



American Concrete Institute®  
Advancing concrete knowledge

# Concrete Columns in High-Rise Buildings

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John Hochwalt, PE, SE  
KPF Consulting Engineers, Seattle, WA

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## DEFORMATION COMPATIBILITY OF COLUMNS IN HIGH RISE BUILDINGS

A Designer's Perspective

John M. Hochwalt, PE, SE  
KPF Consulting Engineers, Seattle, Washington

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### OVERVIEW

- Project Description
- Designer's Perspective
- Deformation Compatibility – ACI 318-11
- Conceptual Approach
- Example
- Questions

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### PROJECT DESCRIPTION

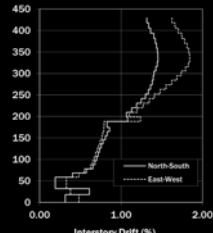
- ~40 Story Hotel and Condominium
- Seattle, Washington
- Concrete Strengths up to 9 ksi



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### PROJECT DESCRIPTION – LATERAL SYSTEM

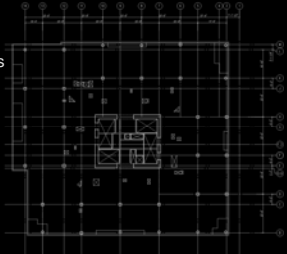
- Special Reinforced Concrete Walls
- Exceeded the IBC Height Limit
- Non-Linear Response History Analysis
- Peer Reviewed
- Flexural Yielding of Wall and Coupling Beams
- Maximum Interstory Drift 1.8%



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**PROJECT DESCRIPTION – GRAVITY SYSTEM**

- Mildly Reinforced Concrete Flat Plate
- 8" Thick, spanning 23 feet
- Deformation Compatibility of Joints

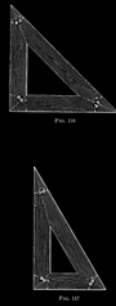


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**DESIGNER'S PERSPECTIVE**

Priorities

- Life Safety (Code compliance or equivalent)
- Owner's Interests
  - Cost
  - Schedule
  - Performance
- My Interests
  - Least effort to meet the above
  - Engineering is driven by drawings
  - Drawings are driven by construction



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**DEFORMATION COMPATIBILITY – ACI 318-11**

```

    graph TD
      A[CALCULATE FORCES?] -- YES --> B[ADEQUATE CAPACITY?]
      A -- NO --> C[MORE DETAILING ACI 21.13.4]
      B -- YES --> D[LESS DETAILING ACI 21.13.3]
      B -- NO --> C
  
```

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**DEFORMATION COMPATIBILITY – ACI 31-11**

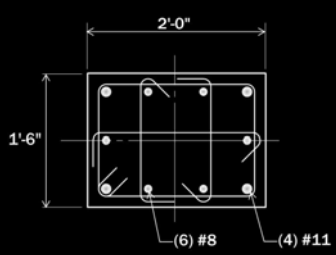
CALCULATING FORCES

ACI 21.13 Commentary

Models used to determine design displacement of buildings should be chosen to produce results that conservatively bound the values expected of the design earthquake and should include, as appropriate, effects of concrete cracking, foundation flexibility, and deformation of floor and roof diaphragms.

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**DEFORMATION COMPATIBILITY – ACI 31-11**

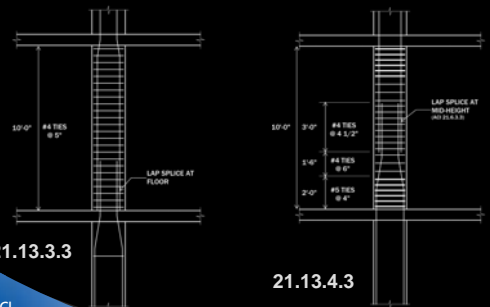


$f'_c = 8,000 \text{ psi}$

$\rho = 2.5\%$

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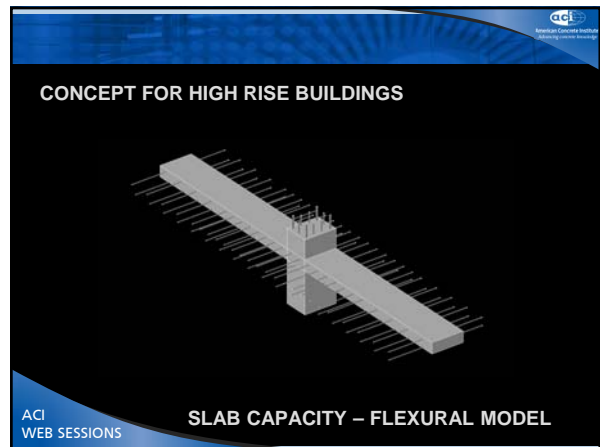
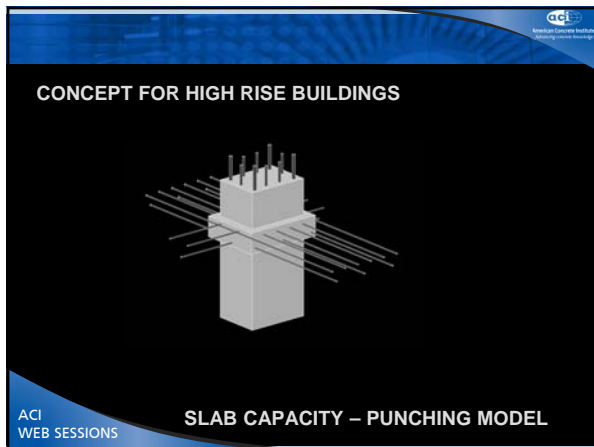
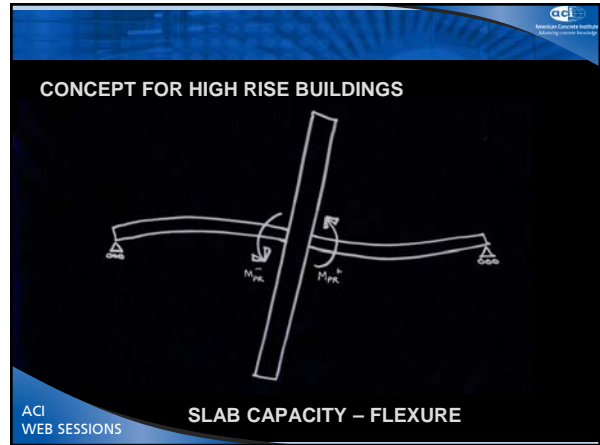
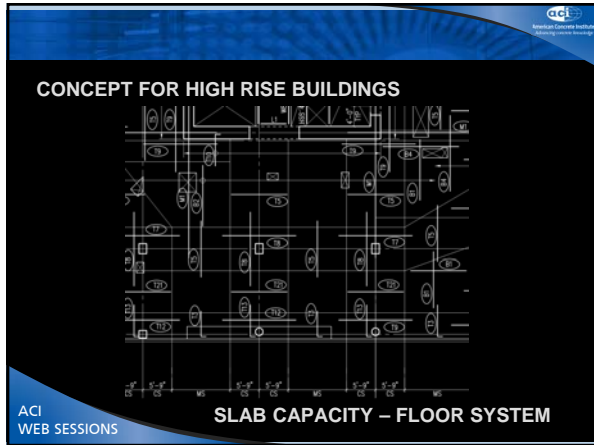
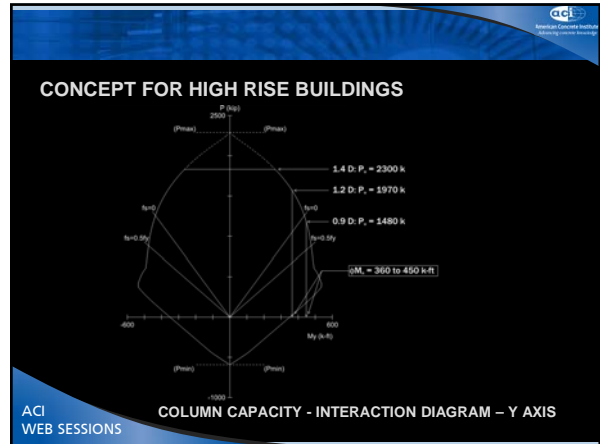
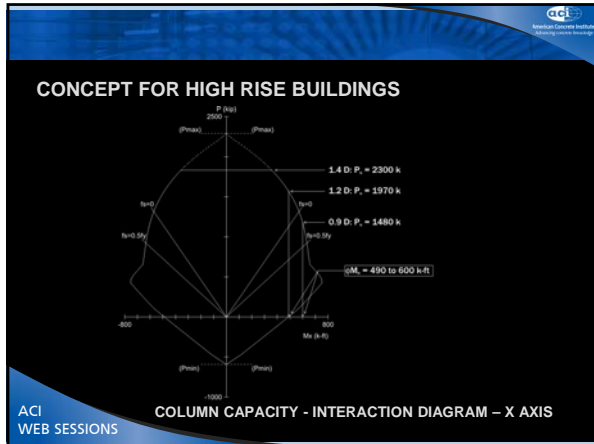
**DEFORMATION COMPATIBILITY – ACI 31-11**



21.13.3.3

21.13.4.3

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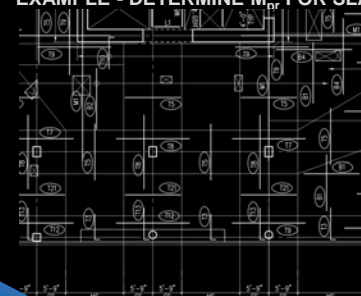


**EXAMPLE – DESIGN STEPS**

- Determine  $M_{pr}$  for Floor Framing
- Determine  $\phi P_{n,min}$  and  $\phi P_{n,max}$  for Column Based on  $\Sigma M_{pr}/2$
- Compare  $P_{u,min}$  and  $P_{u,max}$  to Acceptable Range for  $\phi P_n$
- Determine Minimum Confinement
- Check Shear Capacity Based on Minimum Confinement

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**EXAMPLE - DETERMINE  $M_{pr}$  FOR SLAB**



| MARK | TYPE        | LOCATION |
|------|-------------|----------|
| (1)  | #4 @ 12" OC | TOP      |
| (2)  | #4 @ 12" OC | TOP      |
| (3)  | #4 @ 12" OC | TOP      |
| (4)  | #4 @ 12" OC | TOP      |
| (5)  | #4 @ 12" OC | TOP      |
| (6)  | #4 @ 12" OC | TOP      |
| (7)  | #4 @ 12" OC | TOP      |
| (8)  | #4 @ 12" OC | TOP      |

ACI WEB SESSIONS **DETERMINE  $M_{pr}$**

**EXAMPLE - DETERMINE  $M_{pr}$  FOR SLAB**

$$M_{PR} = A_s(1.25f_y)d \left( 1 - 0.59 \frac{A_s f_y}{b d f'_c} \right)$$

Where:

$$b = 23(12) = 276"$$

$$d = 8 - 0.75 - 0.25 = 7"$$

$$A_s = \#4 @ 13" = \frac{(23)(12)}{13} (0.2) = 4.25 \text{ in}^2$$

$$f_y = 60 \text{ ksi}$$

$$f'_c = 6 \text{ ksi}$$

$$M_{PR} = 184 \text{ k-ft}$$

ACI WEB SESSIONS **POSTIVE MOMENT CAPACITY**

**EXAMPLE - DETERMINE  $M_{pr}$  FOR SLAB**

$$M_{PR} = A_s(1.25f_y)d \left( 1 - 0.59 \frac{A_s f_y}{b d f'_c} \right)$$

Where:

$$b = 23(12) = 276"$$

$$d = 8 - 0.75 - 0.25 = 7"$$

$$A_s = T5 + T8 = (8)\#4 + (18)\#5 = 5.58 \text{ in}^2$$

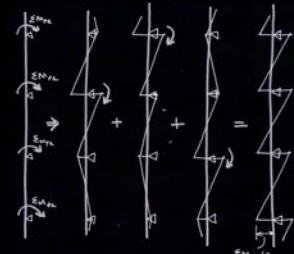
$$f_y = 60 \text{ ksi}$$

$$f'_c = 6 \text{ ksi}$$

$$M_{PR} = 238 \text{ k-ft}$$

ACI WEB SESSIONS **NEGATIVE MOMENT CAPACITY**

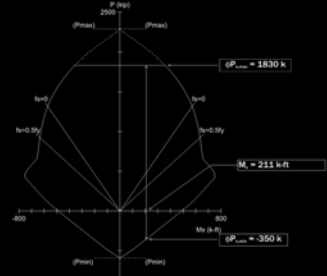
**EXAMPLE - DETERMINE AXIAL COLUMN CAPACITY**



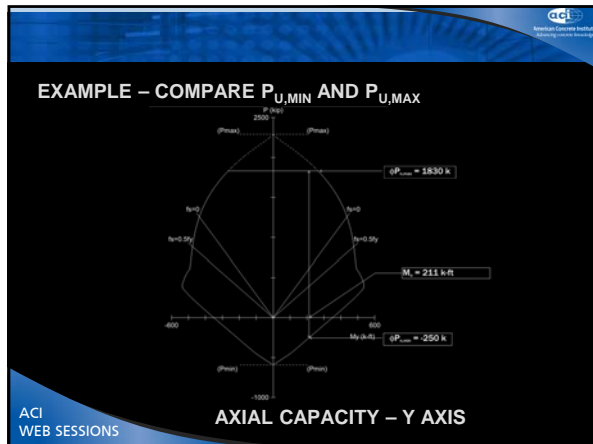
$$\Sigma M_{pr}/2 = (184 + 238) / 2 = 211 \text{ k-ft}$$

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**EXAMPLE - DETERMINE AXIAL COLUMN CAPACITY**



ACI WEB SESSIONS **AXIAL CAPACITY – X AXIS**



**EXAMPLE – COMPARE  $P_{U,MIN}$  AND  $P_{U,MAX}$**

- Minimum  $P_u$  for 18x24 column, 8 ksi, 2.54% reinforcing is 1,114 kips in column L-12 at the sixth floor.
- Maximum  $P_u$  for 18x24 column, 8 ksi, 2.54% reinforcing is 1,608 kips in column L-12 at the seventh floor.
- These demands are well within range established based on  $M_{pr}$ .

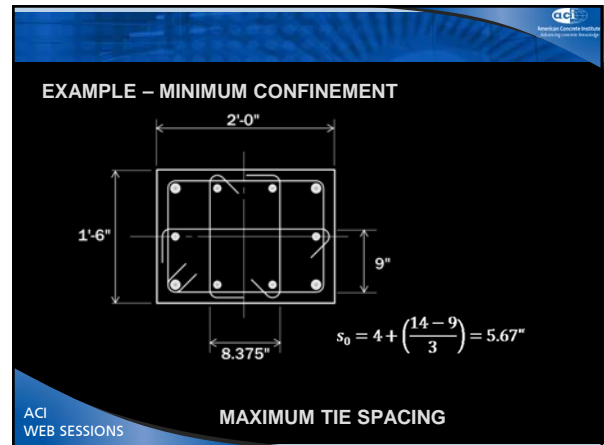
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**EXAMPLE – MINIMUM CONFINEMENT**

- Since  $P_u > 0.35P_o$ , ACI 21.13.3.3 Controls.
- Maximum Tie Spacing Is The Larger Of:
  - 6db of smallest longitudinal bar (#8) = 6 inches
  - 6 inches
  - $s_0 = 4 + \left(\frac{14 - h_x}{3}\right)$

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**MAXIMUM TIE SPACING**



**EXAMPLE – MINIMUM CONFINEMENT**

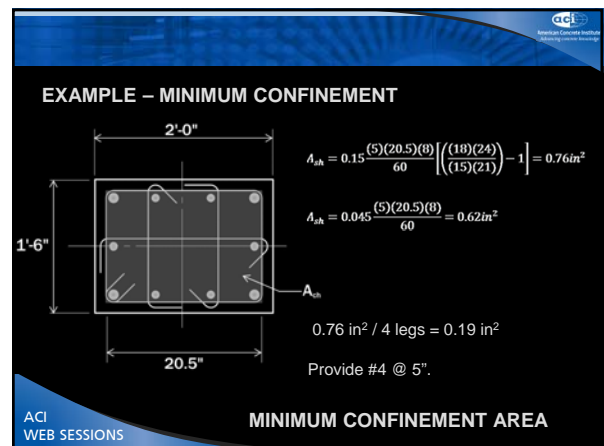
- Since  $P_u > 0.35P_o$ , ACI 21.13.3.3 Controls.
- Tie Area Is One-Half That Required by ACI 21.6.4.4:

$$A_{sh} = 0.3 \frac{s_b f'_c}{f_{yt}} \left[ \left( \frac{A_g}{A_{ch}} \right) - 1 \right]$$

$$A_{sh} = 0.09 \frac{s_b f'_c}{f_{yt}}$$

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**MINIMUM CONFINEMENT AREA**



**EXAMPLE – MINIMUM CONFINEMENT**

$$A_{gh} = 0.15 \frac{(5)(14.5)(9)}{60} \left[ \frac{(19)(24)}{(15)(21)} - 1 \right] = 0.54 \text{ in}^2$$

$$A_{gh} = 0.045 \frac{(5)(14.5)(9)}{60} = 0.44 \text{ in}^2$$

$0.54 \text{ in}^2 / 3 \text{ legs} = 0.18 \text{ in}^2$   
 Provide #4 @ 5".

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**EXAMPLE – SHEAR STRENGTH**

$V_u = \Sigma M_{pr} / 2h$   
 $V_u = (184 + 238) / 2(9.33)$   
 $V_u = 22.6 \text{ kips}$   
 #4 @ 5" Ties are okay by inspection.

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**QUESTIONS?**

#4 TIES @ 8"  
 LAP SPLICE AT FLOOR

#4 TIES @ 8"  
 #3 TIES @ 8"  
 LAP SPLICE AT MID-HEIGHT (OR 1/3 H)

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