



## Approaches for Teaching Shear Analysis and Design of Reinforced Concrete

Matthew D. Lovell, Royce W. Floyd, Benjamin Z. Dymond,  
Kenneth C. Hover



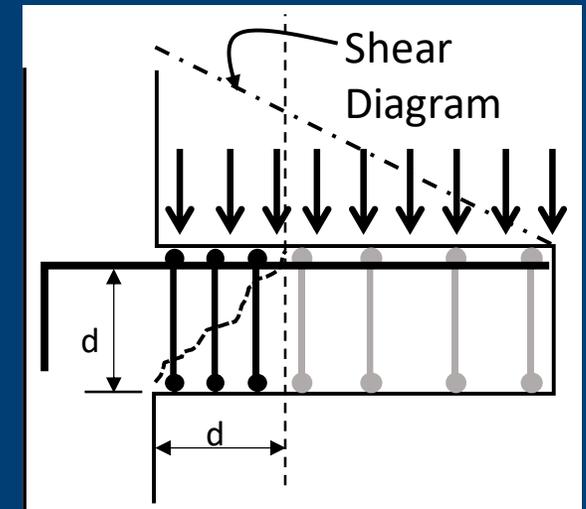
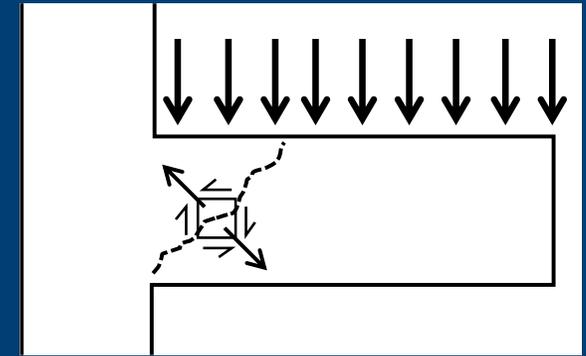
# Introduction

- Not just content, but how is it delivered?
  - Address different learning styles
  - Instructors often have little pedagogical training
  - Instructors tend to emulate their experiences
- This presentation is focused on an introductory Concrete Design course



# Technical Content

- Shear behavior based on combined flexural, axial, and shear stresses
- Rapid and brittle failure
  - $\phi = 0.75$  (ACI 318-19 21.2.1)
  - Diagonal tension failure
  - Cracks at  $45^\circ$  for non-prestressed
- Overall philosophy
  - Estimate cracking
  - Cross cracks with stirrups



# Technical Content

- Shear Design
  - $\phi V_n \geq V_u$
  - $V_n = V_c + V_s$  (ACI 22.5.1.1)
- Ultimate Shear Force ( $V_u$ )
  - Based on the shear diagram, changes along length
  - Based on force at  $d$  from the support for typical supports

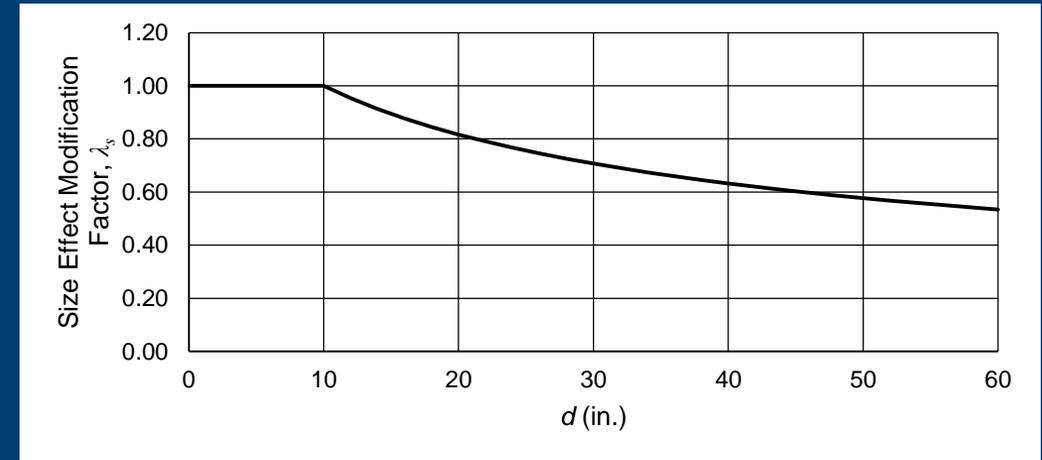
# Technical Content

- Concrete Contribution
  - Changes in 318-19
  - Size effect factor
  - Multiple equations (ACI 22.5.5.1)

For  $A_v \geq A_{v,min}$  either of

$$V_c = \left[ 2\lambda\sqrt{f'_c} + \frac{N_u}{6A_g} \right] b_w d$$

$$V_c = \left[ 8\lambda(\rho_w)^{1/3}\sqrt{f'_c} + \frac{N_u}{6A_g} \right] b_w d$$



For  $A_v < A_{v,min}$

$$V_c = \left[ 8\lambda_s\lambda(\rho_w)^{1/3}\sqrt{f'_c} + \frac{N_u}{6A_g} \right] b_w d$$

# Technical Content

- $d$  = effective depth at section considered for shear
- $b_w$  = width of rectangular beam or T-beam web
- $f'_c$  = specified 28-day compressive strength in psi
- $\lambda$  = modification factor to account for properties of lightweight concrete
- $\lambda_s = \sqrt{\frac{2}{1 + \frac{d}{10}}} \leq 1$
- $\rho_w = \frac{A_s}{b_w d}$

# Technical Content

- Steel Contribution

- Stirrups typically installed vertically

- $V_s = \frac{A_v f_{yt} d}{s}$  (ACI 22.5.10.5)

- Determining required stirrups

- $V_u \leq \phi [V_c + V_s] = \phi 2\lambda \sqrt{f'_c} b_w d + \phi \frac{A_v f_{yt} d}{s}$

- $s(x) \leq \frac{\phi A_v f_{yt} d}{V_u(x) - \phi V_c}$

- Often stepwise approach

- Must consider minimum steel and maximum spacing



# Active Learning Strategies

- Based on experience at four different universities

Shear Topic	RHIT	OU	UMD	Cornell
Shear Stresses in an Uncracked Elastic Beam	MC, NA	MC, NA	LC, NA	MC, A
Crack Initiation and Propagation (i.e. Mohr's circle, crack patterns)	MC, A	HC, A	MC, A	MC, A
Concrete Contribution to Shear Strength, $V_c$	HC, A	HC, A	HC, A	HC, A
Steel Contribution to Shear Strength, $V_s$	HC, A	HC, A	HC, A	HC, A
Shear Analysis of Reinforced Concrete Beams	HC, A	HC, A	HC, A	HC, A
Shear Design of Reinforced Concrete Beams	HC, A	HC, A	HC, A	HC, A
Variable Spacing of Stirrups	HC, A	HC, A	MC, NA	HC, A
Min. Web Reinforcement and Max. Stirrup Spacing	MC, A	MC, A	MC, A	HC, A
Shear in Members with Axial Load	LC, NA	LC, NA	LC, NA	MC, A
Pattern Loading	LC, NA	MC, A	MC, NA	HC, A
Continuous Members	LC, NA	MC, A	NC, NA	HC, A
Two-Way Shear	NC, NA	NC, NA	NC, NA	HC, A
Other Shear Design Methods (Compression Field Theories, Shear Friction)	NC, NA	NC, NA	NC, NA	NC, NA

HC – High Coverage, MC – Moderate Coverage, LC – Light Coverage, NC – Not Covered, A – Assessed, NA – Not Assessed.



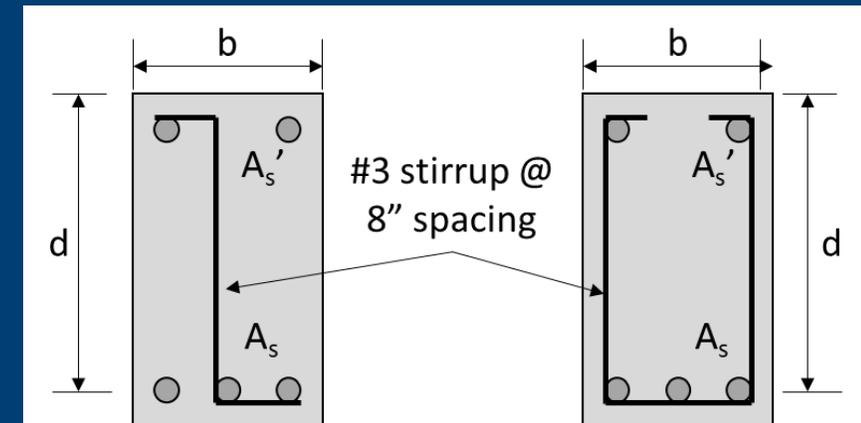
# Active Learning Strategies

- Support instruction and content delivery
- Selected to match objectives and available time
- Engagement, reflection, and retention
- Promote a variety of learning styles
- Promote higher order thinking



# Think-Pair-Share (engagement, retention, reflection)

- Preparation time: 5-10 minutes
- Activity time: < 5 minutes
- Examples
  - Area of shear reinforcement for different stirrup configurations
  - Strength reduction factor value
- Recommendations
  - Make time for each portion
  - Vary student groups



# Muddiest Point (engagement, retention, reflection)

- Preparation time: < 5 minutes
- Activity time: < 5 minutes
- Help instructor know if students are struggling
- Examples
  - “Please write down a question that you have about today’s topic.”
  - “Please write down the concept from today that was the most unclear.”
- Recommendations
  - Collect student responses and address at next class
  - Use for difficult topics like variable spacing and maximum  $V_u$

# Variations (engagement, retention, reflection)

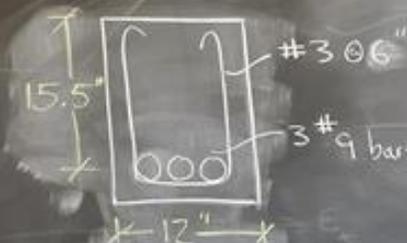
- Preparation time: < 5 minutes
- Activity time: < 5 minutes
- Examples
  - “How would this problem change if the following given information were altered?”
  - “How would changing from a uniform loading to single point load affect the maximum  $V_u$ ?”
- Recommendations
  - Helps students think critically about problem approach
  - Good for addressing common mistakes



# Variations (engagement, retention, reflection)

Example

Find:  $\phi V_n$   
Given:



$V_c = 2.2 \sqrt{f'_c} b_w d$   
 $= 2(1.0) \sqrt{4000 \text{ psi}} (12") (15.5")$   
 $= 23527 \text{ lbf}$

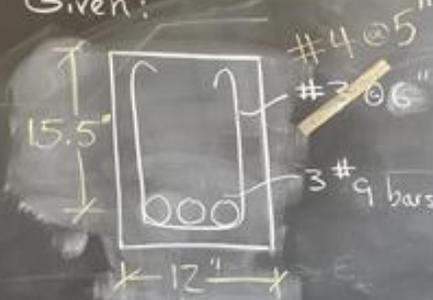
$V_s = \frac{A_v f_y d}{s}$   
 $= \frac{2(0.11 \text{ in}^2) (60 \text{ ksi}) (15.5")}{6"} = 34100 \text{ lbf}$

$\phi V_n = 0.75 (V_c + V_s)$   
 $= \underline{\underline{43.7 \text{ kips}}}$

$f'_c = 4000 \text{ psi}$   
 $f_y = 60,000 \text{ psi}$

Example

Find:  $\phi V_n$   
Given:



$V_c = 2.2 \sqrt{f'_c} b_w d$   
 $= 2(1.0) \sqrt{4000 \text{ psi}} (12") (15.5")$   
 $= 23527 \text{ lbf}$

$V_s = \frac{A_v f_y d}{s}$   
 $= \frac{2(0.11 \text{ in}^2) (60 \text{ ksi}) (15.5")}{6"} = 34100 \text{ lbf}$

$\phi V_n = 0.75 (V_c + V_s)$   
 $= \underline{\underline{43.7 \text{ kips}}}$

$f'_c = 4000 \text{ psi}$   
 $f_y = 60,000 \text{ psi}$

# Skeleton Notes (variety of learning styles)

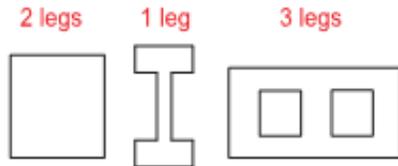
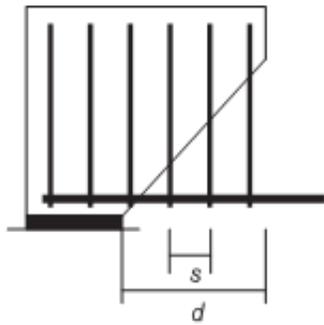
- Preparation time: > 60 minutes per lesson the first time
- Activity time: 15 – 50 minutes
- Description
  - Notes without key concepts or problem solutions distributed before class
  - Faculty member fills in during class
  - Helps students be organized and listen more
- Recommendations
  - Focus on providing items not critical for students to physically write
  - Critical content should be left blank



# Skeleton Notes (variety of learning styles)

## Shear in ACI

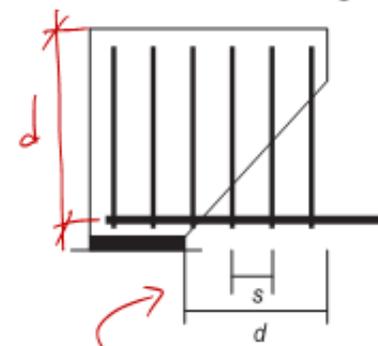
### 2. Shear Strength Provided by Steel



## Shear in ACI

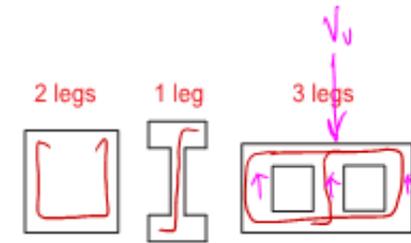
### 2. Shear Strength Provided by Steel

(ACI 22.5.10.5.3)



$$V_s = A_v f_y \left( \frac{d}{s} \right)$$

$$A_v = A_{LEG} (\# LEGS)$$

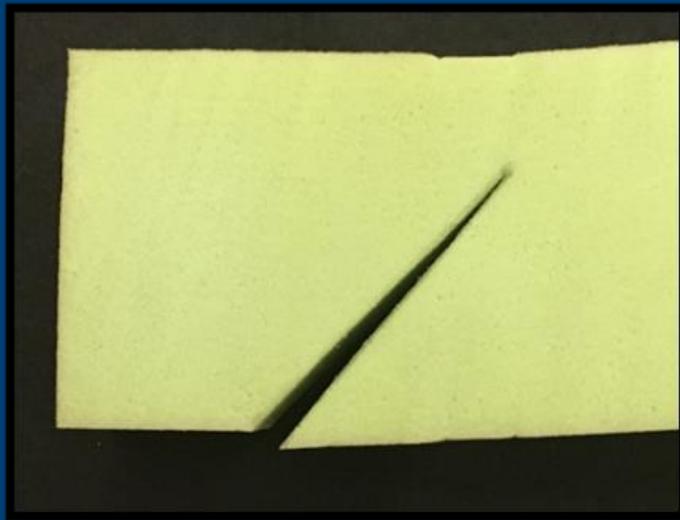


# Physical Artifacts/Demonstrations (variety of learning styles)

- Preparation time: 30 – 60 minutes
- Activity time: 15 – 30 minutes
- Description
  - Provides a tangible connection to the material
  - Multiple possibilities for shear behavior and design
- Recommendations
  - Great way to introduce new concepts and topics
  - Try to get students involved (may need multiple models)
  - Poll students to see what they wish they had seen

# Physical Artifacts/Demonstrations (variety of learning styles)

- Shear Reinforcement
  - Foam prism and masking tape
  - Can be qualitative or quantitative



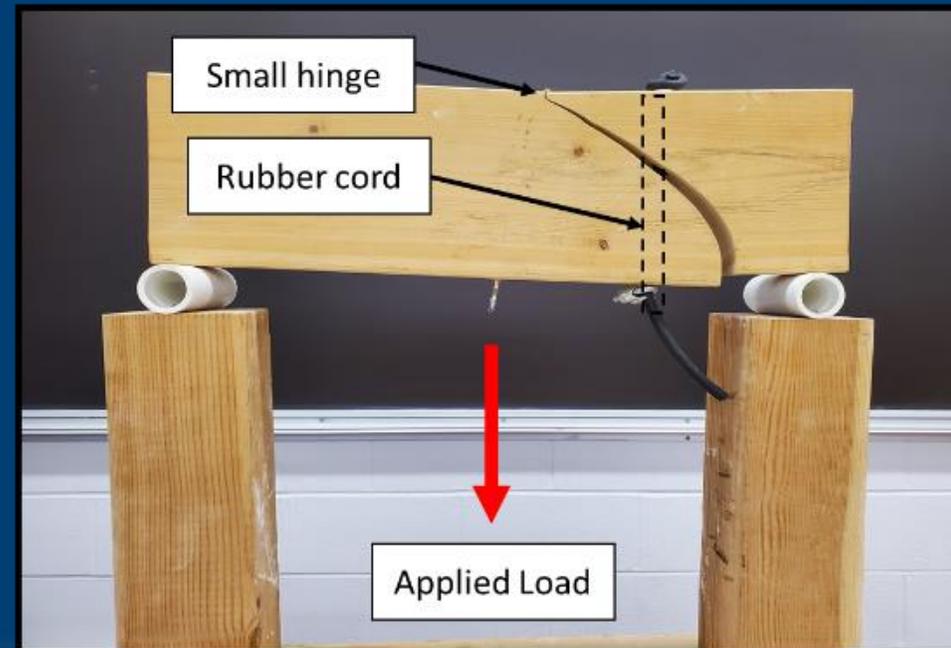
(a)



(b)

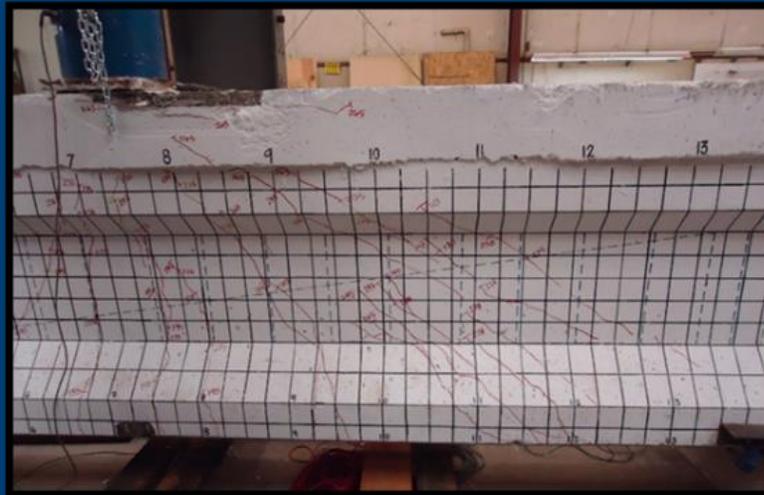
# Physical Artifacts/Demonstrations (variety of learning styles)

- Shear Reinforcement,  $V_{s,max}$ 
  - 2 x 6 with rubber hose
  - Visualization of excessive strain in the reinforcement



# Physical Artifacts/Demonstrations (variety of learning styles)

- Cracking behavior
  - Photos or videos are easy to prepare
  - Can provide a connection to active research



(a)



(b)

# Physical Artifacts/Demonstrations (variety of learning styles)

- Punching Shear
  - Foam padding or Styrofoam



# Experiential Learning (variety of learning styles)

- Preparation time: widely variable
- Activity time: 20 minutes to several class meetings
- Description
  - Students participate in construction and/or testing of physical specimens
  - Laboratory sections often included with design courses
- Recommendations
  - Laboratory activities require significant time, funds, and facilities
  - Best to include in a class with a lab section
  - Can scale to available time and facilities



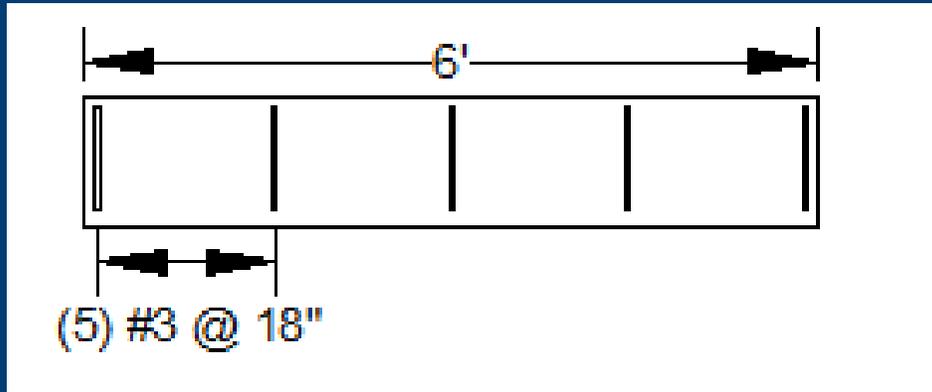
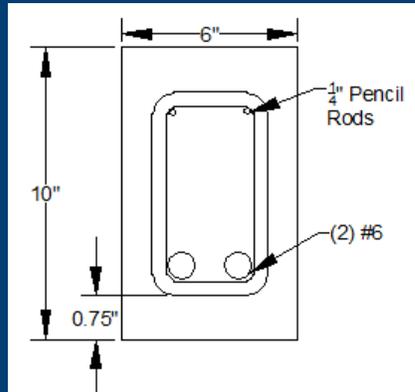
# Experiential Learning (variety of learning styles)

- Pattern loading
  - Students form the “uniformly distributed load”
  - Discuss effect of different loadings on shear forces



# Experiential Learning (variety of learning styles)

- Lab Example 1
  - Students build and test beams over two class periods
  - Minimal stirrups to show brittle failure



# Experiential Learning (variety of learning styles)

- Lab Example 2
  - Students are assigned a failure type and must design for that failure
  - Shear failure is typically spectacular and memorable

Lab Group	Failure/Behavior Type	Minimum Load	ACI 318-19 Section
Team 1	Tension Controlled	12 kips	21.2.2
Team 2	Compression Controlled	12 kips	21.2.2
Team 3	Shear	12 kips	22.5
Team 4	Bond	12 kips	25.4.2
Team 5	Doubly Reinforced	20 kips	
Team 6	T-Beam	20 kips	6.3.2

# Simulation and Computations (higher order thinking)

- Preparation time: < 30 minutes to create the assignment
- Activity time: Approx. 2 weeks for student work and instruction
- Description
  - Student built or instructor provided spreadsheet or “App”
  - Streamline the design process for consideration of alternatives
- Recommendations
  - Be aware of student skills with the proposed software
  - Can be used with other active learning strategies
  - Students can be asked to identify limitations

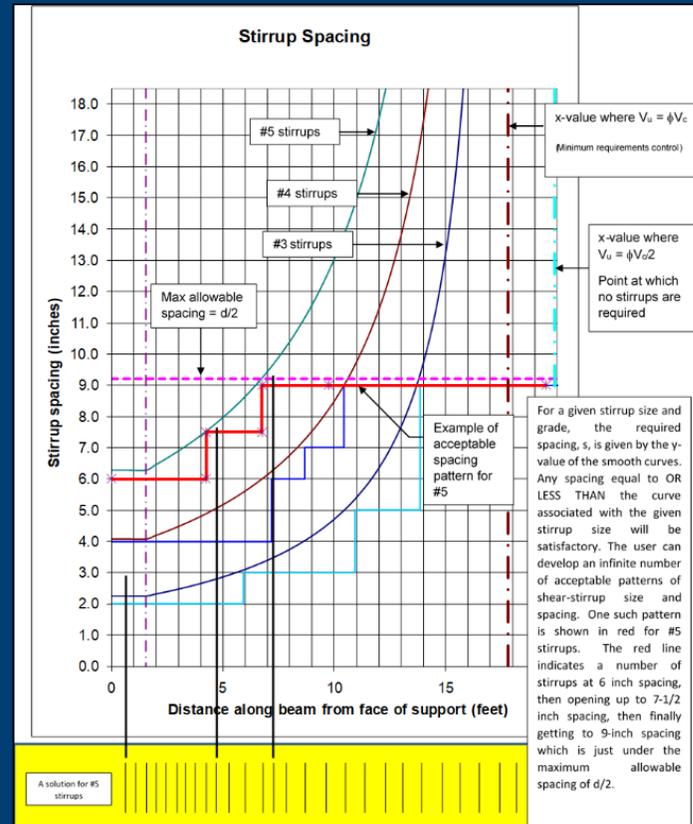


# Simulation and Computations (higher order thinking)

- Example spreadsheet for determining spacing with  $V_u(x)$

Shear Stirrup Calculator		Correction needed for new size effect factor	
Span	38 feet	bw	12 in
Ru left	110 Kips	beam depth h	21 in.
wu	8 Kips/ft	bar cover to stirrup	1.5 in.
Increment	100	flex. bar size	8 #
$f_c$	4000 psi	Stp	#3 #4 #5
$f_y$	60 ksi	d	18.6 18.4 18.3 in
$\phi V_c$		$\phi V_c$	21.1 21.0 20.8 kips
$\phi V_c/2$		$\phi V_c/2$	10.6 10.5 10.4 kips
x @ $V_u = \phi V_c$	17.8 ft	$A_s$ (in <sup>2</sup> )	#3 0.11 #4 0.2 #5 0.31
x @ $V_u = \phi V_c/2$	19.9 ft	No. legs	2 2 2
		$A_v$ (in <sup>2</sup> )	0.22 0.4 0.62
		Smax (in)	22.0 40.0 62.0
		d/2 (in)	9.2 9.2 9.2
		Control	9.2 9.2 9.2
		d=	18.6 18.4 18.3
Point	x feet	$V_u$ Kips	Stp #
0	0	102.3	3
1	0.77	102.3	3
2	1.54	102.3	3
3	1.92	100.4	3
4	2.30	98.5	3
5	2.68	96.6	3
6	3.06	94.7	3
7	3.44	92.8	3
8	3.82	90.9	3
9	4.20	89.0	3
10	4.58	87.1	3
11	4.96	85.2	3
12	5.34	83.3	3
13	5.72	81.4	3
14	6.10	79.5	3
15	6.48	77.6	3
16	6.86	75.7	3
17	7.24	73.8	3
18	7.62	71.9	3
19	8.00	70.0	3
20	8.38	68.1	3

Spreadsheet continues to compute "s" over the balance of the length of the beam



# Lessons Learned

- **Hands-on hands-down** – student comments indicate laboratory experience and physical models are particularly useful to students
- **Application before theory** – show the application first and use it to inform the theory, especially if time is limited
- **Reinforcement detailing** – students think no reinforcement is required within  $d$  from the support and general confusion about minimums and maximums
- **Know your  $b$**  – web width for shear, never flange width
- **Beware the  $\phi$  foul-up** – multiple possible mistakes by students
- **Assessment** – combine homework, open-ended projects, and exam



**THANK YOU!**

rfloyd@ou.edu



American Concrete Institute

# References

- ACI Committee 318. (2019). Building Code Requirements for Structural Concrete and COmmentary. American Concrete Institute, Farmington Hills, MI, 623 pp.
- Angelo, T. A., & Cross, K. P. (1993). Classroom assessment techniques: A handbook for college teachers. San Francisco: Jossey-Bass Publishers.
- Barkley, E. F. (2010). Student engagement techniques: A handbook for college faculty. San Francisco: Jossey-Bass Publishers.
- Behrouzi, A. (2016, June), Physical Artifacts in Introductory-level Reinforced Concrete Design Instruction Paper presented at 2016 ASEE Annual Conference & Exposition, New Orleans, Louisiana. 10.18260/p.25898
- Bolton, M. K. (1999). The role of coaching in student teams: A “just-in-time” approach to learning. Journal of Management Education, 23(3), 233–250. <https://doi.org/10.1177/105256299902300302>
- Carroll, C., & Sell, S. A., & Sabick, M. B. (2019), Introduction to Entrepreneurial-minded Learning for Faculty of Foundational STEM Courses Using the KEEN Framework Paper presented at 2019 ASEE Annual Conference & Exposition, Tampa, Florida. <https://peer.asee.org/33019>
- Cleary, D. (2006). Enhancing a reinforced concrete design course by linking theory and physical testing. ASEE Annual Conference and Exposition, 11.582.1-11.582.14.
- Dunn, R. S., & Griggs, S. A. (2000). Practical Approaches to Using Learning Styles in Higher Education. Bergin & Garvey.
- Dymond, B. Z., Swenty, M. K., & Shearer, C. R. (2020). Implementation of a laboratory experience in reinforced concrete courses. ASEE Virtual Annual Conference and Exposition, DOI: 10.18260/1-2--34770
- Dymond, B., Swenty, M., & Carroll, J. C. (2019). Comparing Exam Performance in a Reinforced Concrete Design Course with Bloom's Taxonomy Levels. Journal of Civil Engineering Education. DOI: 10.1061/(ASCE)EI.2643-9115.0000002
- Estes, A. C., Sibert, D. E., & Conley, C. H. (2002). Using a realistic hands-on laboratory program to enhance a reinforced concrete design course. ASEE Annual Conference and Exposition, 7.1247.1-7.1247.14.
- Estes, A., & Welch, R. (2005), Teaching Pedagogy 101 Paper presented at 2005 Annual Conference, Portland, Oregon. <https://peer.asee.org/15263>
- Felder, R. M., & Silverman, L. K. (1988). Learning and Teaching Styles in Engineering Education. Engineering Education, 78(7), 674-681.
- Ghanat, S., Kaklamanos, J., Ziotopoulou, K., & Selvaraj, I & Fallon, Dennis. (2016). A Multi-Institutional Study of Pre- and Post-Course Knowledge Surveys in Undergraduate Geotechnical Engineering Courses. ASEE Annual Conference and Exposition, New Orleans, LA. Paper ID:14990.



# References

- Ghanat, S. & Michalaka, D. (2017). Study of Pre- and Post-Course Knowledge Surveys in an Engineering Economy Course. ASEE Annual Conference and Exposition, Paper ID: 19197.
- Griffin, M., & Meyer, K. (2004). Reinforcing the Understanding of Reinforced Concrete in the Lab. *Concrete International*, 7, 47–50.
- Hale, M., Freyne, S., & Durham, S. (2007). Student feedback and lessons learned from adding laboratory experiences to the reinforced concrete design course. ASEE Annual Conference and Exposition, 12.1311.1-12.1311.10.
- Hmelo-Silver CE. (2004) Problem-based learning: what and how students learn. *Educ Psychol Rev* 2004;16 (3):235–66.
- Jones, C. a. (2012). Concrete Training Aids in the Classroom. Northeast Section Conference, May, 49–53.
- Kirschner, P. A., Sweller, J., and Clark, R. E. (2006). “Why Minimal Guidance During Instruction Does Not Work: An Analysis of the Failure of Constructivist, Discovery, Problem-Based, Experiential, and Inquiry-Based Teaching,” *Educational Psychologist*, 41(2), 75–86.
- Kuchma, D.; Wei, S.; Sanders, D.; Belarbi, A.; and Novak, L., 2019, “The Development of the One-Way Shear Design Provisions of ACI 318-19,” *ACI Structural Journal*, V. 116 No. 4, July, doi: 10.14359/51716739
- Kuennen, S. T., & Barrett, A. R. (2003). Construct first, design later a hands-on learning experience in reinforced concrete. ASEE Annual Conference and Exposition, 8.318.1-8.318.11.
- LaFave, J., Stojadinovic, B., Wight, & James. (1996). Lab Experiments for Reinforced Concrete Design Course. *Concrete International*, 59–62.
- Lovell, M. D., & Brophy, S. P. (2014). Transfer Effects of Challenge-Based Lessons in an Undergraduate Dynamics Course. ASEE Annual Conference and Exposition, Indianapolis, Indiana. <https://peer.asee.org/23206>
- Lovell, M., (2018). Defining and Assessing Competencies in an Undergraduate Reinforced Concrete Design Course. ASEE Annual Conference and Exposition, June 24-27, Salt Lake City, UT.
- Matsumoto, E. E. (2002). Enhancing student learning through team projects in a reinforced concrete design class. ASEE Annual Conference and Exposition, 7.511.1-7.511.26.
- Mirmiran, A. (1998). NDT and instrumentation in an undergraduate concrete lab. ASEE Annual Conference Proceedings, 1–4.
- Mosteller, F. (1989). The Muddiest Point in the lecture as a feedback device, *On Teaching and Learning*. The Journal of the Harvard-Danforth Center. Vol. 3: 10–21.



# References

- Prince, M. J., & Felder, R. M. (2006). Inductive teaching and learning methods: Definitions, comparisons, and research bases. *Journal of Engineering Education*, 95(2), 123–138. <https://doi.org/10.1002/j.2168-9830.2006.tb00884.x>
- Roberts, M. W., & Thompson, M. K. (2005). The DORC factor: Engaging students in reinforced concrete design. *ASEE Annual Conference and Exposition, Conference Proceedings*, 4745–4756.
- Roselli, R. J., & Brophy, S. P. (2006). “Effectiveness of challenge-based instruction in biomechanics,” *J. Eng. Educ.*, vol. 93, no. 4, pp. 311–324.
- Ruzycki, N.. (2015). Writing, speaking and communicating - Building disciplinary literacy in materials science undergraduate students. *ASEE Annual Conference and Exposition, Conference Proceedings*. 122.
- Schemmel, J. (1998). Practical Experience for Engineering Students. *Concrete International*, 41–44.
- Sternberg, S. P. (1997, June), Small Group, In Class Problem Solving Exercises Paper presented at 1997 Annual Conference, Milwaukee, Wisconsin. <https://peer.asee.org/6785>
- Stronge, J. H., Tucker, P. D., & Hindman, J. L. (2004). *Handbook for Qualities of Effective Teachers*. Alexandria: Association for Supervision and Curriculum Development.
- Swenty, M. K., Dymond, B. Z, Carroll, J. C. (2020). *Effective Teaching Methods in Concrete Education*. American Concrete Institute, ACI Special Publication, SPXXX-1. Chicago, IL.
- Totman, C. A., & Dempsey, J. P. (2003). Design of concrete fracture experiments. *ASEE Annual Conference and Exposition*, 8.375.1-8.375.8.
- Wankat, P. C. (2002). *The Effective Efficient Professor: Teaching, Scholarship, and Service*. Allyn & Bacon, A Pearson Education Company, Boston, MA. pg. 68.
- White, J, K. (2016). *Reinforced Concrete: Mechanics and Design, Seventh Edition*. Pearson Education, Inc. Hoboken, New Jersey, pg. 287-291.

