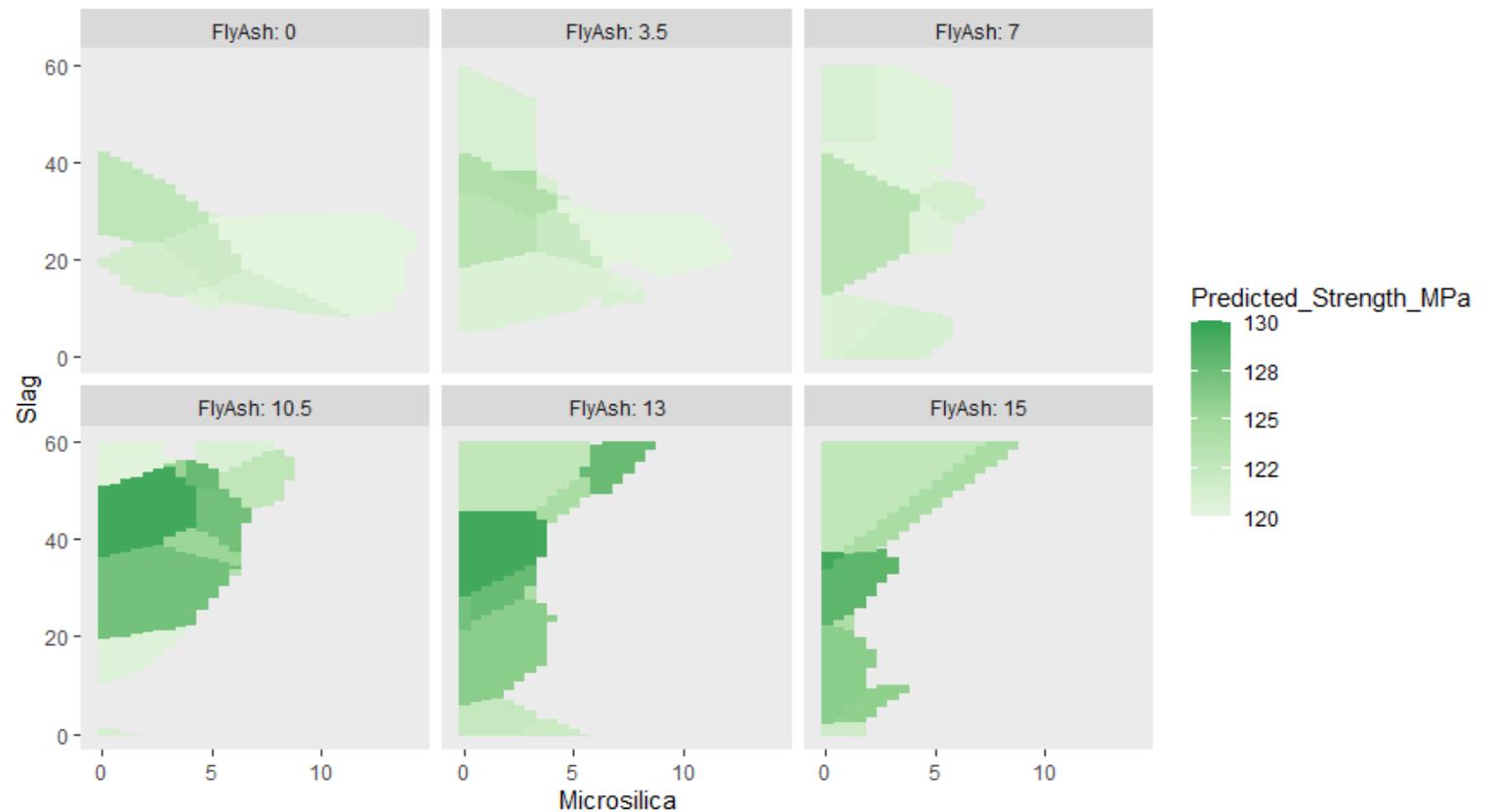
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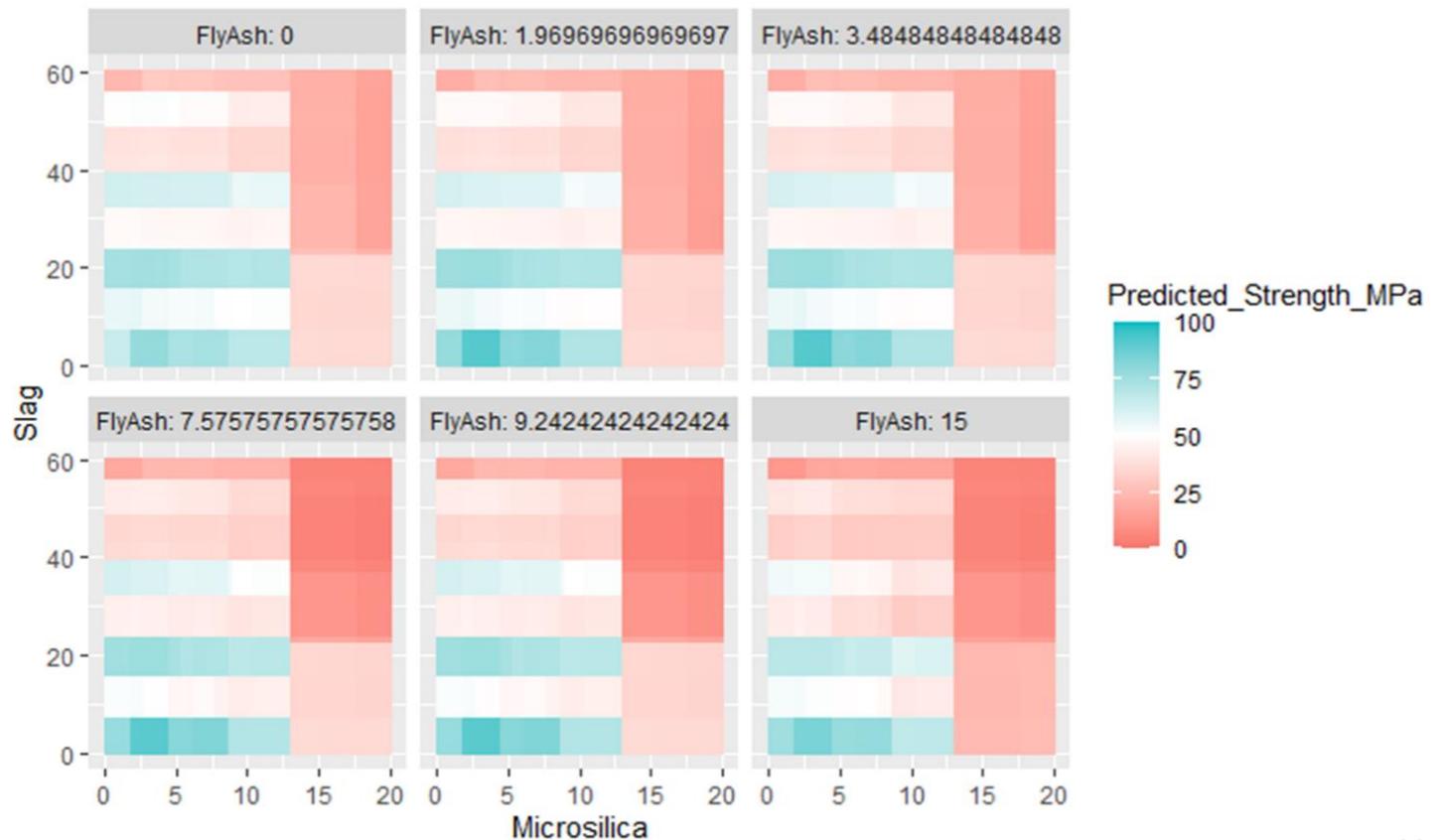
# PDD

2. Impose design limits and evaluate alternative mixtures (e.g.,  $f_c > 120$  MPa)



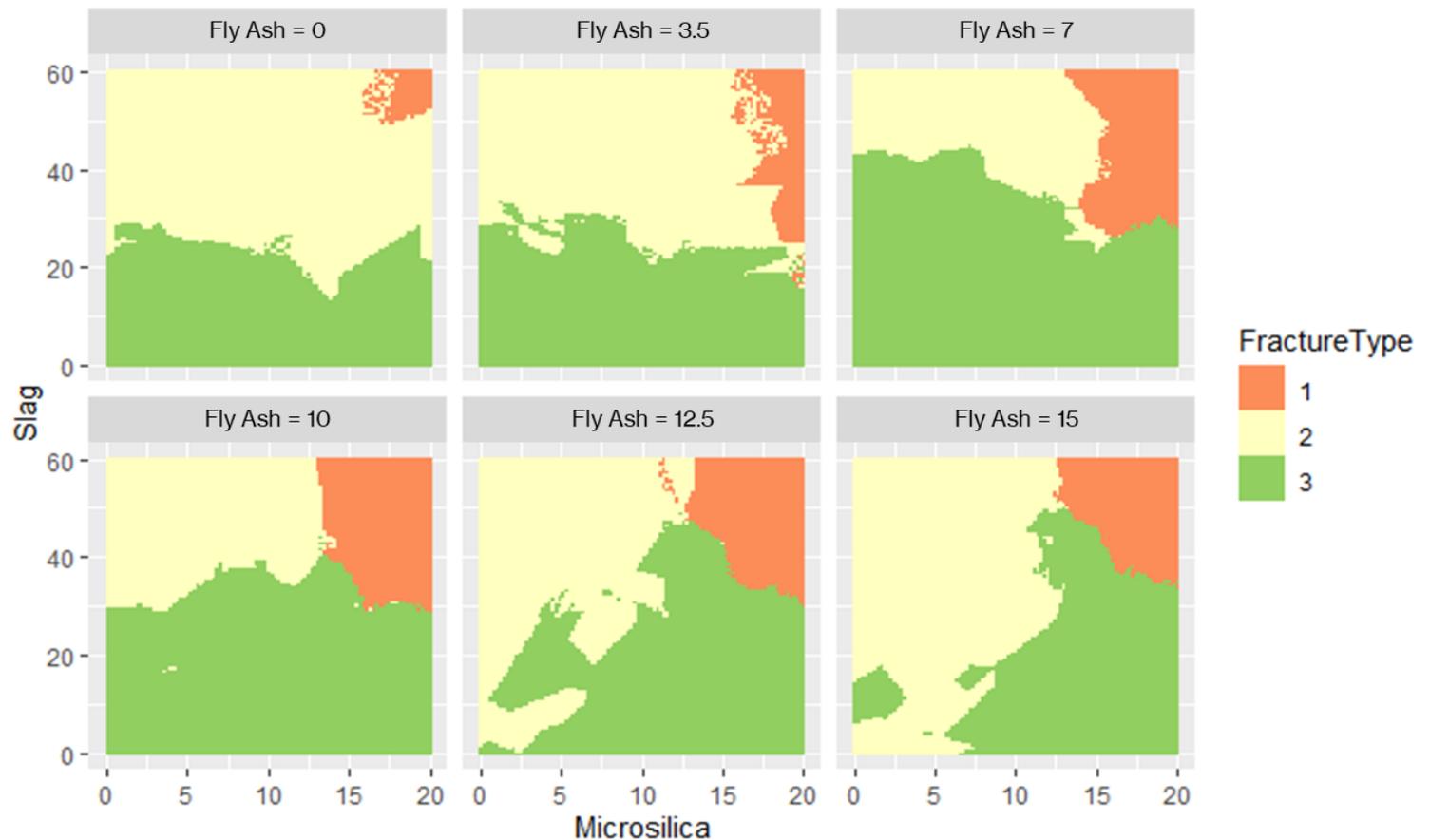
# PDD

3. Use to evaluate predictive structure of models -> detect errors



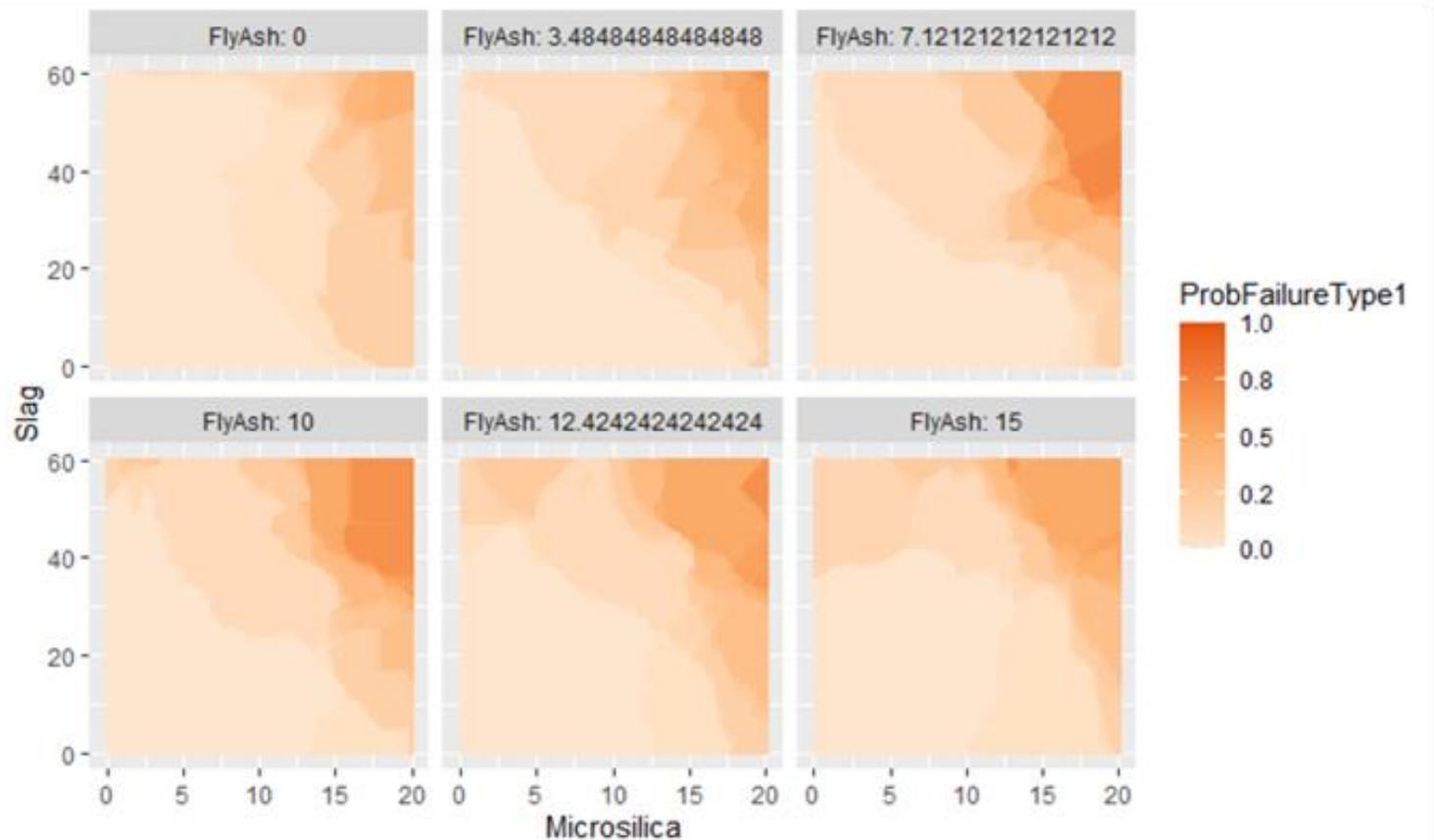
# PDD

4. Make categorical predictions -> e.g., failure models



# PDD

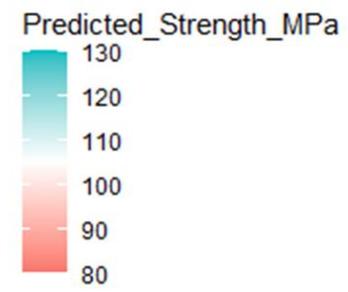
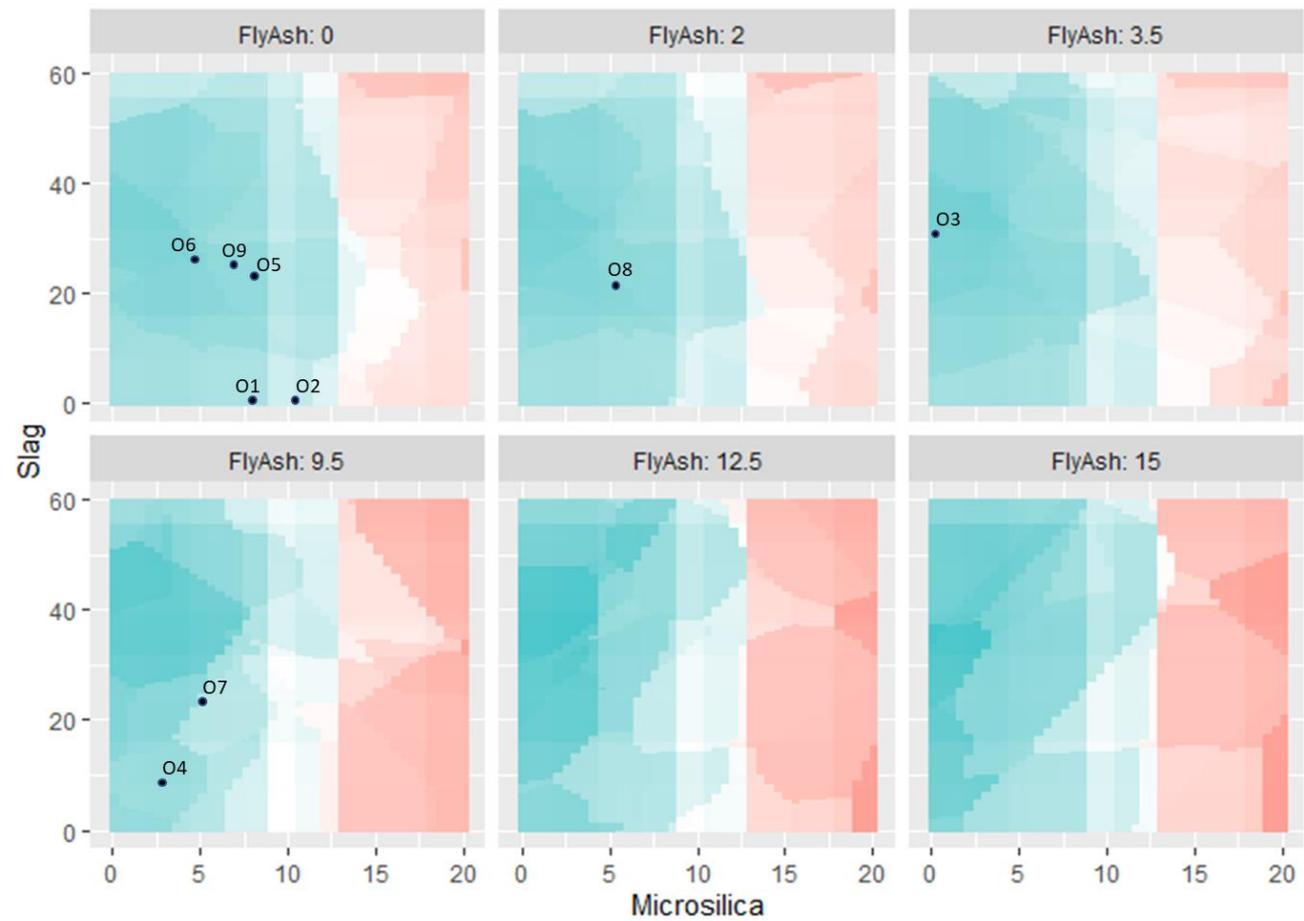
5. Evaluate probability of failure occurrences with Categorical PDDs





# Results

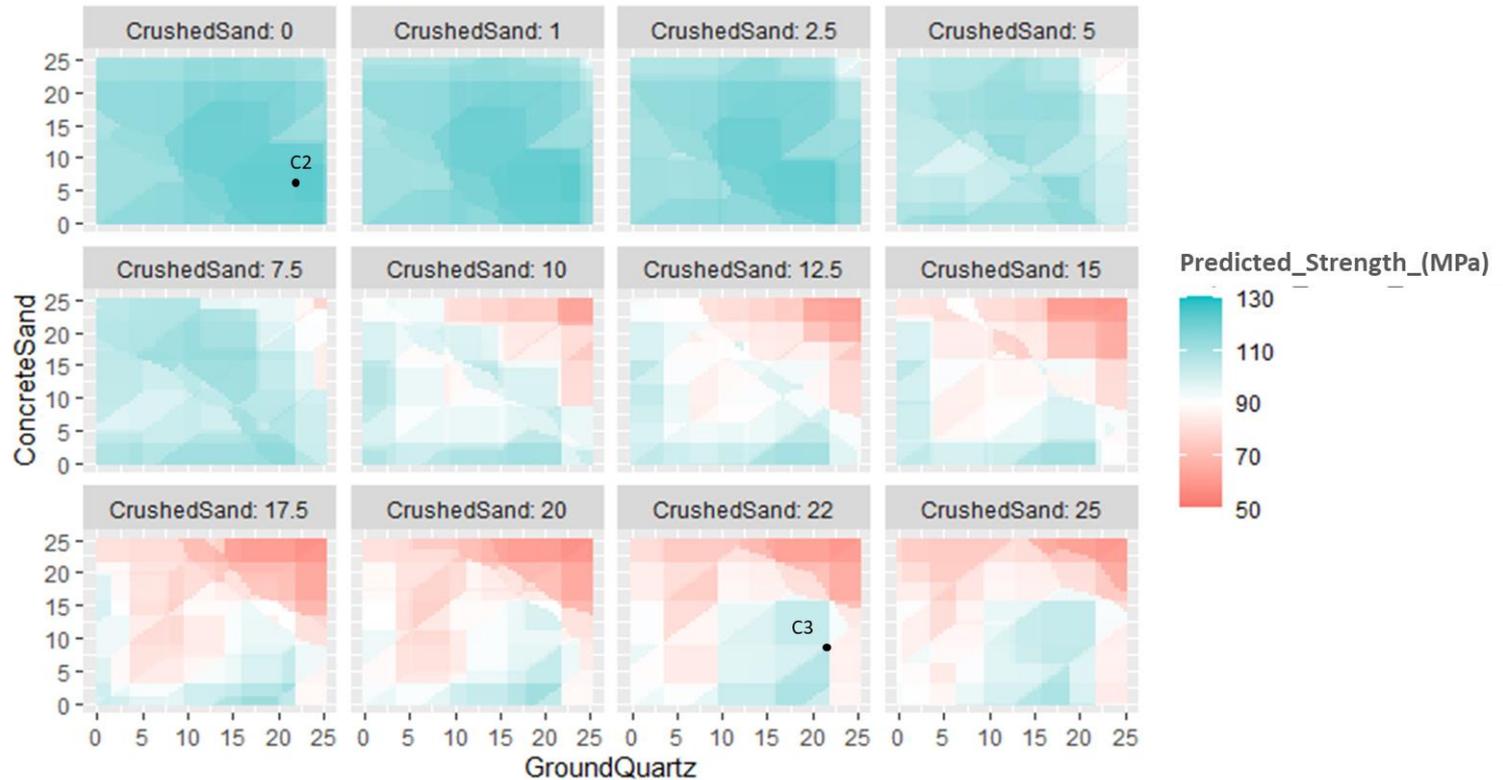
# PDD Phase A



Mixture #	SCM replacing cement (% by wt)			fc (MPa) 56 days
	Slag	Microsilica	Fly Ash	
O1	0	7.7	0	109
O2	0	10.1	0	120
O3	31.5	0.6	3.5	105
O4	8.5	2.6	9.2	114
O5	23	7.7	0	119
O6	27.9	4.6	0.5	126
O7	23	5	9.4	111
O8	22.4	5.3	2	105
O9	26	7	0	119

# PDD

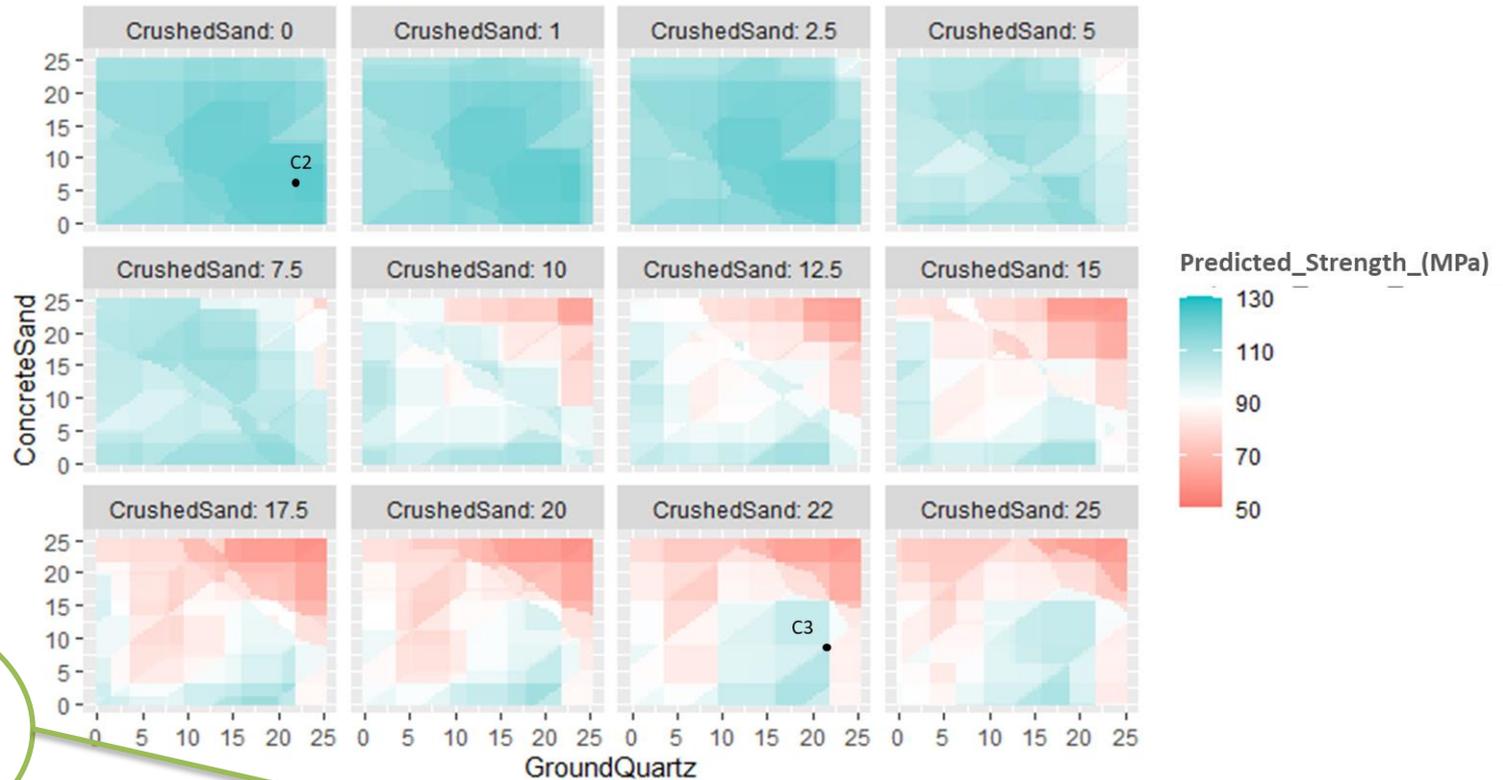
## Phase B



Mixture #	SCM replacing cement (% by wt)			Aggregates replacing cementitious (% by wt)			56 day results	
	Slag	Microsilica	Fly Ash	Ground Quartz	Concrete Sand	Crushed Sand	New test method	ASTM C1856
							f'c (MPa)	f'c (MPa)
C1	0	10.1	0	22	6.5	0	128.4	133.8
C2	22.4	5.25	1.97	22	6.5	0	129.2	158.1
C3	22.4	5.25	1.97	21.5	8.5	22	128.5	154.8

# PDD

## Phase B



**C3**  
 fc = 155 MPa  
 Fa/cm > 1

Mixture #	SCM replacing cement (% by wt)			Aggregates replacing cementitious (% by wt)			56 day results	
	Slag	Microsilica	Fly Ash	Ground Quartz	Concrete Sand	Crushed Sand	New test method	ASTM C1856
							f'c (MPa)	f'c (MPa)
C1	0	10.1	0	22	6.5	0	128.4	133.8
C2	22.4	5.25	1.97	22	6.5	0	129.2	158.1
C3	22.4	5.25	1.97	21.5	8.5	22	128.5	154.8

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# Cost and Environmental Impact

# Eco-efficiency Indices

$$^{[1]} \chi_{column} = \frac{i_c}{f_c}$$

$$^{[1],[2]} \chi_{cracking} = \lambda_{fr} \left( \frac{i_c}{f_c^{0.25}} \right)$$

$f_c$  Compressive strength (MPa)

$\lambda_{fr}$  Coefficient for modulus of rupture  $\lambda_{fr} = 1.1125e^{-0.004f_c}$

$i_c$  Volumetric environmental impact (kg CO<sub>2-eq</sub>/m<sup>3</sup>)

[1] proposed by Kourehpaz and Miller ([Kourehpaz and Miller 2019](#))

[2] proposed modification in this work

# Cost-efficiency Indices

$$\rho_{column} = \frac{u_c}{f_c}$$

$$\rho_{cracking} = \lambda_{fr} \left( \frac{u_c}{f_c^{0.25}} \right)$$

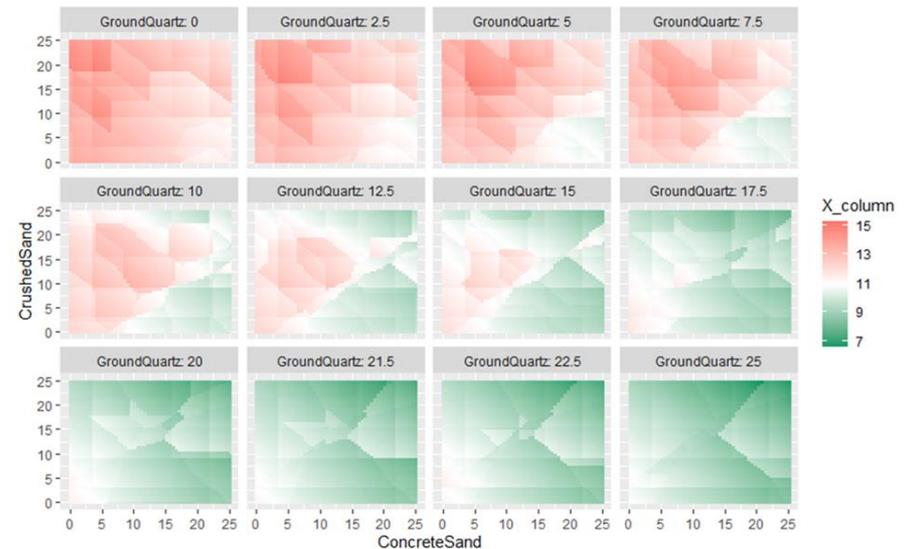
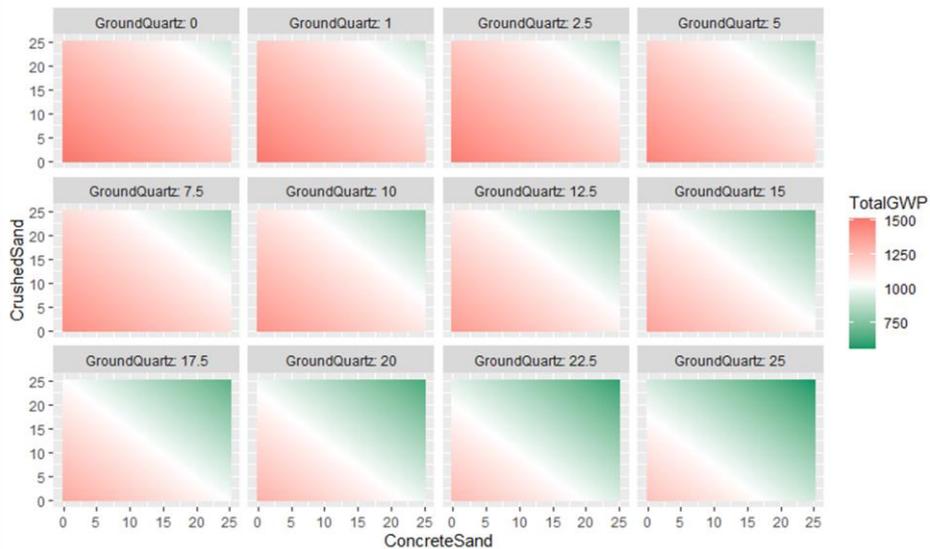
$f_c$  Compressive strength (MPa)

$\lambda_{fr}$  Coefficient for modulus of rupture

$$\lambda_{fr} = 1.1125e^{-0.004f_c}$$

$u_c$  Volumetric unit cost (\$/m<sup>3</sup>)

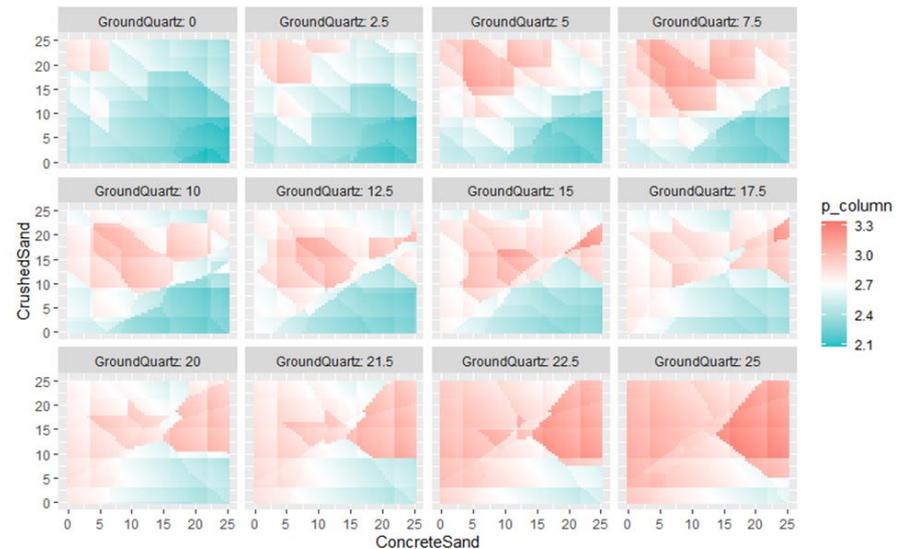
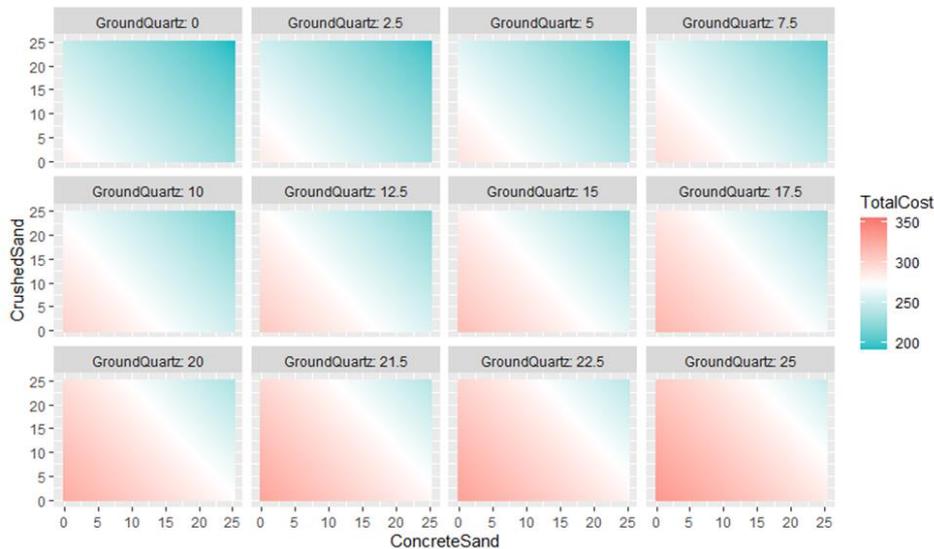
# Volumetric environmental impact vs Eco-Efficiency Density Diagrams



$$TotalGWP = i_c (ingredientA) + i_c (ingredientB) + \dots$$

(kg CO<sub>2</sub>-eq/m<sup>3</sup>)

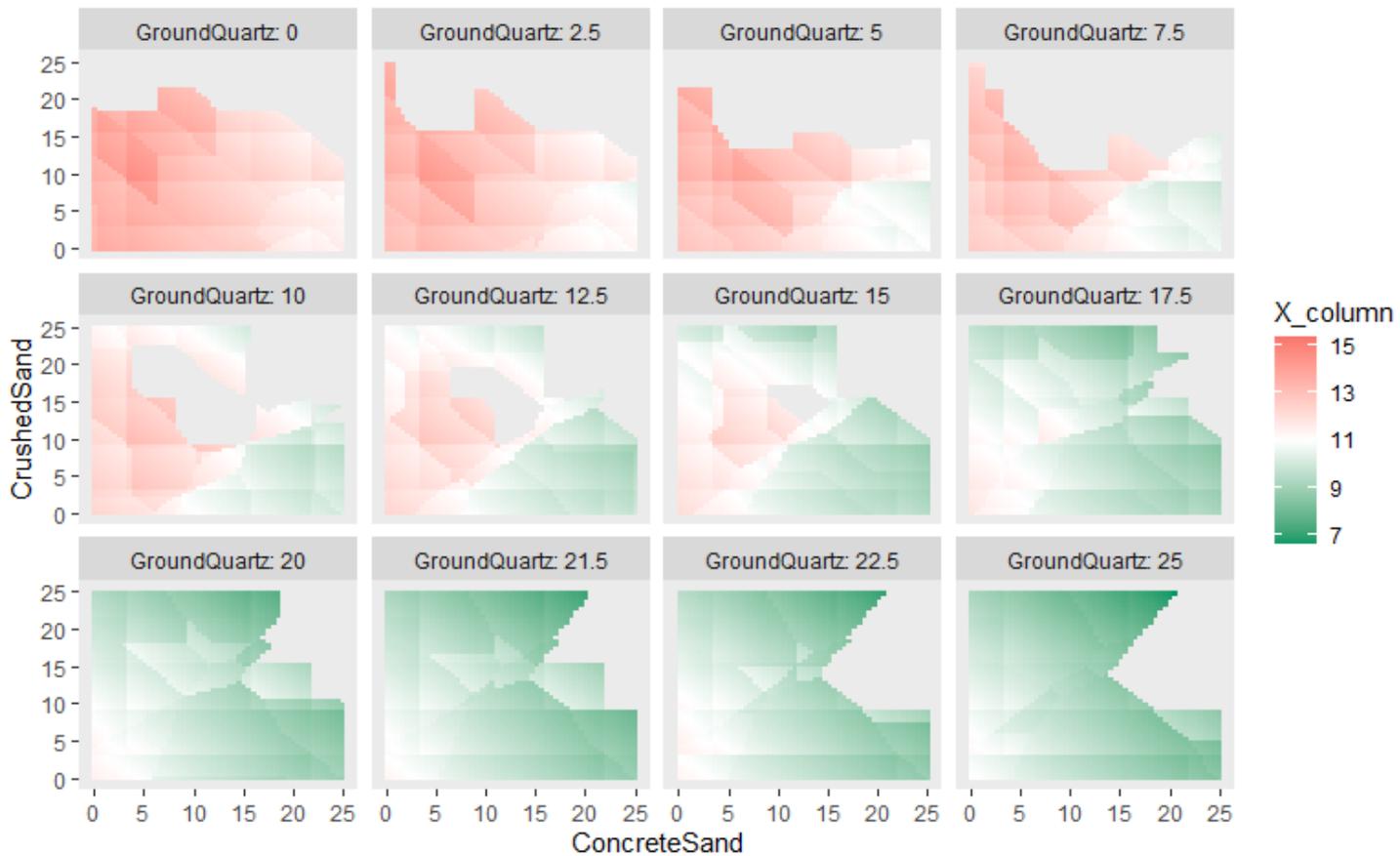
# Volumetric Unit Cost vs Cost-Efficiency Density Diagrams



# Volumetric Indicators vs Efficiency Indicators

Mix #	Description	aggregates (% by wt) replacing cementitious content			Total Cost (\$/m <sup>3</sup> )	$\rho_{\text{column}}$	fc (MPa)
		concrete sand	crushed sand	ground quartz			
p-Col-1	with min( $\rho_{\text{column}}$ )	21.5	2.5	0	233	2.08	112
p-Col-2	with min(Total Cost)	25	25	0	190	2.37	80
p-Col-3	same $\rho_{\text{column}}$ p-Col-2 & higher cost	11	2.5	11.5	279	2.37	118
p-Col-4	with lowest predicted strength	22	17.5	14	240	3.21	74.8
p-Col-5	with highest predicted strength	9.5	0	19	303	2.56	118
					Total GWP (kg CO <sub>2</sub> -eq/m <sup>3</sup> )	$\chi_{\text{column}}$	fc (MPa)
$\chi$ -Col-1	with min( $\chi_{\text{column}}$ )	20.5	25	25	625	6.58	95
$\chi$ -Col-2	with min(Total GWP)	25	25	25	552	6.75	82
$\chi$ -Col-3	same $\chi_{\text{column}}$ as $\chi$ -Col-2 & higher GWP	19.5	25	25	641	6.75	95
$\chi$ -Col-4	with lowest predicted strength	22	17.5	14	875	11.70	74.8
$\chi$ -Col-5	with highest predicted strength	9.5	0	19	1197	10.10	118

# Filtered Eco-Efficiency Density Diagrams

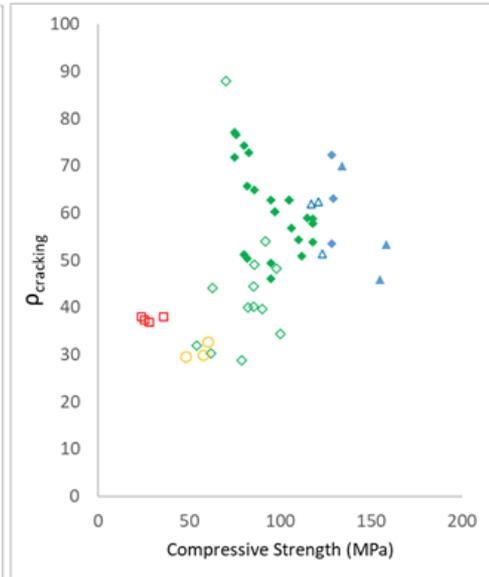
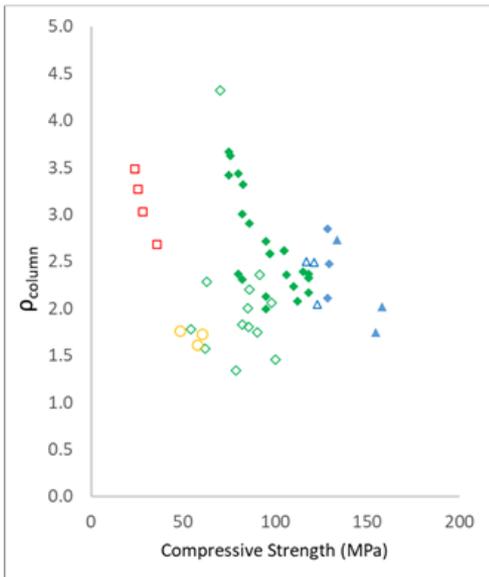
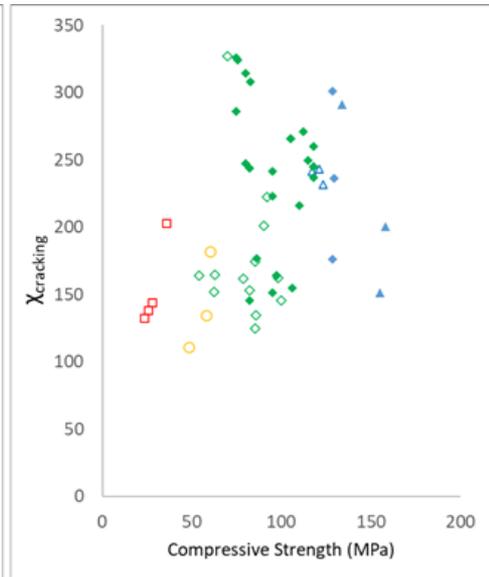
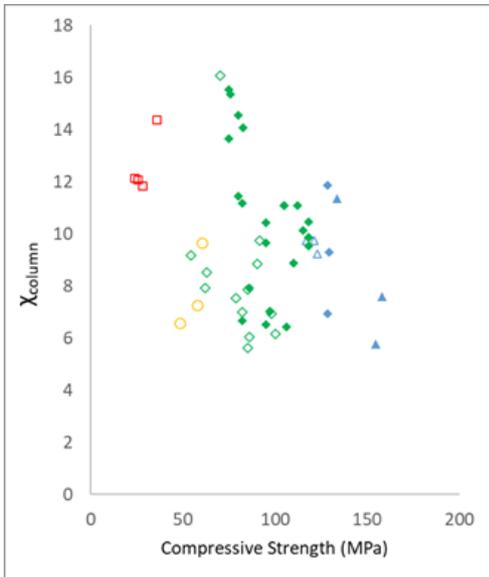


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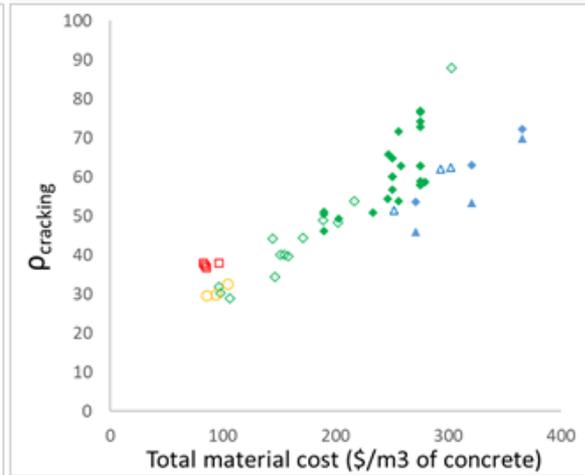
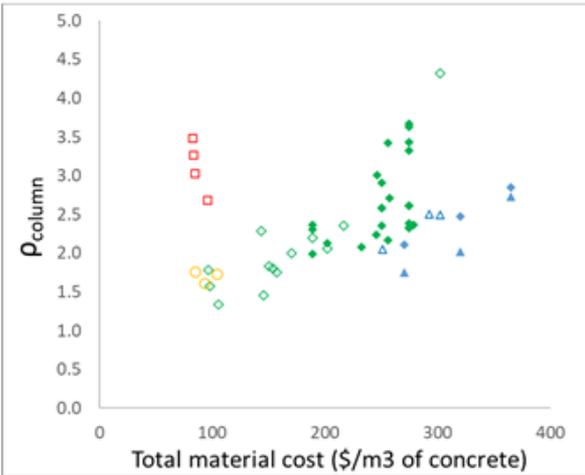
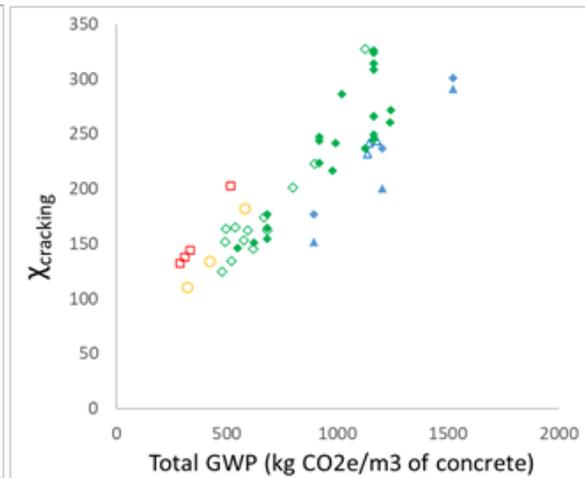
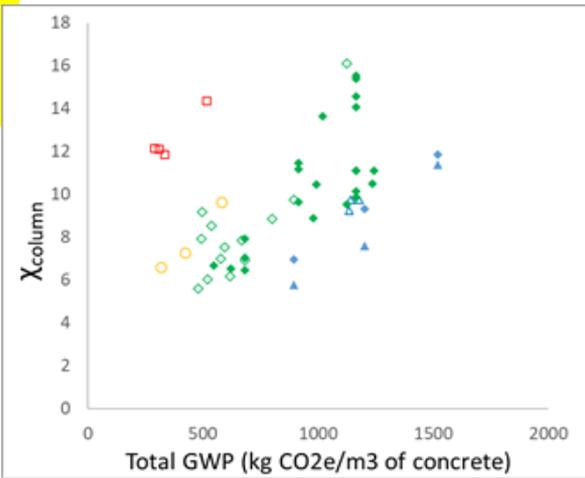
- ✓ 1. Can we accurately estimate the compressive strength of UHPC with reduced experimental runs & ML models? -> **YES**
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- ✓ 3. Can we evaluate the effect of mix proportioning & mechanical performance on cost and eco-efficiency concurrently? -> **YES**
4. Are high paste content, high strength (and ultra-high strength) concrete technologies detrimental to cost and/or eco efficiencies?



# COMPARISON BETWEEN DIFFERENT CONCRETE TECHNOLOGIES



- ◆ HPC and UHPC mixtures from Sections 6.6 and 7.2 (Tables 7, 8, 9 and 10)
- ◇ HSCs mixtures from the literature
- SCC mixtures from the literature
- Traditional concrete mixtures from the literature
- UHPC mixtures from Section 5.2 (Fig.16) following new test protocol
- ▲ UHPC mixtures from Section 5.2 (Fig.16) following ASTM C1856
- ▲ UHPC mixtures from the literature



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# CONCLUSIONS

- ✓ 1. Can we accurately estimate the compressive strength of UHPC with reduced experimental runs & ML models? -> **YES (OA+ML)**
- ✓ 2. Can we evaluate the effect of changes in mix proportioning on mechanical performance in an easy and intuitive way? -> **YES (PDD)**
- ✓ 3. Can we evaluate the effect of mix proportioning & mechanical performance on cost and eco-efficiency concurrently? -> **YES (CEDD & EEDD)**
- ✓ 4. Are high paste content, high strength (and ultra-high strength) concrete technologies detrimental to cost and/or eco efficiencies? -> **NO**



# IMPLICATIONS

# Implications

- This study provides guidance -> develop EEDDs -> proof of optimization -> EPDs
- Facilitate decision making (material availability, cost, accessibility, embodied CO2)
- Facilitate communication between non-expert personnel (in AI and materials) involved in projects (owners, policy makers, designers, architects and producers)
- Lift mis-conceptual barriers on UHPC -> promote application where suitable
- Encourage innovative mix designs with new materials (e.g., nanomaterials)

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# FUTURE WORK

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- New indices -> CO2 of reinforcing steel on eco-efficiency
- New indices -> difference in span achieved in bridge elements (beams, girders) for different concretes -> weight of the superstructure -> number and volume of supporting substructural elements (columns, footing and piles)
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- Further improvement of the end-specimen conditions -> strengths over 125 MPa
- New indices -> CO2 of reinforcing steel on eco-efficiency
- New indices -> difference in span achieved in bridge elements (beams, girders) for different concretes -> weight of the superstructure -> number and volume of supporting substructural elements (columns, footing and piles)
- PDDs to optimize material properties other than compressive strength should be explored (e.g., fiber reinforced concretes)

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- New models -> inputs related to individual particle make-up (fineness, characteristic particle size and compound composition of the raw ingredients) -> potential to overcome the multi-source variability issue
- Inclusion of nanomaterials & fibers should be evaluated through standard test protocols -> compare UHPCs w/ much higher strengths vs other concretes

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# Upcoming Publications

- C. Tavares, *Multi-Objective Density Diagrams Developed with Machine Learning Models to Optimize Sustainability and Cost-Efficiency of UHPC Mix Design*, Ph.D. dissertation, Texas A&M University (May 2022)
- C. Tavares, X. Wang, S. Saha, Z. Grasley, *Machine Learning-Based Mix Design Tools to Minimize Carbon Footprint and Cost of UHPC. Part 1: Efficient Data Collection and Modeling* (under review 2022)
- C. Tavares and Z. Grasley, *Machine Learning-Based Mix Design Tools to Minimize Carbon Footprint and Cost of UHPC. Part 2: Cost- and Eco-Efficiency Density Diagrams* (under review 2022)

# References

Kourehpaz, Pouria, and Sabbie A. Miller. 2019. 'Eco-efficient design indices for reinforced concrete members', *Materials and Structures*, 52: 96.



**THANK YOU!**

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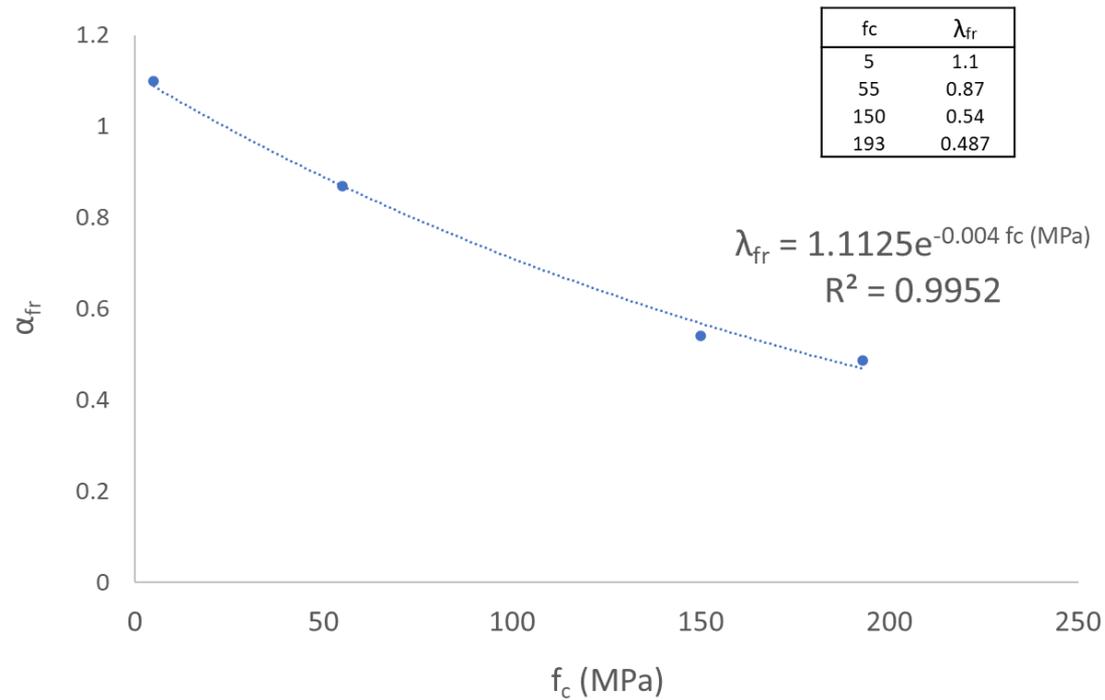
phone: (832)819-9856

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# APPENDIX

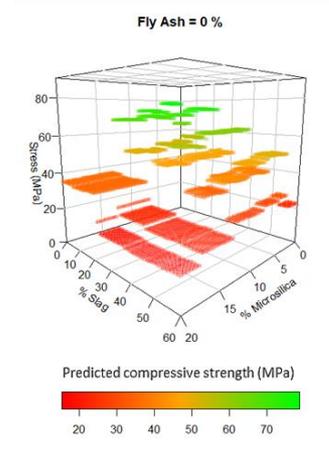
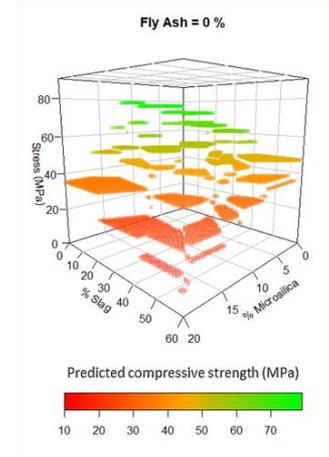
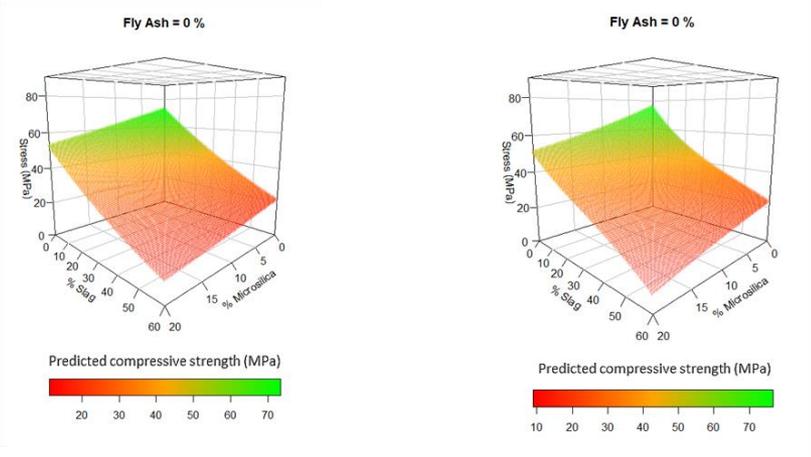


$$f_r = 0.62\sqrt{f_c \text{ (MPa)}}$$

$$f_r = 0.94\sqrt{f_c \text{ (MPa)}}$$

$$f_r = 2.55\sqrt{f_c \text{ (MPa)}}$$

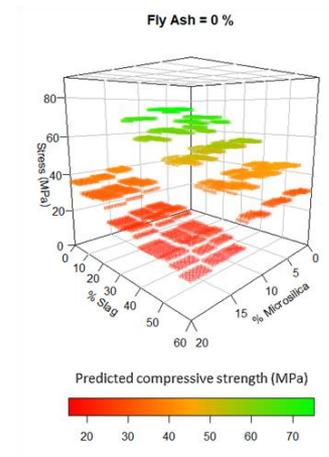
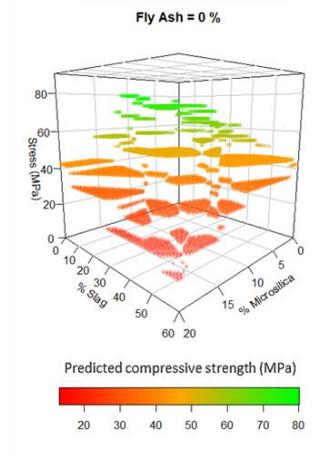
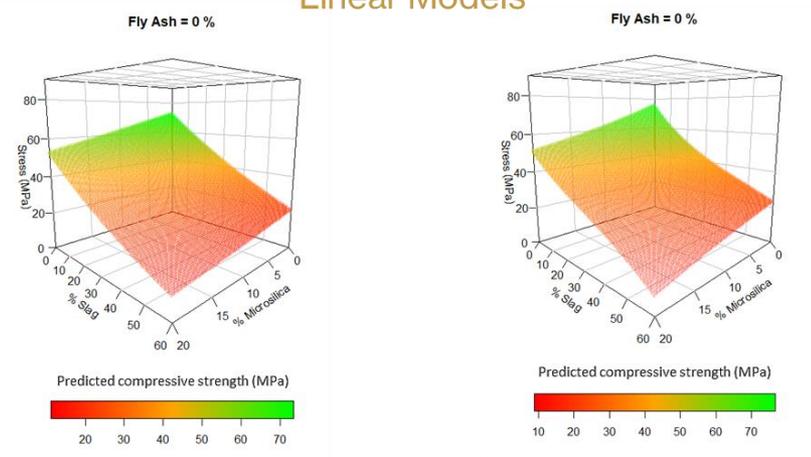
# 3D density plots -> predictive structure



## Linear Models

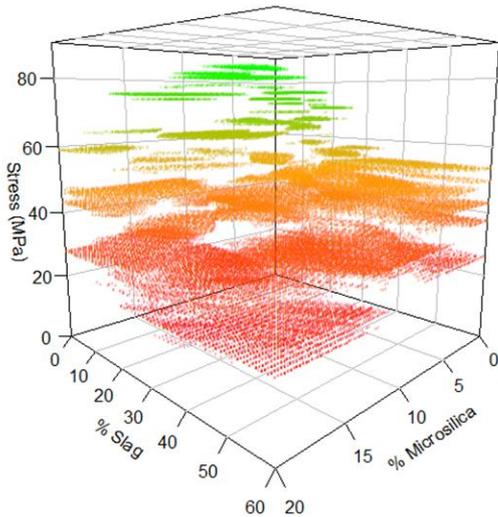
## kNN Models

## RF Models



# Modeling

Fly Ash = 3.5 %



Predicted compressive strength (MPa)

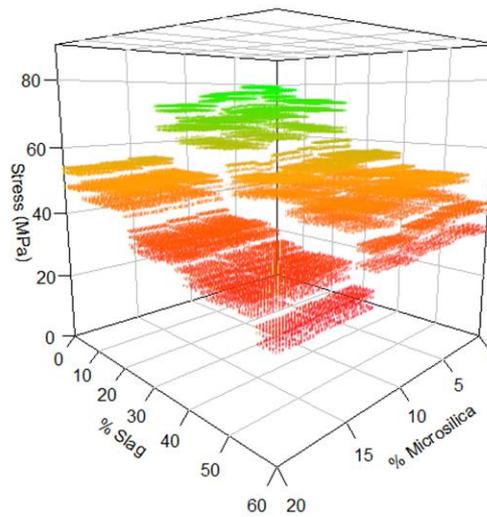


20 30 40 50 60 70 80

kNN Model

+

Fly Ash = 3.5 %



Predicted compressive strength (MPa)

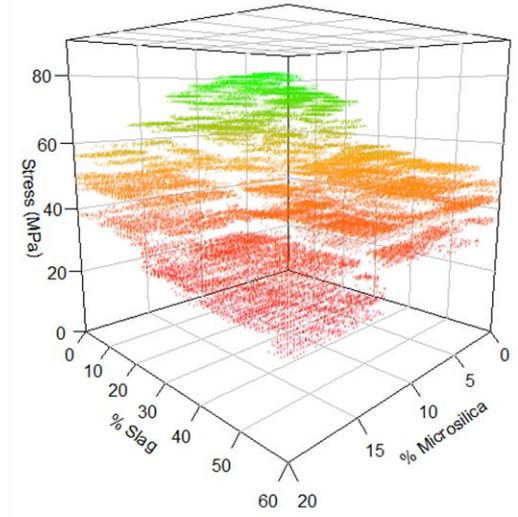


30 40 50 60 70

RF Model

=

Fly Ash = 3.5 %



Predicted compressive strength (MPa)



30 40 50 60 70 80

Ensemble Model

# Modeling

Evaluating predictive performance of models:

- 3D density plots
- **RMSE**
- ***Correlation plots (predictions vs actual outcomes)***

**$R^2$  is only applicable to evaluate linear regression\***

*\*Spiess and Neumeyer, An evaluation of  $R^2$  as an inadequate measure for nonlinear models in pharmacological and biochemical research: a Monte Carlo approach*

# Eco-efficiency Indices

$$\sigma = \frac{M^*c}{I_x} \quad \text{---} \rightarrow \quad fr = \frac{6M}{bh^2}$$



$$\underbrace{M_c = \frac{f_r b h^2}{6} \quad \text{vs} \quad M_{\max} = \frac{w l^2}{8}}_{}$$

$$h = 0.866 \frac{w^{0.5} l}{b^{0.5} f_r^{0.5}}$$

# Eco-efficiency Indices

$$h = 0.866 \frac{w^{0.5} l}{b^{0.5} f_r^{0.5}} \quad \dashrightarrow \quad \tilde{I} = l(bh - A_s)i_c + lA_s i_s$$

ACI 318 building code (NSC):  $f_c < 55\text{MPa}$

ACI 363 (HSC):  $f_c > 55\text{MPa}$

ACI 239 (UHPC):  $f_c > 150\text{ MPa}$

$$f_r = 0.62\sqrt{f_c(\text{MPa})}$$

$$f_r = 0.94\sqrt{f_c(\text{MPa})}$$

$$f_r = 2.55\sqrt{f_c(\text{MPa})}$$

$$\lambda_{fr} = 1.1125e^{-0.004f_c}$$

$$\tilde{I} = l^2 (wb)^{0.5} \lambda_{fr} \left( \frac{i_c}{f_c^{0.25}} \right) - lA_s i_c + lA_s i_s$$

# Eco-efficiency Indices

$$\tilde{I} = l^2 (wb)^{0.5} \lambda_{fr} \left( \frac{i_c}{f_c^{0.25}} \right) - lA_s i_c + lA_s i_s$$

$$\chi_{cracking} = \lambda_{fr} \left( \frac{i_c}{f_c^{0.25}} \right)$$