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Advancing concrete knowledge

FRP Shear Strengthening of RC Beams

ACI Spring 2011 Convention
April 3 - 7, Tampa, FL

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Fall 2011 Seminars

These seminars, cosponsored by ACI and the Portland Cement Association (PCA), will cover all the major changes in the new edition of the **318-11 Building Code**.

DATE	LOCATION	DATE	LOCATION
September 13	Chicago, IL	November 3	Charlotte, NC
September 27	Philadelphia, PA	November 8	Boston, MA
September 29	Houston, TX	November 10	Detroit, MI
October 4	Seattle, WA	November 15	Des Moines, IA
October 6	Los Angeles, CA	November 17	Portland, OR
October 11	New York, NY	November 29	Denver, CO
October 13	Minneapolis, MN	December 1	Phoenix, AZ
October 20	Cincinnati, OH	December 6	Atlanta, GA
October 25	New Brunswick, NJ	December 8	Washington, DC
October 27	St. Louis, MO	December 13	Dallas, TX
November 1	Orlando, FL	December 15	San Francisco, CA

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FRP Shear Strengthening of RC Beams

ACI Spring 2011 Convention
April 3 - 7, Tampa, FL

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Amir Mofidi is a PhD candidate in the Department of Construction Engineering, University of Quebec, Ecole de technologie supérieure, Montreal, Quebec, Canada. His research interests include the use of fiber-reinforced polymer composites for strengthening and retrofitting concrete structures.

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Shear Strengthening of RC Beams with EB FRP: Evolutive Model versus Code

10th International Symposium on Fiber Reinforced
Polymer Reinforcement for Concrete Structures
(in conjunction with the Spring 2011 ACI Convention)

April 2-4, 2011, Marriott Tampa Waterside & Westin
Harbor Island

Amir Mofidi and Omar Chaallal

Presented by: Ahmed Godat



Université du Québec
Ecole de technologie supérieure
DRSR

FRPRCS - 10
Tampa, FL - April 2-4 2011

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Influencing Parameters

The following parameters that influence debonding of FRP are studied:

- Bond Model
- Effective Strain
- FRP Effective Anchorage Length
- FRP Effective Width
- Strip-Width to Strip-Spacing Ratio
- Transverse Steel
- Crack Pattern

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International Design Codes and Guidelines

Status of influencing factors on shear strengthening of RC beams in the current design guidelines.

FRP design guidelines	Latest revision	Influencing factors						
		Bond model	Effective strain	Anchorage length	w / s _f	Crack angle	Crack pattern	Effect of transverse steel
ACI 440.2R	2008	YES	YES	YES	NO	NO	NO	NO
CSA-S06	2006	YES	YES	YES	NO	YES	NO	NO
CSA-S06	2002	NO	YES	NO	NO	NO	NO	NO
AS-TG 9.3	2001	NO	YES	NO	NO	YES	NO	NO
EN-12501	2004	YES	YES	YES	YES	YES	NO	NO
EN-12501 (CEN)	2008	YES	YES	YES	YES	YES	NO	NO

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Research Significance

The main impetus to carry out current study are:

- to study the effect of parameters which have been proven to influence the shear resistance of EB FRP, but which have not been sufficiently documented in the guidelines,
- to develop a transparent and evolutive design model for the shear resistance of FRP-strengthened beams which fail by FRP debonding.

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Influencing Parameters (cont'd)

Bond Model:

To study the mechanism of FRP debonding from concrete, a reliable bonding model is required.

$$P_{frp} = w_{frp} \times L_e \times \tau_{eff}$$

	Advantage	disadvantage
Holzenträger (1994)		
Maeda et al. (1997)	The method is based on the assumption that the FRP bond strength is proportional to the effective strain of FRP.	It is not applicable for FRP-strengthened beams with high FRP content.
Khalifa et al. (1998)	It is based on the assumption that the FRP bond strength is proportional to the effective strain of FRP.	It is not applicable for FRP-strengthened beams with high FRP content.
Neubauer and Rostásy (1997)	It is based on the assumption that the FRP bond strength is proportional to the effective strain of FRP.	It is not applicable for FRP-strengthened beams with high FRP content.
Chen and Teng (2001)	It is based on the assumption that the FRP bond strength is proportional to the effective strain of FRP.	It is not applicable for FRP-strengthened beams with high FRP content.

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Influencing Parameters (cont'd)

Effective Strain:

- Assuming that FRP carries only normal stresses in the principal direction, FRP may be treated by analogy to internal steel.
- All the FRP strips intersected by the selected shear crack are assumed to contribute the same FRP effective strain.
- Most of design models or equations basically use similar design analogy with different definitions of the effective strain.

$$V_f = \frac{2t_f \cdot w_f \cdot \epsilon_{fe} \cdot E_f \cdot (\cot \theta + \cot \alpha) \cdot \sin \alpha \cdot d_f}{s_f}$$

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Influencing Parameters (cont'd)

FRP Effective Anchorage Length:

- Beyond a certain FRP bond-length threshold, increasing bond length does not result in an increase in the ultimate bond strength.

Note: In NLFM equation f_c is assumed to be equal to 5 MPa.

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Influencing Parameters (cont'd)

FRP Effective Width:

- Only the FRP fibers that have an anchorage length greater than the FRP effective length remain adequately anchored.
- The width of the FRP sheet, w_f , is replaced by an effective width, w_{fe} .

$w_{fe} = d_f - L_e$

Effective width of FRP in RC beam strengthened with side-bonded FRP

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Influencing Parameters (cont'd)

Strip-Width to Strip-Spacing Ratio:

- Previous FRP-to-concrete direct pull-out tests have shown that the width of the FRP sheets bonded to a concrete block has a significant effect on the maximum bond strength of the FRP.
- According to experimental research studies as the FRP sheets become narrower, the bond strain increases.

$$k_p = \sqrt{1.125 \times \frac{2 - \frac{b_f}{b_c}}{1 + \frac{b_f}{400}}}$$

Holzkaempfer (1994) and Neubauer and Rostasy (1997)

$$\beta_w = \sqrt{\frac{2 - \frac{w_f}{s_f}}{1 + \frac{w_f}{s_f}}}$$

Chen and Teng (2001).

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Influencing Parameters (cont'd)

Transverse Steel:

- It has been clearly established that the effectiveness of the strengthening contribution of FRP to shear resistance depends on the amount of internal shear-steel reinforcement.
- None of the guidelines has yet considered in their formulae the effect of transverse steel on V_f .

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Influencing Parameters (cont'd)

Cracking Pattern:

Experimental observations clearly showed that in RC beams with transverse reinforcement the shear-crack pattern tends to be distributed over a large width compared with the pattern in RC beams with no or low shear reinforcement.

No transverse reinforcement

Transverse steel reinforcement

EB U-Jacket FRP sheet

Transverse steel reinforcement + EB U-Jacket FRP sheet

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Influencing Parameters (cont'd)

```

    graph TD
      A[Transverse Reinforcement Ratio (Steel + FRP) ↑] --> B[Crack Pattern Distribution ↑]
      B --> C[FRP Anchorage Length ↓]
      C --> D[Amount of FRP fibers longer than (or equal to) effective anchorage length ↓]
      D --> E[Bond Strength between FRP and Concrete ↓]
      E --> F[EB FRP contribution to the shear resistance ↓]
  
```

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Proposed Model (cont'd)

(a) FRP U-jacket actual width

(b) FRP U-jacket effective width

(c) Side bonded FRP actual width

(d) Side bonded FRP effective width

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Proposed Model (cont'd)

○ U-jacket FRP-debonded
 ● Side-bonded FRP-debonded
 ▲ U-jacket concrete crushing

$y = 0.43x^{0.65}$
 $y = 0.6x^{0.5}$

- In the calculation of w_{eff} , it is assumed that the cracking pattern changes with the amount of internal steel and external FRP shear reinforcement as measured by their respective rigidities.

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Proposed Model (cont'd)

- The effective width is then calibrated as a function of $(\rho_f \cdot E_f + \rho_s \cdot E_s)$ for beams strengthened with a continuous U-jacket and side-bonding configurations.

$$w_{fe} = \frac{0.6}{\sqrt{\rho_f \cdot E_f + \rho_s \cdot E_s}} \times d_f \text{ for U-Jacket}$$

$$w_{fe} = \frac{0.43}{\sqrt{\rho_f \cdot E_f + \rho_s \cdot E_s}} \times d_f \text{ for side bonded}$$
- The cracking modification factor can then be calculated as:

$$k_c = \frac{w_{fe}}{d_f} = \frac{0.6}{\sqrt{\rho_f \cdot E_f + \rho_s \cdot E_s}} \text{ for U-Jackets}$$

$$k_c = \frac{w_{fe}}{d_f} = \frac{0.43}{\sqrt{\rho_f \cdot E_f + \rho_s \cdot E_s}} \text{ for side bonded}$$

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Proposed Model (cont'd)

- The effects of k_c to consider the effect of cracking pattern and that of k_w to incorporate the w_f / s_f ratio of the FRP strips are considered in the equation for effective strain:

$$\epsilon_{fe} = \frac{k_c \cdot k_L \cdot k_w \cdot \tau_{eff} \cdot L_e}{t_f \cdot E_f} = 0.31 k_c \cdot k_L \cdot k_w \sqrt{\frac{f_c'}{t_f E_f}} \leq \epsilon_{fu}$$
- The shear contribution of FRP, V_f , can be calculated as a function of ϵ_{fe} using the following equation:

$$V_f = \frac{2t_f \cdot w_f \cdot \epsilon_{fe} \cdot E_f \cdot (\cot \theta + \cot \alpha) \cdot \sin \alpha \cdot d_f}{s_f}$$

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Validation of the Proposed Model

$R^2 = 0.61$

○ Side bonded-Proposed model
 ■ U-Jacket-Proposed model

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Validation of the Proposed Model

$R^2 = 0.37$

○ Side bonded-Proposed model
 ■ U-Jacket-Proposed model

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Validation of the Proposed Model (cont'd)

Applying k_c to V_f calculated using the ACI 440.2R 2008, fib - TG 9.3 2001, CAN/CSA-S806 2002, HB 305 2008 (CIDAR 2006), and CNR-DT200 2004 guidelines resulted in a significant improvement on the accuracy of the calculated results for all the mentioned guidelines.

Design Code	R^2 Value
Proposed model	0.37
CSA-S806	0.06
ACI 440-2R	0.42
fib-TG 9.3	0.35
CNR-DT200	0.42
HB 305 (CIDAR)	0.36
Proposed model (with k_c)	0.61

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Conclusions

- A new design approach has been proposed for calculating the shear contribution of FRP, taking into consideration the effect of transverse steel on the EB FRP contribution in shear.
- The proposed model showed an acceptable correlation with experimental results in comparison with the current guidelines.

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Acknowledgement

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- The Fonds québécois de la recherche sur la nature et les technologies (FQRNT),
- The Ministère des Transports du Québec (MTQ).

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Thanks for your attention

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FIBER-REINFORCED POLYMER REINFORCEMENT FOR CONCRETE STRUCTURES
FRP-RCS10 April 2-4, 2011 - Tampa, Florida, USA

PARAMETRIC STUDIES OF THE NSM FRP STRIPS SHEAR STRENGTH CONTRIBUTION TO A RC BEAM

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MECHANICAL MODEL : 1 – Physical Aspects
POSSIBLE FAILURE MODES OF A SINGLE NSM FRP STRIP

In analogy with the fastening technology, 4 possible failure modes can be foreseen.

SCHEMATIZATION OF R.C. BEAM WEB AND NSM FRP STRIPS

The strengthened web can be seen as a prism divided in two parts by the Critical Diagonal Crack (CDC) which can be schematized as an inclined plane intersecting the strips.

The two resulting web parts are sawn together by the FRP strips.

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Parametric studies of the NSM FRP strips shear strength contribution to a RC beam

FRP-RCS10 - Tampa - Florida
2-4 Aprile 2011

DEVELOPED MECHANICAL MODEL: 2 – Physical Aspects

$[\alpha = 45^\circ; \beta = 45^\circ; s_j \rightarrow \infty]$

SCHEME OF A SINGLE FRP STRIP

$$V_f^{p,cf} = \int_{C_f} (f_{cm} \cdot \sin \alpha_f) \cdot dC_f$$

Semi-conical tensile fracture capacity is evaluated by spreading the average concrete tensile strength f_{cm} throughout the semi-conical surface C_f and integrating.

INTERACTION AMONG ADJACENT STRIPS

By reducing the strips spacing, the adjacent strips semi-conical fracture surfaces overlap and the overall fracture surface progressively becomes smaller than the mere summation of each of them.

The components of f_{cm} orthogonal to the web faces are **balanced only from an overall point of view but not locally**. This justifies the spalling of the concrete cover which was observed experimentally.

$\theta = \beta = 45^\circ; s_j \rightarrow 0.0$

$f_{cm} = f_{cm} \cdot \sin \alpha$

components of f_{cm} parallel and orthogonal to the web faces

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MECHANICAL MODEL: 3 – Some Computational Aspects

$x_{f,ik} \cdot N_{f,ik} \cdot i_{f,ik}$

Main flow chart

```

    graph TD
      Start([Start]) --> Input[Input Parameters]
      Input --> Init[Initial geometry to crack]
      Init --> Det[Detect and store general information]
      Det --> Det2[Detect number of bond steps]
      Det2 --> Init2[Initialize vector]
      Init2 --> Build[Build and initialize the following]
      Build --> Calc[Calculate]
      Calc --> Calc2[Calculate and store imposed end slip]
      Calc2 --> Calc3[Calculate]
      Calc3 --> Calc4[Calculate]
      Calc4 --> Calc5[Calculate]
      Calc5 --> Calc6[Calculate]
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      Calc99 --> Calc100[Calculate]
      Calc100 --> End([End])
  
```

During the loading process of a beam subject to shear, after the occurrence of the Critical Diagonal Crack, the two parts of the beam start moving apart by pivoting around the CDC end (point E).

The strips oppose this movement by anchoring to the surrounding concrete to which they transfer, through bond stresses, the force originating at the intersection with the CDC and due to the imposed end slip.

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MECHANICAL MODEL: 4 – Computational Aspects

Possible geometrical configurations taken into consideration

In order to single out the range $[V_{max} - V_{min}]$ of analytical values, the following three possible geometrical configurations were considered:

1. The first strip is placed at a distance equal to the spacing s_j from the assumed crack origin O;
2. An even number of strips are placed symmetrically with respect to the axis of the crack;
3. An odd number of strips are placed so that the central one gets the maximum available bond length.

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MECHANICAL MODEL: 5 – Single Strip Contribution

Iteration and search for the equilibrium condition

$\theta = 45^\circ; \beta = 45^\circ; s_j \rightarrow \infty; [h, h_c] \rightarrow \infty$

It can happen that, for a certain value of the imposed end slip, after the formation of some successive and co-axial semi-conical fractures, the portion of the strip still adhered to concrete, fails by debonding since the diagram of the progressive bond-transferred force remains confined beneath the diagram of the progressive concrete fracture capacity.

It can also happen, mainly for small resisting bond lengths, and for low concrete strength, that the fracture mechanism reach the strip's free end, so that the ultimate configuration is composed of a semi-cone whose height is equal to the initial available bond length.

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MECHANICAL MODEL: 6 – Concrete Fracture Capacity

General case: strips are not orthogonal to the Critical Diagonal Crack

$\theta = 45^\circ; \beta = 90^\circ; s_j \rightarrow 0; [h, h_c] \rightarrow 0$

The evaluation of the concrete semi-conical fracture capacity can be reduced the evaluation of the area of the semi-ellipse intersection of the semi-cone with the critical diagonal crack.

$$V_f^{p,cf} = \int_{C_f} (f_{cm} \cdot \sin \alpha_f) \cdot dC_f$$

$$V_f^{p,cf} = \int_{C_f} (f_{cm} \cdot \sin \alpha_f) \cdot dC_f$$

$$dE_{\beta} = (A_{\beta}^{int} + A_{\beta}^{ext})$$

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EMPLOYMENT OF BOND AND LOSS OF BOND (BOND; DEBONDING)

1) Local bond stress-slip relationship: physical phenomena occurring in sequence, within the adhesive layer, by increasing the imposed end slip

The initial strength is due to the micro-mechanical and chemical properties of the materials involved. It is the average of the physical entities encountered in sequence by stresses flowing from the strip to the surrounding concrete: 1) adhesion at the strip-adhesive interface, 2) cohesion within the adhesive and 3) adhesion at the adhesive-concrete interface.

2) The governing differential equation, considering a pull-out scheme, has been written fulfilling equilibrium, kinematic compatibility and constitutive laws.

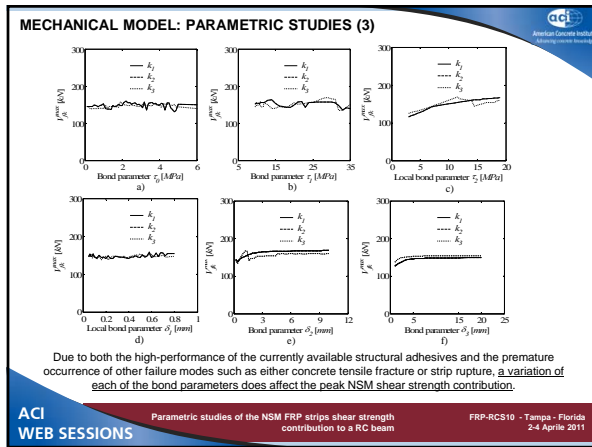
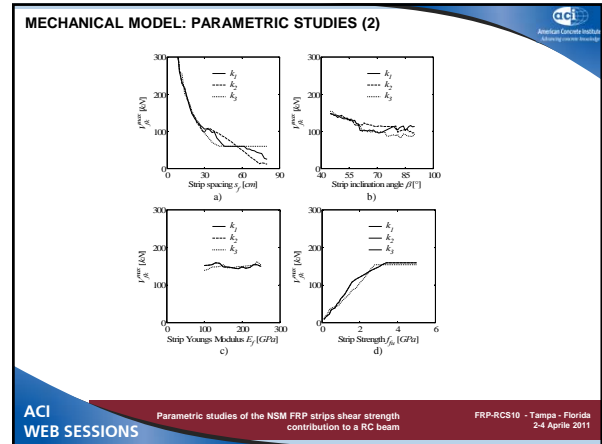
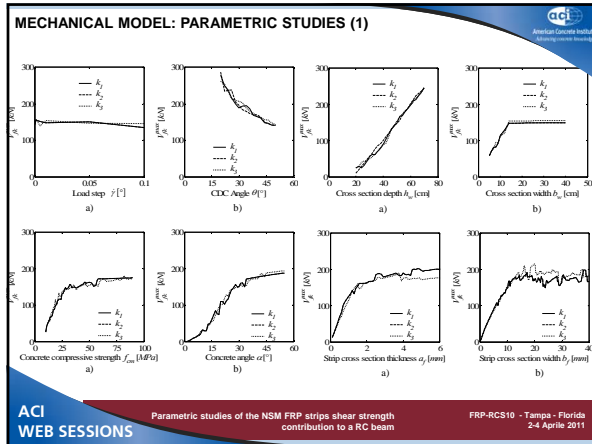
3) Governing differential equation for an infinite resisting bond length:

Equilibrium: $\frac{d\sigma_f(x)}{dx} - \tau(x) \frac{L_f}{A_f} = 0$ $\sigma_f(x) \cdot A_f + \sigma_c(x) \cdot A_c = 0$

Constitutive laws: $\tau = \tau(\delta)$ $\sigma_f = E_f \frac{du_f}{dx}$ $\sigma_c = E_c \frac{du_c}{dx}$ $\frac{d^2\delta}{dx^2} - \tau[\delta(x)] \cdot J_1 = 0$

Kinematic compatibility: $\delta(x) = u_f(x) - u_c(x)$ with: $J_1 = \frac{L_f}{A_f} \left(\frac{1}{E_f} + \frac{A_f}{A_c \cdot E_c} \right)$

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Thank you for your attention

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Let me invite you to attend the 6th International Conference on FRP Composites in Civil Engineering - CICE2012 which will be held in the "Eternal City" of Rome, in ITALY

Further information at www.cice2012.it

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[!\[\]\(a6b9d537ade5cf45a66ee3a813e9094b_img.jpg\)](#) [!\[\]\(ec53459f38187785891e752376d79262_img.jpg\)](#) [!\[\]\(9f131dd88db234ebbfbe2fbc2cfedb95_img.jpg\)](#)

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